



SHORT CIRCUIT STUDIES



Short circuit study

Requirements:

1. Determining the fault level at buses
2. Selection of breaker ratings
3. Protective device co-ordination



Symmetrical components

Unbalanced system of 'n' related phasors can be resolved to 'n' system of balanced phasors.

In each balanced phasor, angle between two phasors and magnitude of each phasor are equal.

Phase Quantities: I_a , I_b & I_c and

Sequence components are :

I_{a1} stands for Positive sequence current.

I_{a2} stands for Negative sequence current.

I_{a0} stands for Zero sequence current.



Sequence components

$I_{a1}, I_{b1} \text{ \& } I_{c1}$: Same phase sequence as $I_a, I_b \text{ \& } I_c$

$I_{a2}, I_{b2}, \text{ \& } I_{c2}$: Opposite phase sequence as $I_a, I_b \text{ and } I_c$

$I_{a0}, I_{b0}, \text{ \& } I_{c0}$: All in-phase

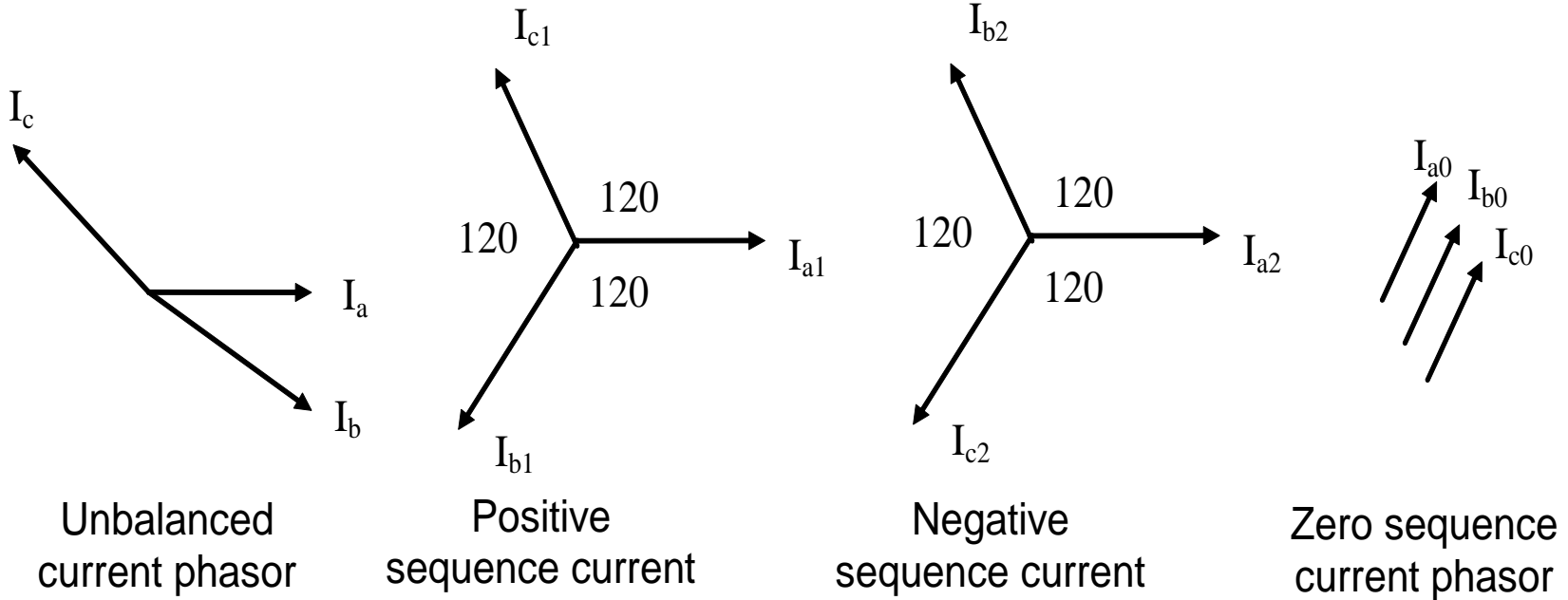
$$I_a = I_{a1} + I_{a2} + I_{a0}$$

$$I_b = I_{b1} + I_{b2} + I_{b0}$$

$$I_c = I_{c1} + I_{c2} + I_{c0}$$



Sequence components





Similarly for voltages:

$$\begin{aligned}V_a &= V_{a1} + V_{a2} + V_{a0} \\V_b &= V_{b1} + V_{b2} + V_{b0} \\V_c &= V_{c1} + V_{c2} + V_{c0}\end{aligned}$$

$$\begin{bmatrix} V_a \\ V_b \\ V_c \end{bmatrix} = \begin{bmatrix} 1 & 1 & 1 \\ a^2 & a & 1 \\ a & a^2 & 1 \end{bmatrix} \begin{bmatrix} V_{a1} \\ V_{a2} \\ V_{a0} \end{bmatrix}$$



$$T_{sp} = \begin{bmatrix} \mathbf{1} & \mathbf{1} & \mathbf{1} \\ a^2 & a & 1 \\ a & a^2 & 1 \end{bmatrix}$$

$$a = 1\angle 120, \quad a^2 = 1\angle 240 = 1\angle -120$$

and sp = Sequenceto phase

$$T_{ps} = \frac{1}{3} \begin{bmatrix} 1 & a & a^2 \\ 1 & a^2 & a \\ 1 & 1 & 1 \end{bmatrix}$$

ps = Phaseto sequence



$$\begin{bmatrix} V_{a1} \\ V_{a2} \\ V_{a0} \end{bmatrix} = \frac{1}{3} \begin{bmatrix} 1 & a & a^2 \\ 1 & a^2 & a \\ 1 & 1 & 1 \end{bmatrix} \begin{bmatrix} V_a \\ V_b \\ V_c \end{bmatrix}$$

$$V_{a0} = \frac{1}{3} (V_a + V_b + V_c)$$

$$V_{aL-L} + V_{bL-L} + V_{cL-L} = 0 \text{ always}$$

Therefore no zero sequence exists in line voltage phasor.

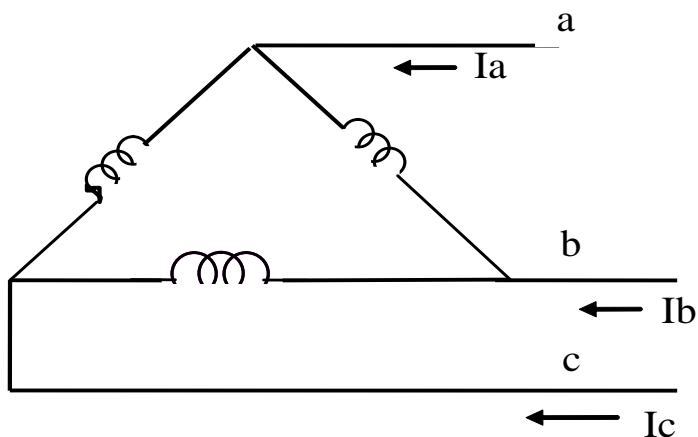
Since phase voltage sum is not always zero, in the phase voltage phasor, the zero sequence voltage exists.

Sequence Currents:



$$\begin{bmatrix} I_{a1} \\ I_{a2} \\ I_{a0} \end{bmatrix} = \frac{1}{3} \begin{bmatrix} 1 & a & a^2 \\ 1 & a^2 & a \\ 1 & 1 & 1 \end{bmatrix} \begin{bmatrix} I_a \\ I_b \\ I_c \end{bmatrix}$$

$$I_{a0} = \frac{1}{3} [I_a + I_b + I_c]$$

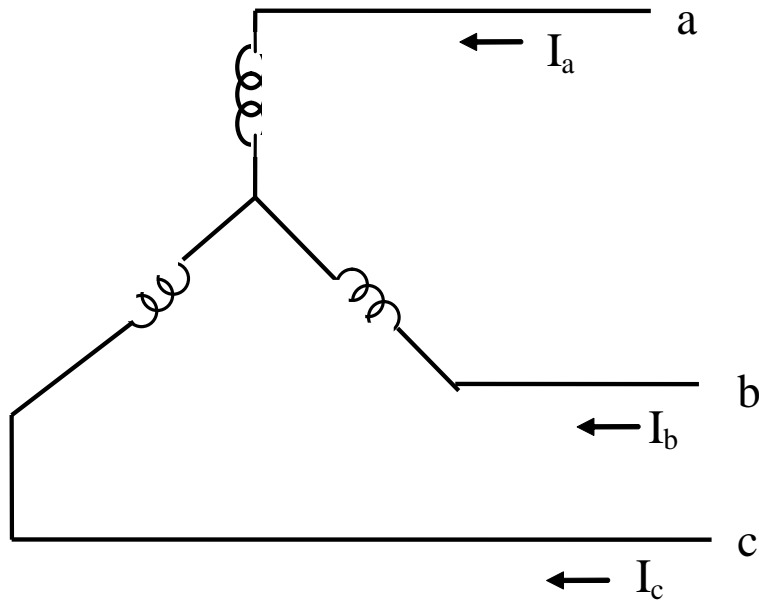


$$I_a + I_b + I_c = 0$$

Therefore no zero sequence current flows into delta connection.

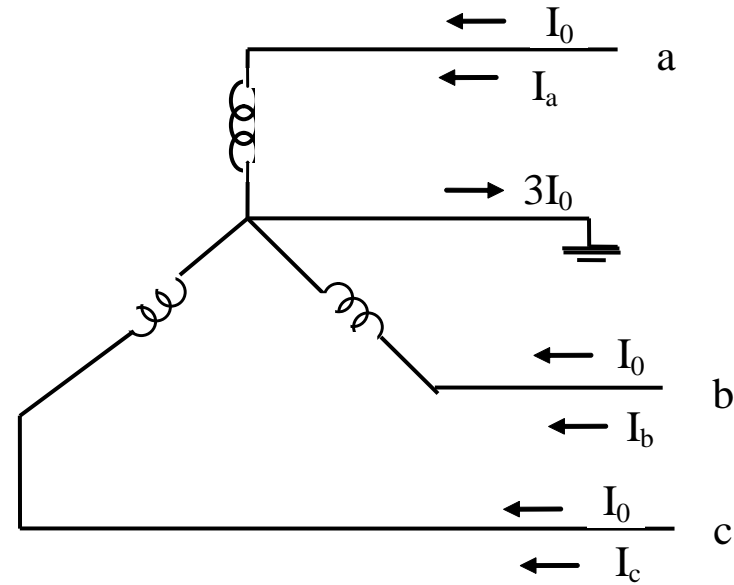


Star connection



$I_a + I_b + I_c = 0$, Therefore no zero sequence current flows into star connection

Star grounded

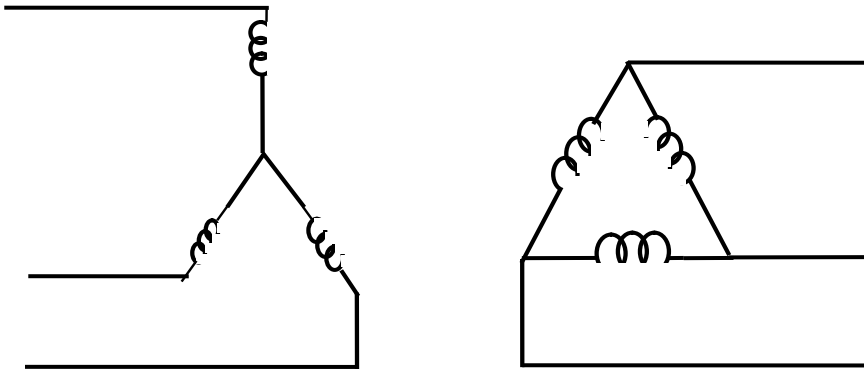


$I_a + I_b + I_c$ may not be zero. Hence path always exists for zero sequence currents.

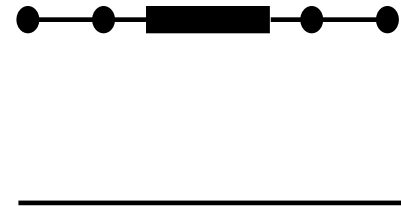


Transformer sequence impedance diagram

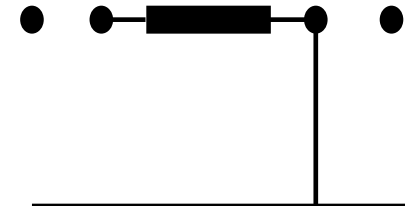
Star - Delta



+ve and -ve



Zero



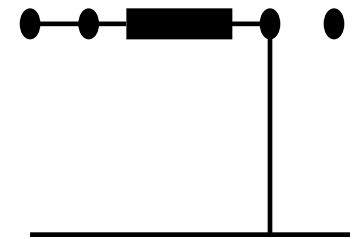
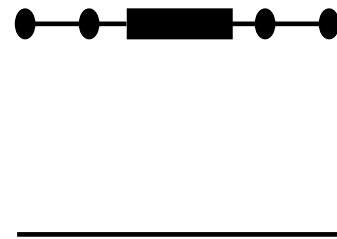
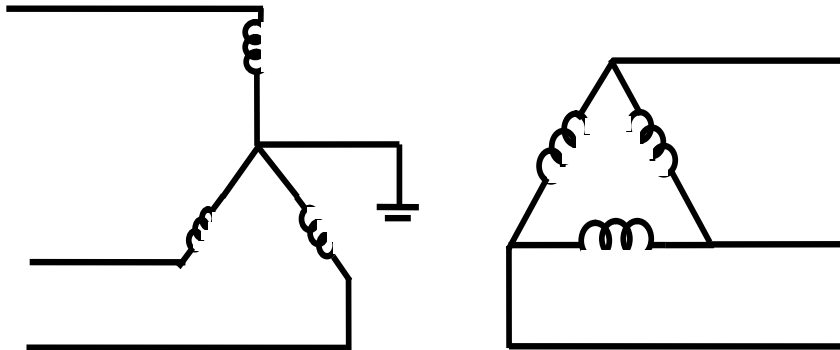


Transformer sequence impedance diagram

Star grounded-Delta

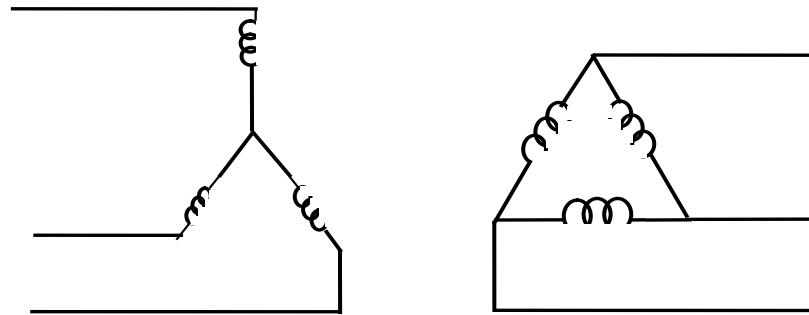
+ve and -ve

Zero





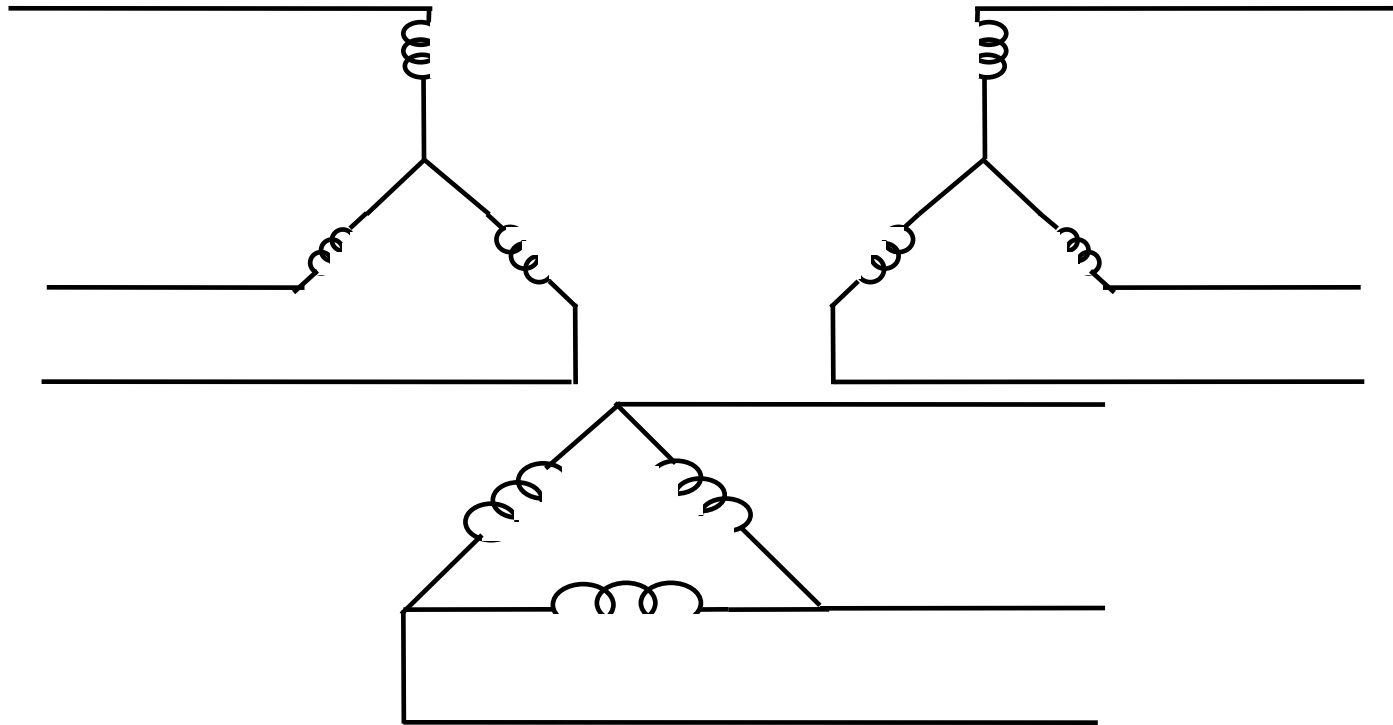
Transformer Connection to reduce the 3rd harmonic content (flow)



- Inrush current (Magnetising current)
- 3rd harmonic content : 40 to 50 % of fundamental.
- No 3rd harmonic current.

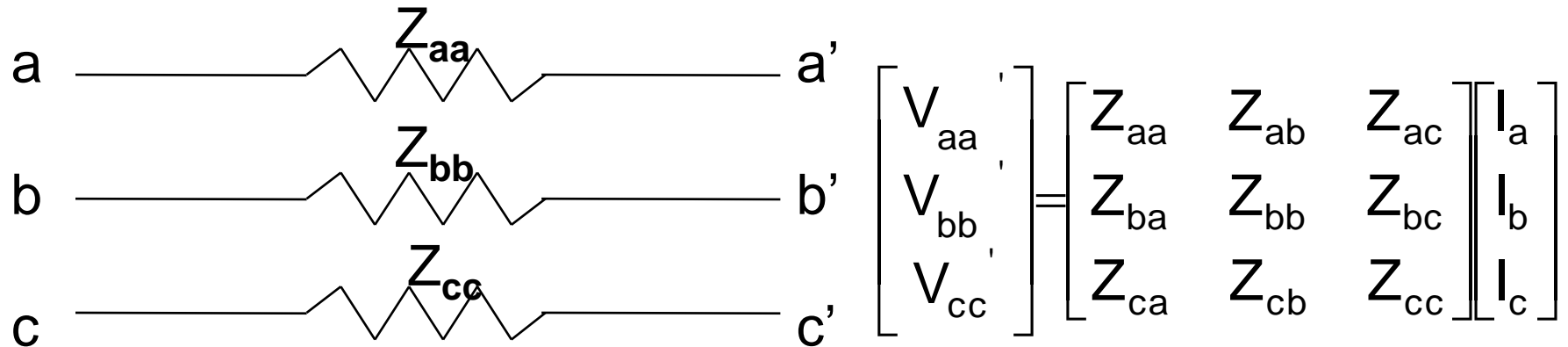


Three winding Transformer





Sequence Impedance



Let $Z_{aa} = Z_{bb} = Z_{cc} = Z_s$ and $Z_{ab} = Z_{ac} = Z_{ba} = Z_{bc} = Z_{ca} = Z_{cb} = Z_m$

$$V_s = [Z] \cdot T_{sp} \cdot I_s$$



$$\begin{bmatrix} 1 & 1 & 1 \\ a^2 & a & 1 \\ a & a^2 & 1 \end{bmatrix} \begin{bmatrix} V_{a1} \\ V_{a2} \\ V_{a0} \end{bmatrix} = \begin{bmatrix} Z_s & Z_m & Z_m \\ Z_m & Z_s & Z_m \\ Z_m & Z_m & Z_s \end{bmatrix} \begin{bmatrix} 1 & 1 & 1 \\ a^2 & a & 1 \\ a & a^2 & 1 \end{bmatrix} \begin{bmatrix} I_{a1} \\ I_{a2} \\ I_{a0} \end{bmatrix}$$

$$\begin{bmatrix} V_{a1} \\ V_{a2} \\ V_{a0} \end{bmatrix} = \begin{bmatrix} Z_s - Z_m & 0 & 0 \\ 0 & Z_s - Z_m & 0 \\ 0 & 0 & Z_s + 2Z_m \end{bmatrix} \begin{bmatrix} I_{a1} \\ I_{a2} \\ I_{a0} \end{bmatrix}$$

$$Z_{1,2,0} = Z_s = \begin{bmatrix} Z_s - Z_m & 0 & 0 \\ 0 & Z_s - Z_m & 0 \\ 0 & 0 & Z_s + 2Z_m \end{bmatrix}$$

$$\begin{aligned} V_{a1} &= (Z_s - Z_m) I_{a1} \\ V_{a2} &= (Z_s - Z_m) I_{a2} \\ V_{a0} &= (Z_s + 2Z_m) I_{a0} \end{aligned}$$



For Rotating Machines

$Z_{a,b,c}$ is not symmetric. Even then, the $Z_{1,2,0}$ is diagonalized.

Exercise:

$$\begin{bmatrix} V_a \\ V_b \\ V_c \end{bmatrix} = \begin{bmatrix} Z_s & Z_{m1} & Z_{m2} \\ Z_{m2} & Z_s & Z_{m1} \\ Z_{m1} & Z_{m2} & Z_s \end{bmatrix} \begin{bmatrix} I_a \\ I_b \\ I_c \end{bmatrix}$$

Find the expression for $Z_{1,2,0}$
and Prove that it is a diagonal matrix:

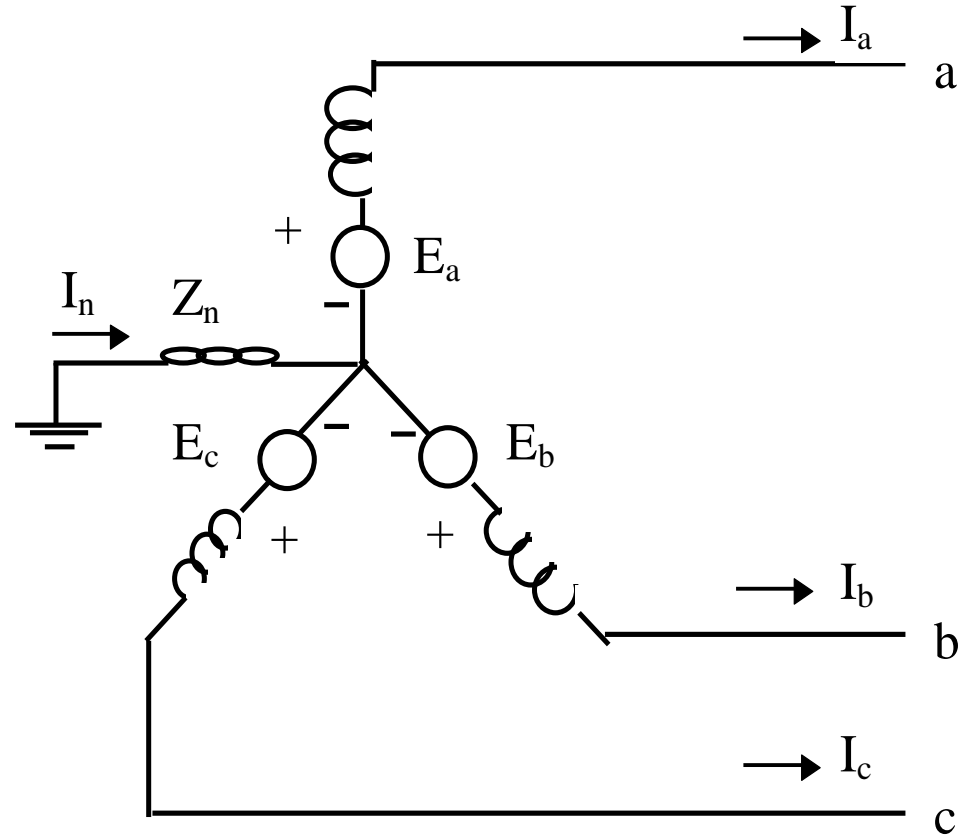


Advantages of Sequence Component

- De-couples the equation to +ve, -ve and zero sequence and hence easy to solve.
- End conditions can be applied easily for fault studies in sequence components.
- Since the equations are de-coupled, same set of subroutines can be called for solving the +ve, -ve and zero sequence system.

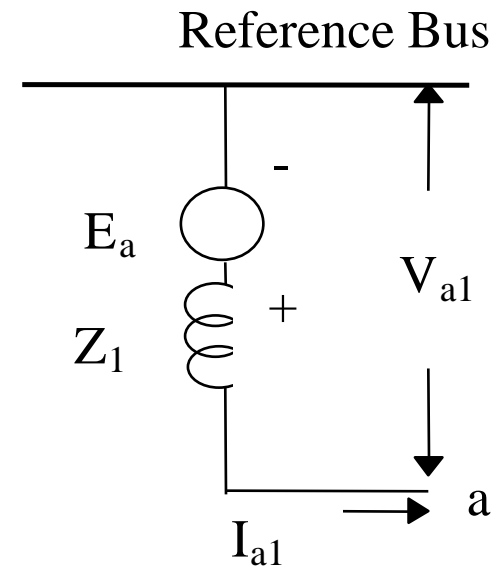
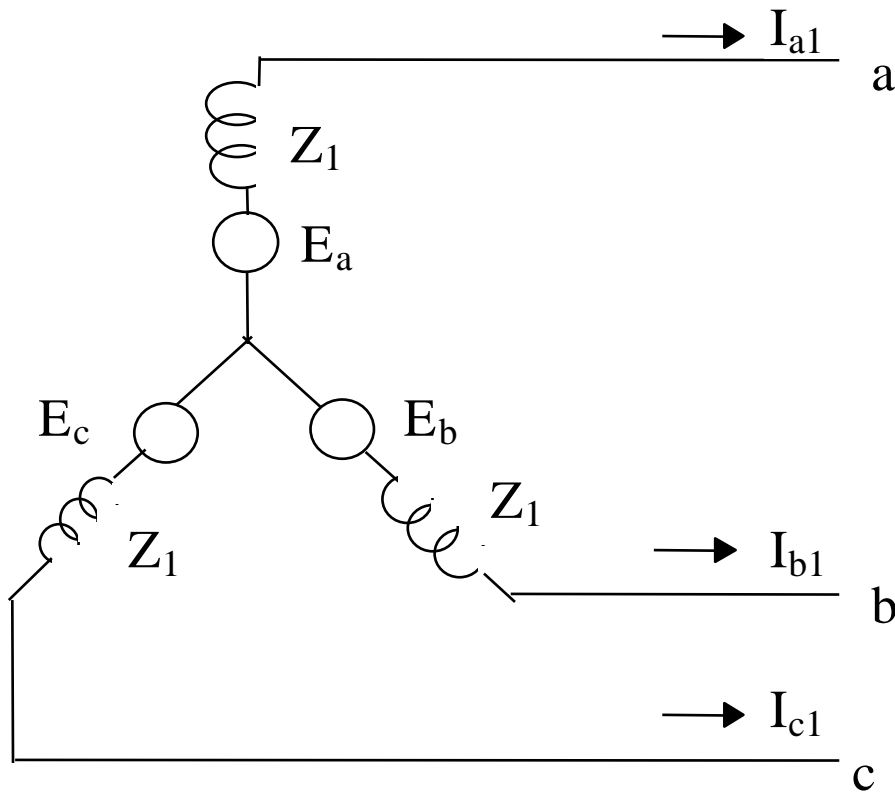


Steady State





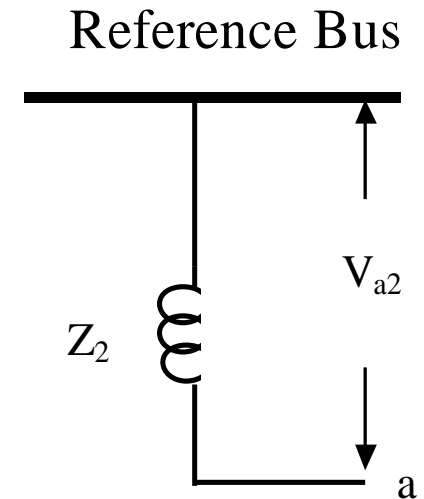
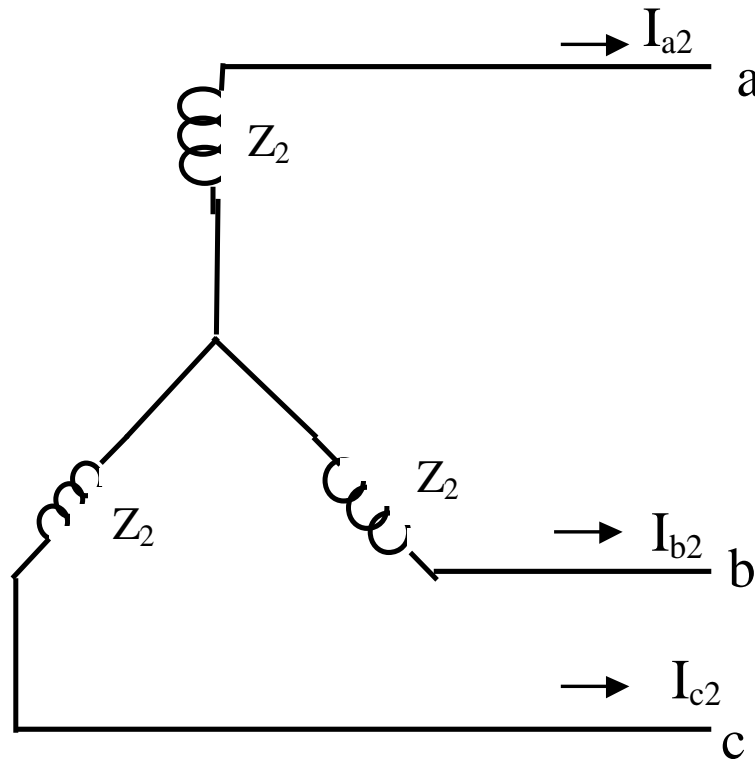
Positive Sequence Network



$$V_{a1} = E_a - I_{a1} Z_1$$



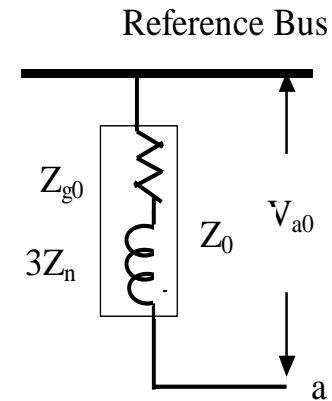
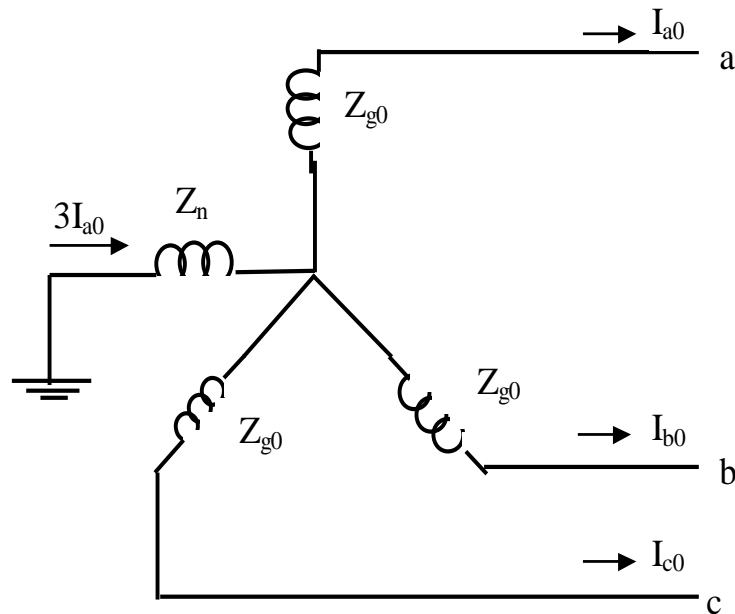
Negative Sequence Network



$$V_{a2} = - I_{a2} Z_2$$



Zero Sequence Network



$$V_{a3} = -I_{a0}Z_0$$

Generator impedance for fault study :



1. Transient (x_d') or sub-transient (x_d'') is considered for positive sequence.
2. X_2 i.e. Negative sequence which is close to x_d'' . (Approximately).
3. X_0 is small 0.1 to 0.7 times x_d''

Typical values on own rating :

X_d 100 to 200 %

X_q 60 to 200 %

X_d' 21 to 41 %

X_d'' 13 to 30 %

$X_2 \cong X_d''$

Transmission line :



Positive sequence impedance = Negative sequence impedance

Zero sequence impedance depends upon : Return path, Ground wires and Earth resistivity.

Zero sequence reactance is approximately 2 - 2.5 times positive sequence impedance.

R_0 is usually large. May be 5 to 10 times also.

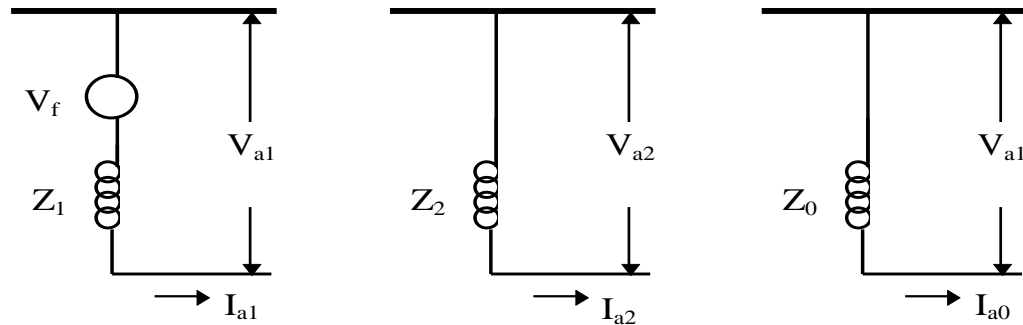
B_0 is 65 to 80 % of B positive sequence

Transformers :

All are equal i.e. $Z_{pt} = Z_{nt} = Z_{zt}$ for transformer.

$Z_{zt} \cong 90\%$ of Z_{pt} , if magnetising branch is neglected.

Fault Representation:



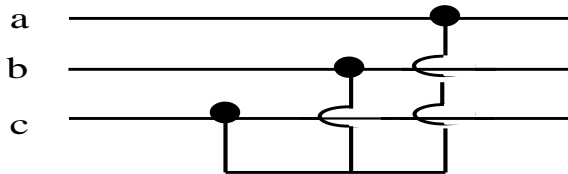
$$V_{a1} = V_f - Z_1 \cdot I_{a1}$$

$$V_{a2} = -Z_2 \cdot I_{a2}$$

$$V_{a0} = -Z_0 \cdot I_{a0}$$

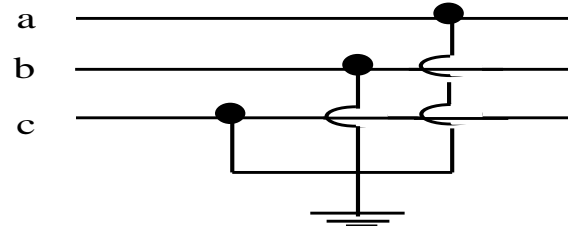
$$\begin{bmatrix} V_{a1} \\ V_{a2} \\ V_{a0} \end{bmatrix} = \begin{bmatrix} V_f \\ 0 \\ 0 \end{bmatrix} - \begin{bmatrix} Z_1 & 0 & 0 \\ 0 & Z_2 & 0 \\ 0 & 0 & Z_0 \end{bmatrix} \begin{bmatrix} I_{a1} \\ I_{a2} \\ I_{a0} \end{bmatrix}$$

Three phase fault representation:



$$\begin{aligned} V_{ab} &= 0 \\ V_{bc} &= 0 \\ V_{ca} &= 0 \end{aligned}$$

$$\begin{aligned} V_a &= 0 \\ V_b &= 0 \\ V_c &= 0 \end{aligned}$$



$$\begin{aligned} V_{a1} &= 0 \\ V_{a2} &= 0 \\ V_{a0} &= 0 \end{aligned}$$

$$\begin{bmatrix} 0 \\ 0 \\ 0 \end{bmatrix} = \begin{bmatrix} V_f \\ 0 \\ 0 \end{bmatrix} - \begin{bmatrix} Z_1 & 0 & 0 \\ 0 & Z_2 & 0 \\ 0 & 0 & Z_0 \end{bmatrix} \begin{bmatrix} I_{a1} \\ I_{a2} \\ I_{a0} \end{bmatrix}$$

Three phase fault representation:



$$I_{a1} = V_f / Z_1 \quad , \quad I_{a2} = 0 \quad , \quad I_{a0} = 0$$

$$I_a = I_{a1}$$

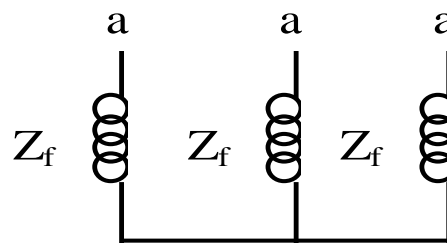
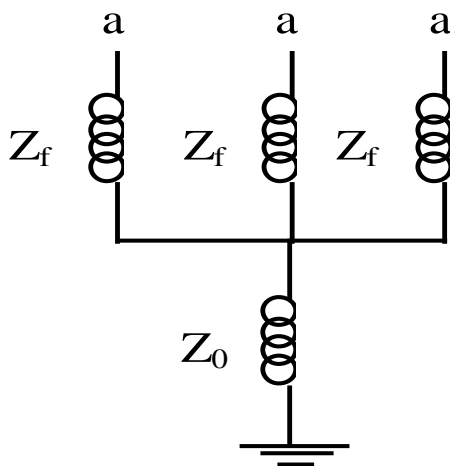
$$I_b = a^2 I_{a1}$$

$$I_c = a I_{a1}$$

$$\begin{bmatrix} I_a \\ I_b \\ I_c \end{bmatrix} = \begin{bmatrix} 1 & 1 & 1 \\ a^2 & a & 1 \\ a & a^2 & 1 \end{bmatrix} \begin{bmatrix} I_{a1} \\ I_{a2} \\ I_{a0} \end{bmatrix}$$

$$| I_a | = | I_b | = | I_c |$$

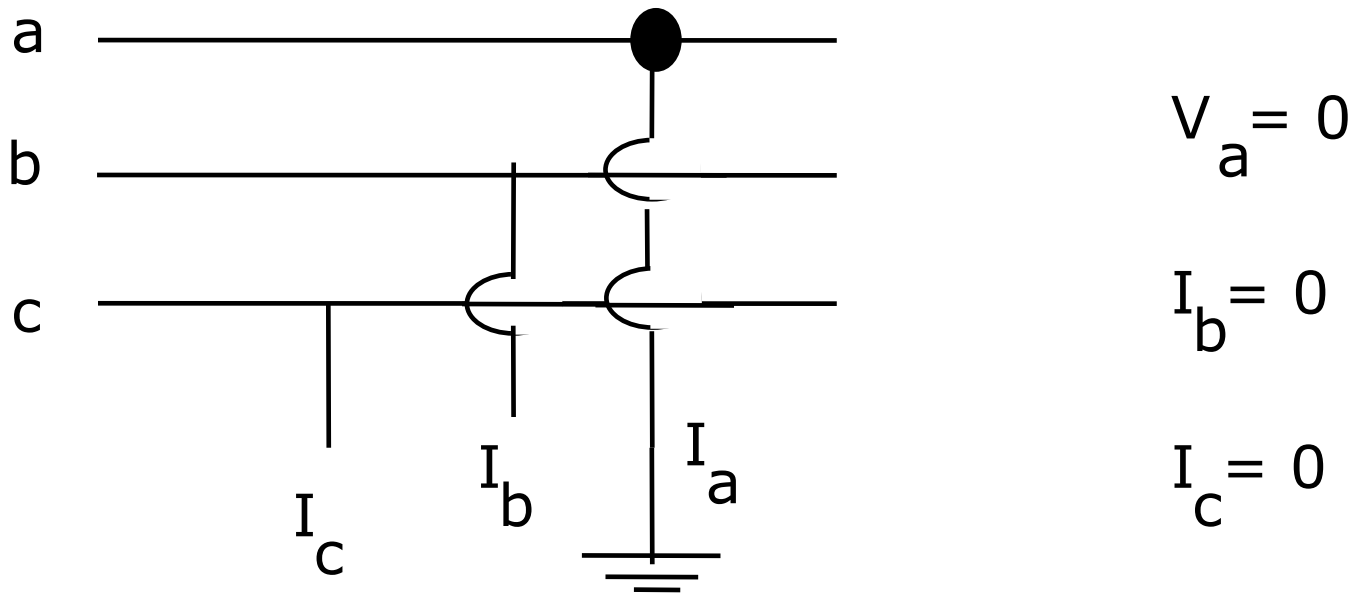
Fault Through Impedance :



$$I_{a1} = \frac{V_f}{Z_1 + Z_f} , I_{a2} = 0 , I_{a0} = 0$$



Single Line to Ground Fault Representation





$$\begin{bmatrix} I_{a1} \\ I_{a2} \\ I_{a0} \end{bmatrix} = \frac{1}{3} \begin{bmatrix} 1 & a & a^2 \\ 1 & a^2 & a \\ 1 & 1 & 1 \end{bmatrix} \begin{bmatrix} I_a \\ I_b \\ I_c \end{bmatrix}$$

$$I_{a1} = \frac{1}{3} I_a, \quad I_{a2} = \frac{1}{3} I_a, \quad I_{a0} = \frac{1}{3} I_a \quad \therefore I_{a1} = I_{a2} = I_{a0}$$

$$\begin{bmatrix} V_{a1} \\ V_{a2} \\ V_{a0} \end{bmatrix} = \begin{bmatrix} V_f \\ 0 \\ 0 \end{bmatrix} - \begin{bmatrix} Z_1 & 0 & 0 \\ 0 & Z_2 & 0 \\ 0 & 0 & Z_0 \end{bmatrix} \begin{bmatrix} I_{a1} \\ I_{a2} \\ I_{a0} \end{bmatrix}$$

$$V_{a1} = V_f - Z_1 I_{a1} \quad V_{a2} = -Z_2 I_{a2} \quad V_{a0} = -Z_0 I_{a0}$$

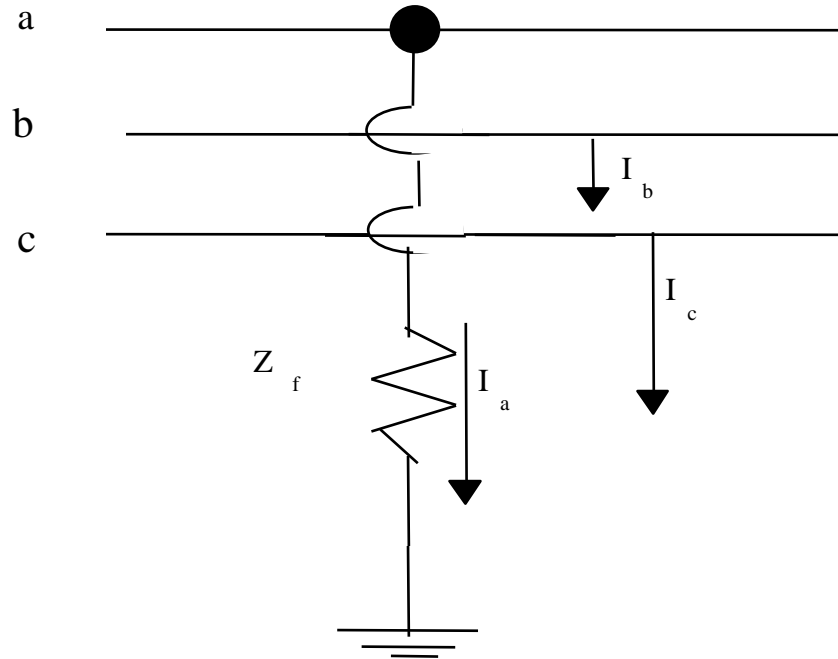
$$V_{a1} + V_{a2} + V_{a0} = V_f - Z_1 I_{a1} - Z_2 I_{a2} - Z_0 I_{a0}$$

$$\therefore V_a = V_{a1} + V_{a2} + V_{a0} = 0$$

$$I_{a1} = I_{a2} = I_{a0} = \frac{V_f}{Z_1 + Z_2 + Z_0} \quad I_a = \frac{3V_f}{Z_1 + Z_2 + Z_0}$$

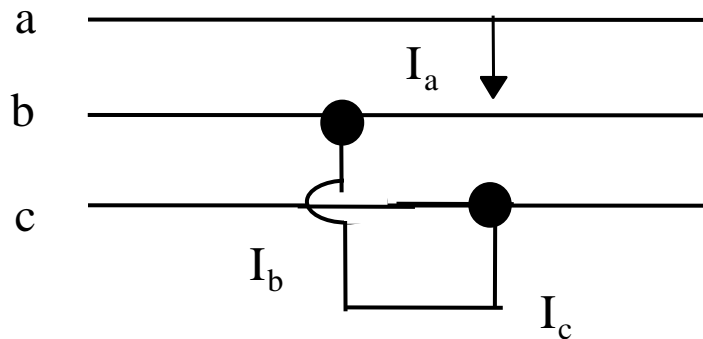


Fault Through Impedance :



$$I_{a1} = I_{a2} = I_{a0} = \frac{V_f}{Z_1 + Z_2 + Z_0 + 3z_f}$$

Line to Line Fault Representation



$$V_b = V_c$$

$$I_a = 0$$

$$I_b = -I_c$$

$$\begin{bmatrix} V_{a1} \\ V_{a2} \\ V_{a0} \end{bmatrix} = \frac{1}{3} \begin{bmatrix} 1 & a & a^2 \\ 1 & a^2 & a \\ 1 & 1 & 1 \end{bmatrix} \begin{bmatrix} V_a \\ V_b \\ V_c \end{bmatrix}$$

$$V_{a1} = 1/3 [V_a + aV_b + a^2V_c] = 1/3 [V_a + aV_b + a^2V_c]$$

$$V_{a2} = 1/3 [V_a + a^2V_b + aV_c] = 1/3 [V_a + a^2V_b + aV_c]$$

$$V_{a1} = V_{a2}$$



$$I_{a0} = 1/3 (I_a + I_b + I_c) = 1/3 (I_b - I_b) = 0$$

$$I_{a1} = 1/3 (aI_b + a^2I_c) = 1/3(aI_b - a^2I_b)$$

$$I_{a2} = 1/3 (a^2I_b + aI_c) = 1/3 (a^2I_b - aI_b)$$

$$\begin{bmatrix} I_{a1} \\ I_{a2} \\ I_{a0} \end{bmatrix} = \frac{1}{3} \begin{bmatrix} 1 & a & a^2 \\ 1 & a^2 & a \\ 1 & 1 & 1 \end{bmatrix} \begin{bmatrix} I_a \\ I_b \\ I_c \end{bmatrix}$$

$$\therefore I_{a1} = -I_{a2}$$

$$V_{a1} = V_f - Z_1 I_{a1}$$

$$V_{a2} = Z_2 I_{a2} = V_{a1} = V_f - Z_1 I_{a1}$$

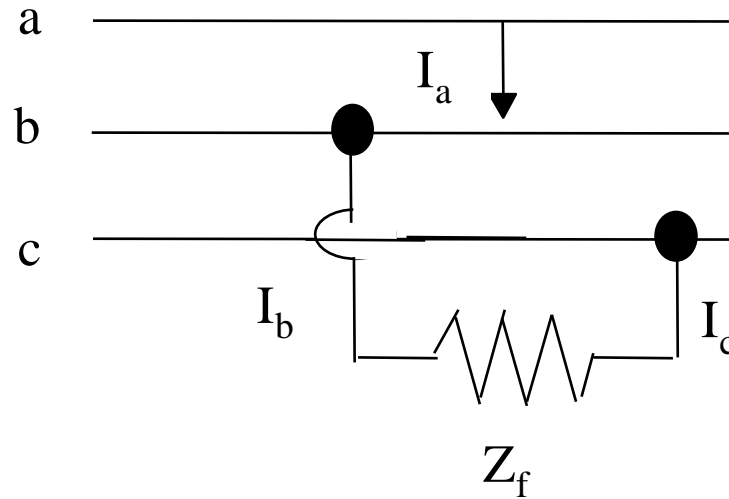
$$Z_2 I_{a1} = V_f - Z_1 I_{a1}$$

$$\begin{bmatrix} V_{a1} \\ V_{a2} \\ V_{a0} \end{bmatrix} = \begin{bmatrix} V_f \\ 0 \\ 0 \end{bmatrix} - \begin{bmatrix} Z_1 & 0 & 0 \\ 0 & Z_2 & 0 \\ 0 & 0 & Z_0 \end{bmatrix} \begin{bmatrix} I_{a1} \\ -I_{a1} \\ 0 \end{bmatrix}$$

$$\therefore I_{a1} = \frac{V_f}{(Z_1 + Z_2)} \quad \text{and} \quad I_{a2} = -I_{a1}, I_{a0} = 0, V_{a0} = 0$$

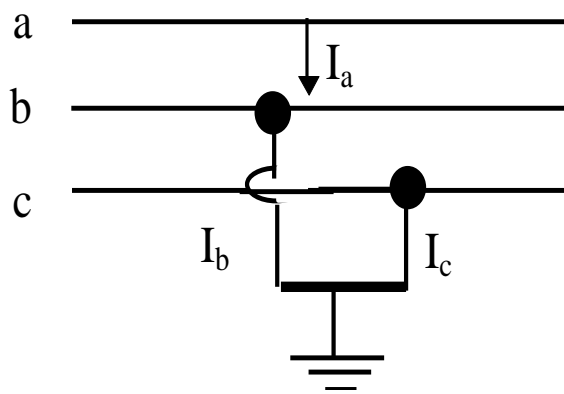


Fault Through Impedance :



$$I_{a1} = -I_{a2} = \frac{V_f}{(Z_1 + Z_2 + Z_f)}$$

Double Line to Ground Fault Representation:



$$V_b = 0$$

$$V_c = 0$$

$$I_a = 0$$

$$\begin{bmatrix} V_{a0} \\ V_{a1} \\ V_{a2} \end{bmatrix} = \frac{1}{3} \begin{bmatrix} 1 & a & a^2 \\ 1 & a^2 & a \\ 1 & 1 & 1 \end{bmatrix} \begin{bmatrix} V_a \\ 0 \\ 0 \end{bmatrix}$$

$$V_{a1} = \frac{1}{3} V_a, V_{a2} = \frac{1}{3} V_a, V_{a0} = \frac{1}{3} V_a$$

$$V_{a1} = V_{a2} = V_{a0}$$



$$I_{a1} + I_{a2} + I_{a0} = I_a = 0$$

$$I_{a1} = 1/3 (aI_b + a^2I_c)$$

$$I_{a2} = 1/3 (a^2I_b + aI_c)$$

$$I_{a0} = 1/3 (I_b + I_c)$$

$$1/3(aI_b + a^2I_c) + 1/3(a^2I_b + aI_c) + 1/3(I_b + I_c) = 0$$

$$aI_b + a^2I_c + a^2I_b + aI_c + I_b + I_c = 0$$

$$\begin{bmatrix} I_{a1} \\ I_{a2} \\ I_{a0} \end{bmatrix} = \frac{1}{3} \begin{bmatrix} 1 & a & a^2 \\ 1 & a^2 & a \\ 1 & 1 & 1 \end{bmatrix} \begin{bmatrix} 0 \\ I_b \\ I_c \end{bmatrix}$$

$$V_{a1} = V_f - Z_1 I_{a1}$$

$$V_{a2} = -Z_2 I_{a2}$$

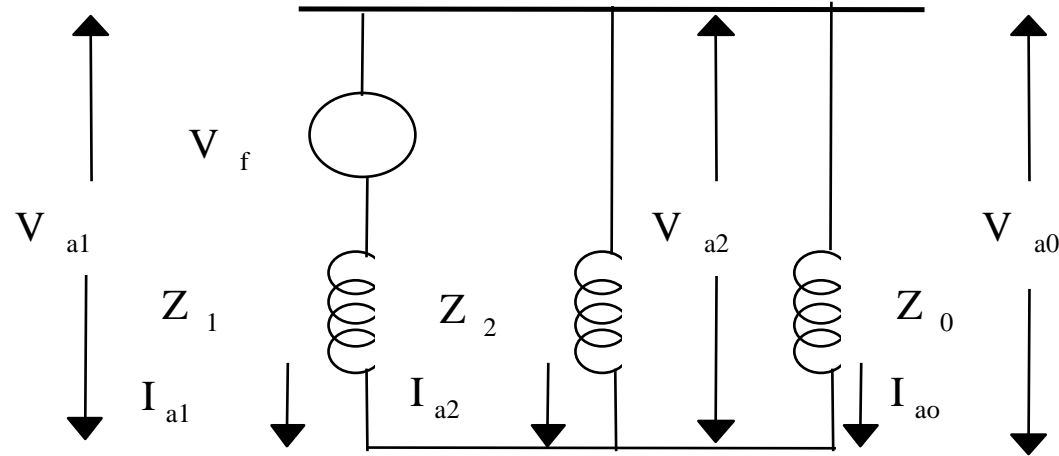
$$V_{a0} = -Z_0 I_{a0}$$

$$V_{a1} = V_{a2} = V_{a0}$$

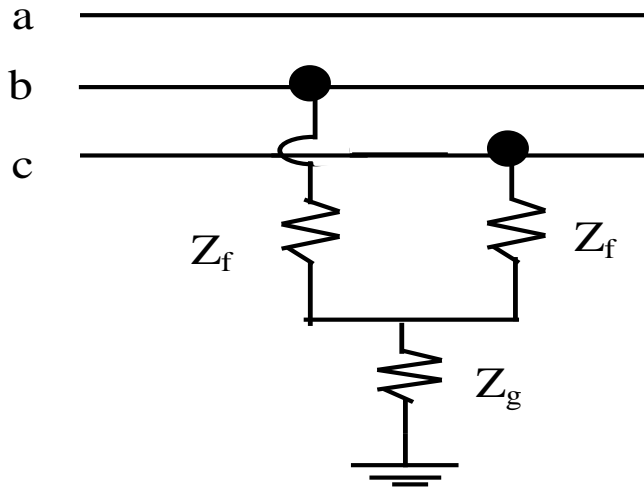
$$\therefore V_f - Z_1 I_{a1} = -Z_2 I_{a2} - Z_0 I_{a0}$$

$$\begin{bmatrix} V_{a1} \\ V_{a2} \\ V_{a0} \end{bmatrix} = \begin{bmatrix} V_f \\ 0 \\ 0 \end{bmatrix} - \begin{bmatrix} Z_1 & 0 & 0 \\ 0 & Z_2 & 0 \\ 0 & 0 & Z_0 \end{bmatrix} \begin{bmatrix} I_{a1} \\ I_{a2} \\ I_{a0} \end{bmatrix}$$

$$\therefore \Rightarrow I_{a1} = \frac{V_f}{\left[Z_1 + \left(\frac{Z_2 Z_0}{Z_2 + Z_0} \right) \right]}$$



Fault Through Impedance:



$$I_{a1} = \frac{V_f}{Z_1' + \left(\frac{Z_2' Z_0'}{Z_2' + Z_0'} \right)}$$

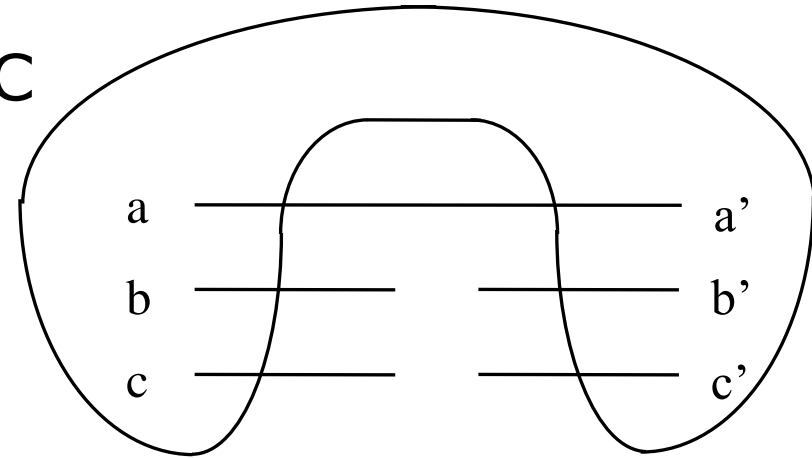
$$Z_1' = Z_1 + Z_f$$

$$Z_2' = Z_2 + Z_f$$

$$Z_0' = Z_0 + Z_f + 3Z_g$$



Open in phase B & C



$$I_b = 0 \text{ and } I_c = 0$$

$$V_i^a - V_k^a = Z_{aa}' I_a = Z_{aa}' I_f$$

$$\begin{bmatrix} I_{a1} \\ I_{a2} \\ I_{a0} \end{bmatrix} = \frac{1}{3} \begin{bmatrix} 1 & a & a^2 \\ 1 & a^2 & a \\ 1 & 1 & 1 \end{bmatrix} \begin{bmatrix} I_a \\ 0 \\ 0 \end{bmatrix}$$

$$I_{a1} = I_{a2} = I_{a0} = \frac{1}{3} I_a = \frac{1}{3} I_f$$



$$\begin{aligned}
 V_{a1} &= V_f - Z_1 I_{a1} \\
 V_{a2} &= -Z_2 I_{a2} \\
 V_{a0} &= -Z_0 I_{a0}
 \end{aligned}
 \quad
 \begin{bmatrix} V_{a1} \\ V_{a2} \\ V_{a0} \end{bmatrix} = \begin{bmatrix} V_f \\ 0 \\ 0 \end{bmatrix} - \begin{bmatrix} Z_1 & 0 & 0 \\ 0 & Z_2 & 0 \\ 0 & 0 & Z_0 \end{bmatrix} \begin{bmatrix} I_{a1} \\ I_{a2} \\ I_{a0} \end{bmatrix}$$

$$V_k^a - V_l^a = V_{kl}^1 + V_{kl}^2 + V_{kl}^0 = Z'_{zz} I_f = 3Z'_{aa} I_{a1}$$

$$V_f = V_{kl}$$

$$3Z'_{aa} I_{a1} = V_{kl} - Z_1 I_{a1} - Z_2 I_{a2} - Z_0 I_{a0}$$

$$I_{a1} = I_{a2} = I_{a0} = \frac{V_{kl}}{Z_1 + Z_2 + Z_0 + 3Z'_{aa}}$$



V_{kl} is the Thevenin equivalent voltage, once the line is removed, between buses k & l.

$$Z_1 = Z_{kk}^1 + Z_{ll}^1 - Z_{lk}^1 - Z_{kl}^1$$

$$Z_2 = Z_{kk}^2 + Z_{ll}^2 - Z_{lk}^2 - Z_{kl}^2$$

$$Z_0 = Z_{kk}^0 + Z_{ll}^0 - Z_{lk}^0 - Z_{kl}^0$$

$$3Z'_{aa} = Z_f = Z_1^f + Z_2^f + Z_0^f$$

Solution Methodology:

1. Do the load flow with the line isolated.
2. Then insert the line with two phase open.



Open in phase A :

- $I_a = 0$
- Similar type of analysis like double line fault.
- Voltage is between two nodes, rather than between node and ground.
- Impedance is the Thevenin's equivalent impedance between nodes.

$$I_f^1 = \frac{V_k - V_1}{Z_1' + \frac{Z_2' \cdot Z_0'}{Z_2' + Z_0'}}$$

$$Z_1^1 = Z_{kk}^1 + Z_{ll}^1 - Z_{lk}^1 - Z_{kl}^1 + Z_f^1$$

$$Z_2^1 = Z_{kk}^2 + Z_{ll}^2 - Z_{lk}^2 - Z_{kl}^2 + Z_f^2$$

$$Z_0^1 = Z_{kk}^0 + Z_{ll}^0 - Z_{lk}^0 - Z_{kl}^0 + Z_f^0$$

$$I_f^2 = I_f^1 \cdot \frac{Z_0'}{Z_0' + Z_2'}$$

$$I_f^0 = \frac{I_f^1 \cdot Z_2'}{Z_0' + Z_2'}$$



Solution Methodology:

1. Form the Y bus for +ve, -ve and zero sequence.
2. Do the LU factorisation for +ve, -ve and zero sequence.
3. To find the driving point impedance-

In fault study, particular row or column of Z bus is required.

Consider, $Yx = z$

$$x = Y^{-1}z$$

$$x = Z.z$$

Let z have 1 in p^{th} location and 0, at all other location.



$$\mathbf{x} = \begin{bmatrix} \mathbf{Z}_{11} & \mathbf{Z}_{12} & \cdots & \mathbf{Z}_{1p} & \mathbf{Z}_{1n} \\ \mathbf{Z}_{p1} & \mathbf{Z}_{p2} & \cdots & \mathbf{Z}_{pp} & \mathbf{Z}_{pn} \\ \vdots & & & & \\ \mathbf{Z}_{n1} & \mathbf{Z}_{n2} & \cdots & \mathbf{Z}_{np} & \mathbf{Z}_{nn} \end{bmatrix} \begin{bmatrix} 0 \\ 1 \\ \vdots \\ 0 \end{bmatrix} = \begin{bmatrix} \mathbf{Z}_{1p} \\ \mathbf{Z}_{pp} \\ \vdots \\ \mathbf{Z}_{np} \end{bmatrix}$$

$$\therefore \mathbf{Yx} = \mathbf{z}$$

Pass in z, 1.0 for the desired bus and 0 else where.
Call LU solution - x will be the desired column of Z bus.

4. Find the sequence fault current I_1^f , I_2^f and I_0^f .
5. Determine the post fault bus voltage



$$\begin{aligned}
 [V_f] &= [Z] [I_f^1] \\
 &= [Z] \{[I_0] - [I_f]\} \\
 &= [Z] [I_0] + [Z] [-I_f] \\
 &= [V_0] + [\Delta V]
 \end{aligned}$$

$$\Delta V = [Z] [-I_f]$$

$$Y[\Delta V] = [-I_f]$$

Solve ΔV using LU solution.

Above can be written as :

$[Y]_p [\Delta V]_p = [-I_f]_p$, p : positive sequence and similarly for other sequences.



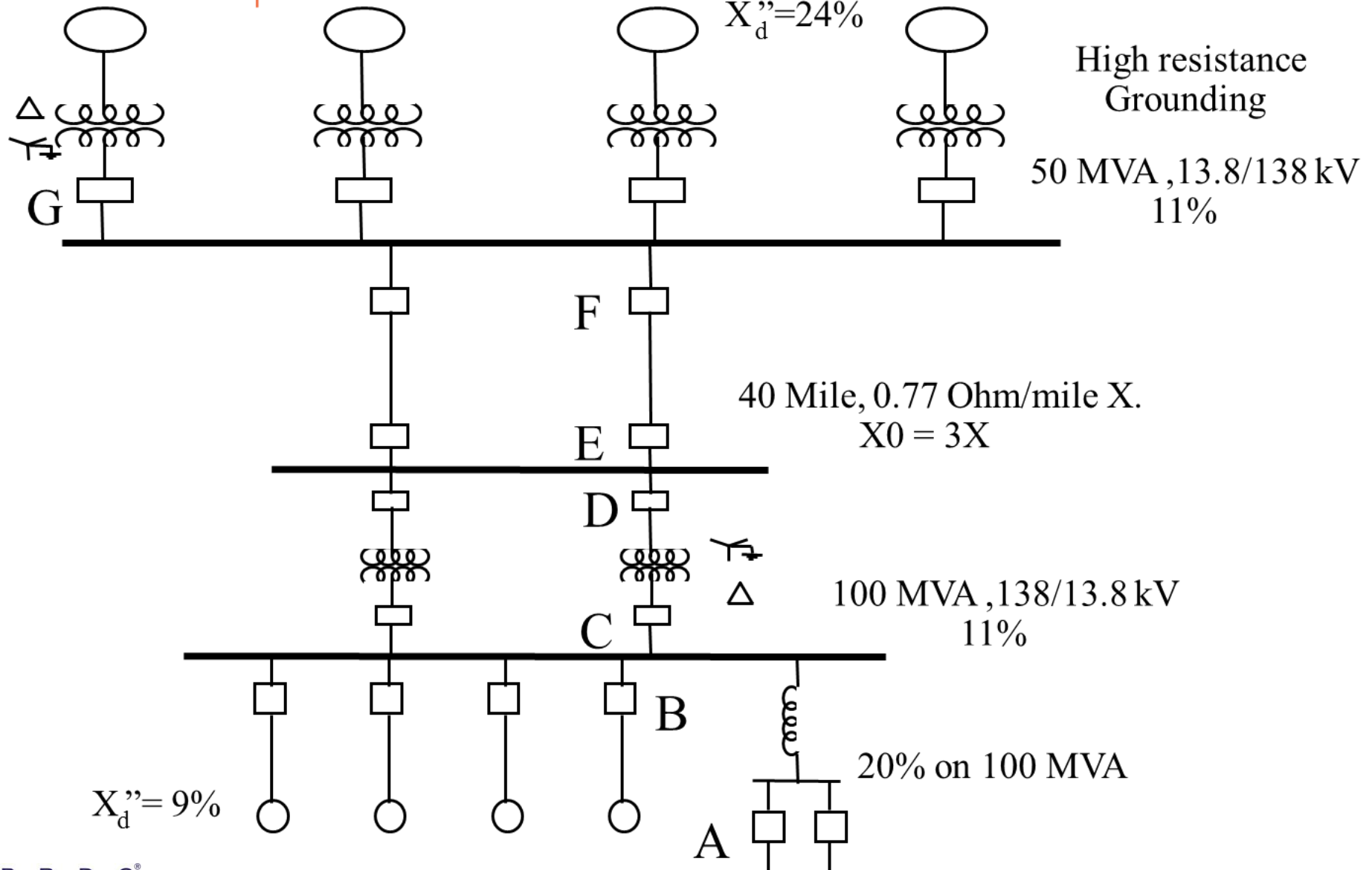
For faults other than open fault,

$$[-I_f]_p = \begin{bmatrix} 0 \\ 0 \\ \vdots \\ -I_f \\ \vdots \\ 0 \end{bmatrix}_p$$

For open fault, between k & l,

$$[-I_f]_p = k \begin{bmatrix} 0 \\ 0 \\ \vdots \\ -I_f \\ \vdots \\ +I_f \\ \vdots \\ 0 \end{bmatrix}$$

Example:





Grounding Practice in Power System :

Advantages of ungrounded system :

- Ground connection normally doesn't carry current. Hence elimination saves the cost.
- Current can be carried in other phases, with fewer interruptions.



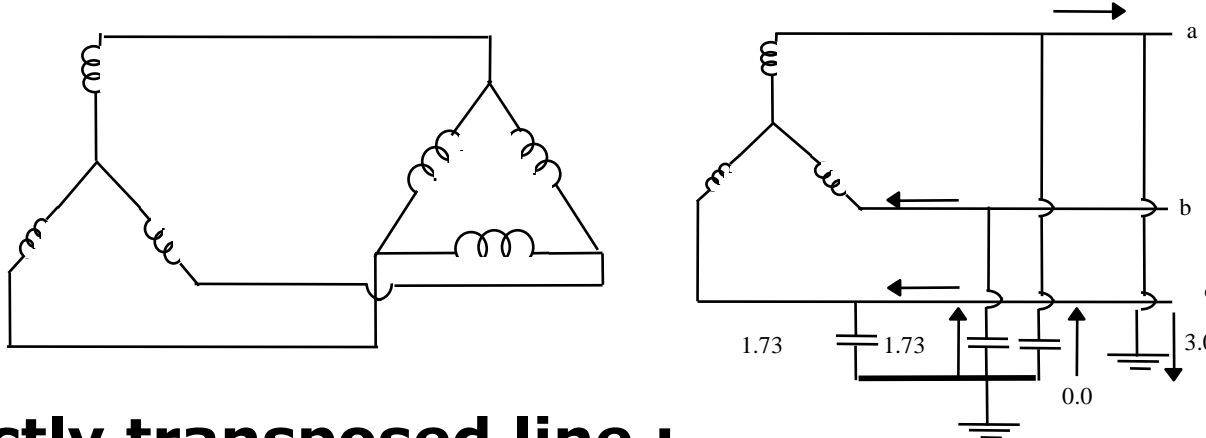
Grounding Practice in Power System :

Limitations of ungrounded system :

- With the increase in voltage and line length current has increased and self clearing nature advantage couldn't be seen.
- Arcing ground : Phenomena of alternate clearing and re-striking of the arc, which cause high voltage (surge and transient).
- If grounded, the insulation can be graded in transformer from line to neutral, thereby reducing the cost.
- In case of ungrounded system, influence on communication lines is more.
- Ground current can't be limited.



Ungrounded System :



Perfectly transposed line :

Neutral of transformer is at zero potential.

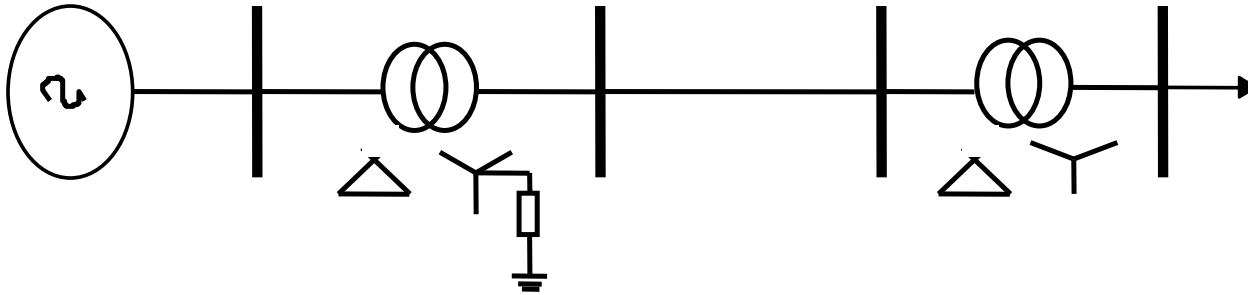
Un-transposed line :

Neutral is shifted.

Capacitance grounded :

Perfectly transposed line.

Resistance Grounded System:

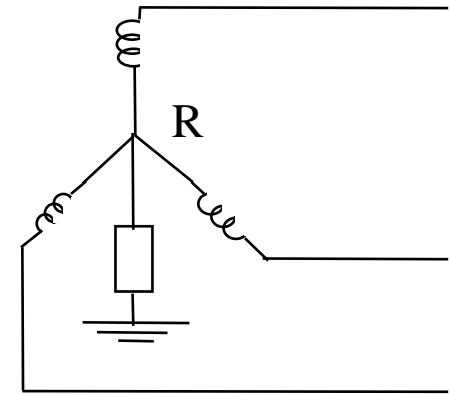
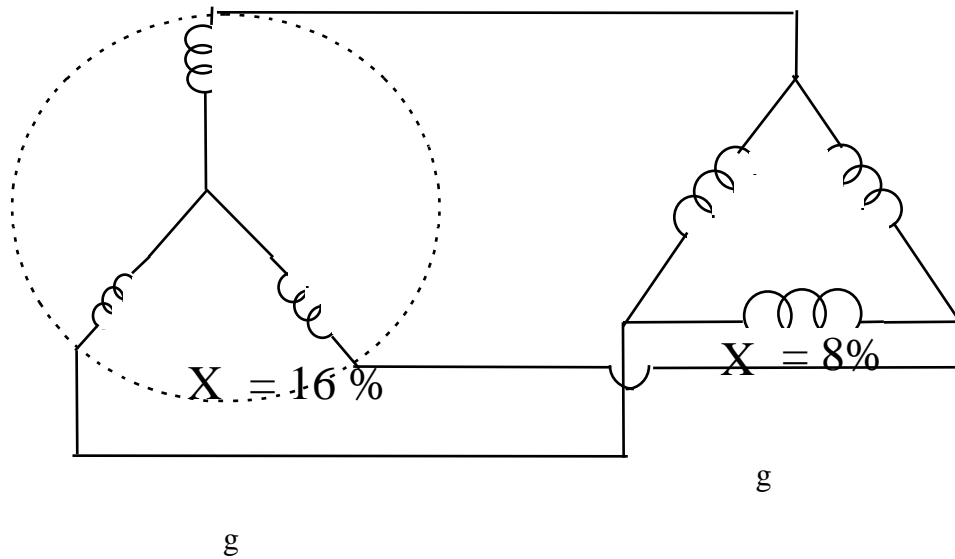


The resistance to neutral limits ground current.

Selection of resistance value:

- Amount of ground fault current.
- Power loss in resistor during ground fault.

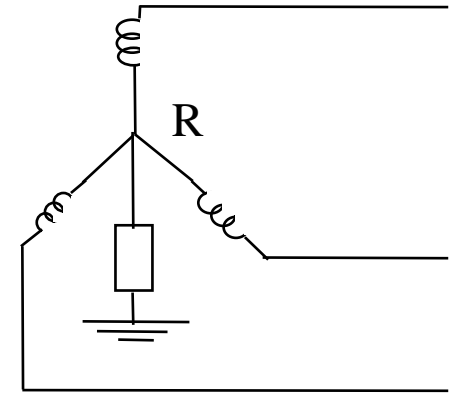
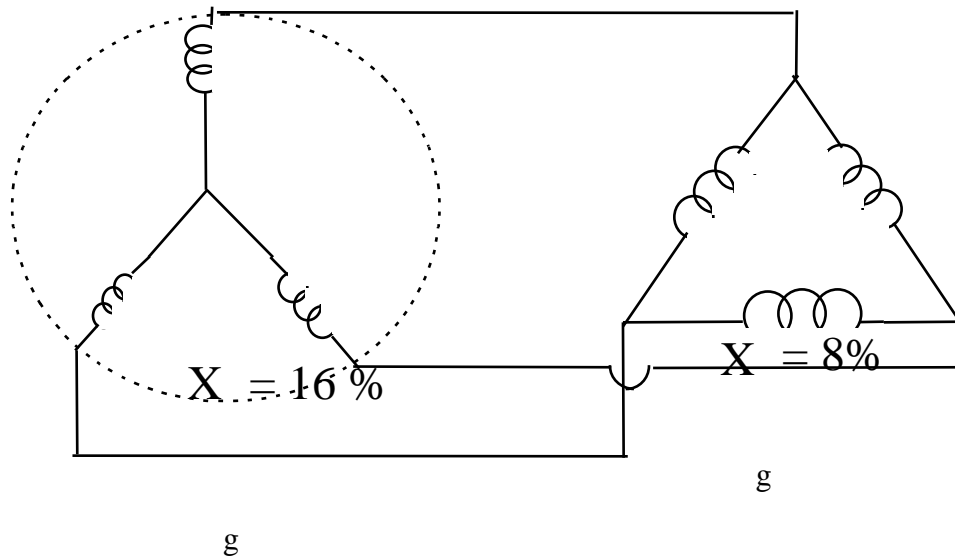
Power loss: usually expressed as a percentage of system rating.



$$Z_1 = 24\% , Z_2 = 24\% , Z_0 = 3R + j8$$

$$I_f = \frac{3}{Z_1 + Z_2 + Z_0} = \frac{3 * 100}{j24 + j24 + 3R + j8} = \frac{300}{3R + j56}$$

$$\text{Power Loss} = I_f^2 R = \left(\frac{300}{3R + j56} \right)^2 * R$$



$$Z_1 = 24\% , Z_2 = 24\% , Z_0 = 3R + j8$$

$$I_f = \frac{3}{Z_1 + Z_2 + Z_0} = \frac{3 * 100}{j24 + j24 + 3R + j8} = \frac{300}{3R + j56}$$

$$\text{Power Loss} = I_f^2 R = \left(\frac{300}{3R + j56} \right)^2 * R$$



I_f : in pu, R : in pu

For three phase system, power loss

$$= \frac{I_f^2 R}{3} \text{ percentage of 3 phasesystemkVA rating}$$

R is in percent p.u.

Maximum power loss = ?

Selection :

How much be the value of ground fault current ?

What should be the percent power loss in the ground resistance ?

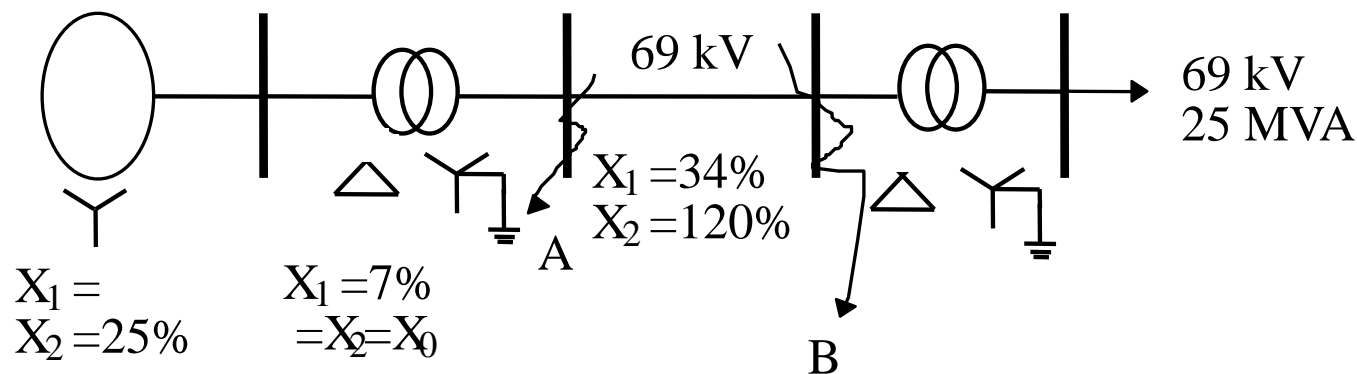


Effectively grounded system:

Solidly grounded : No impedance between neutral and earth

Effectively grounded : As per AIEE standard No.32, Section 32 - 1.05, May 1947 :

$$\frac{X_0 \text{ system}}{X_1 \text{ system}} \leq 3.0 \qquad \frac{R_o}{X_1 \text{ system}} \leq 1.0$$





Effectively grounded system:

For fault at A $\frac{X_0}{X_1} = \frac{7}{32}$

For fault at B $\frac{X_0}{X_1} = \frac{127}{32+34} = \frac{127}{66}$

Reactance Grounded System

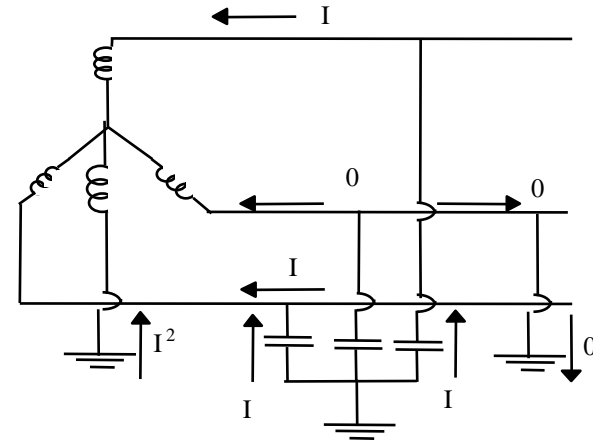
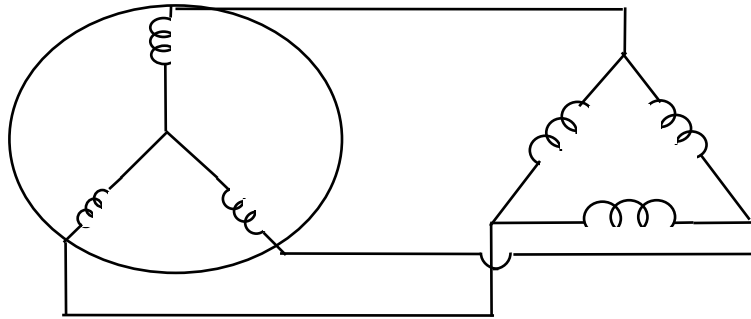
$\frac{X_0}{X_1} = 3.0$; but no resonance (resonance grounding)

If $X_g = 50 \Omega$ at A , find the nature of grounding at A & B.

Resonant - Grounded System :



Capacitance current is tuned or neutralised by a neutral reactor or similar device.



Fault current is made zero by selecting the suitable tap on the ground reactor.



Circuit Breaker Selection

1. Determine the symmetrical current (maximum) for any type of fault.
 2. Multiply the current by factor obtained from standard tables depending on the duty cycle.
(2 cycles clearing, 5 cycles clearing etc.)
- Use the above current to specify the interrupting current



References

1. Stagg and A.H. El-Abiad, "Computer Methods in Power System Analysis", Mcgraw-Hill, 13th print, New Delhi, 1988.
2. William D. Stevenson "Elements Of Power System Analysis", McGraw-Hill, Fourth edition, New Delhi, 1982.
3. George L. Kusic, "Computer Aided Power System Analysis", Prentice-Hall, International, N.J., New Delhi, 1989.
4. J. Arrillaga, C.P. Arnold and B.J. Harker, "Computer Modeling of Electrical Power Systems", John Wiley and Sons, 1983.



Queries & Discussions





Thank You

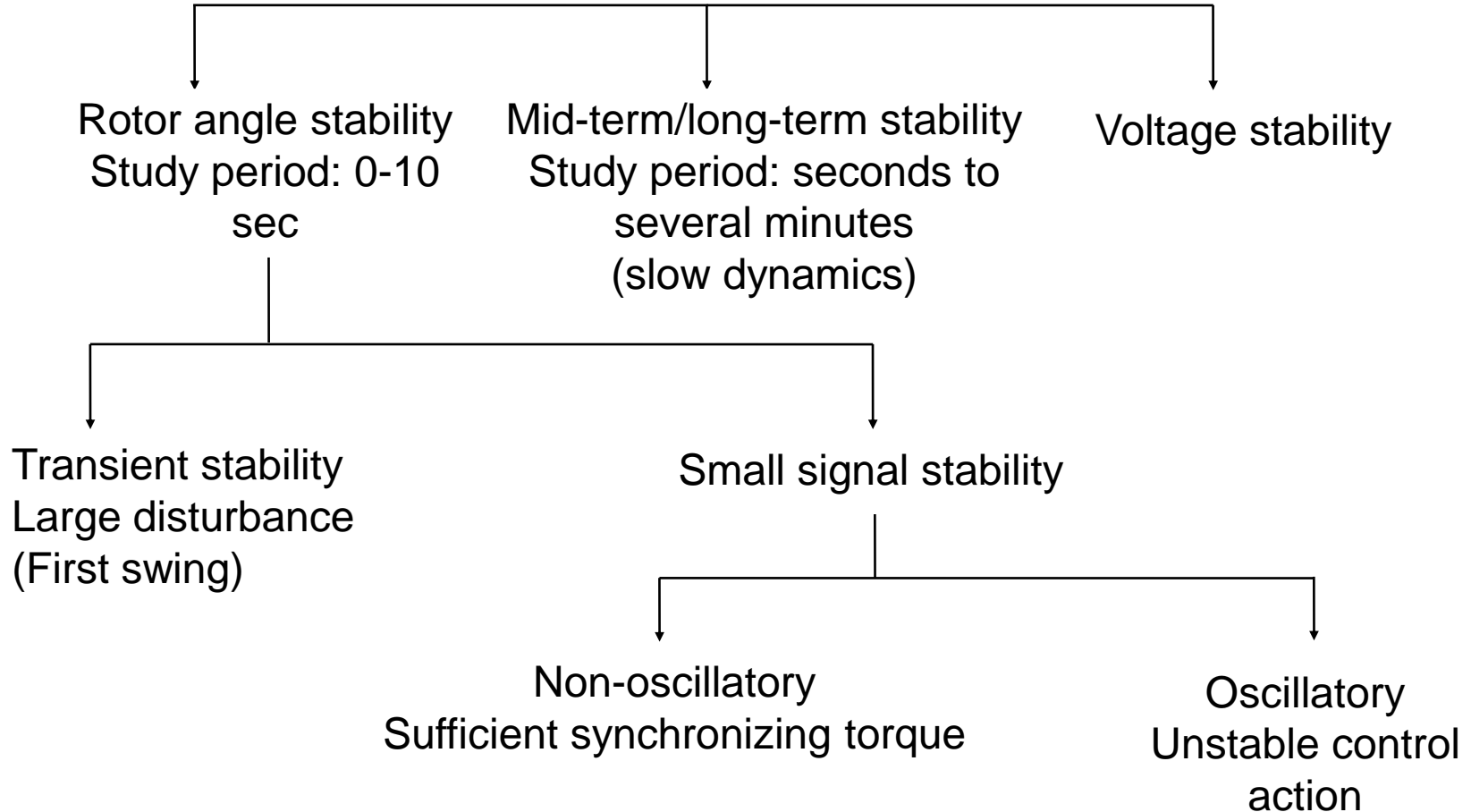




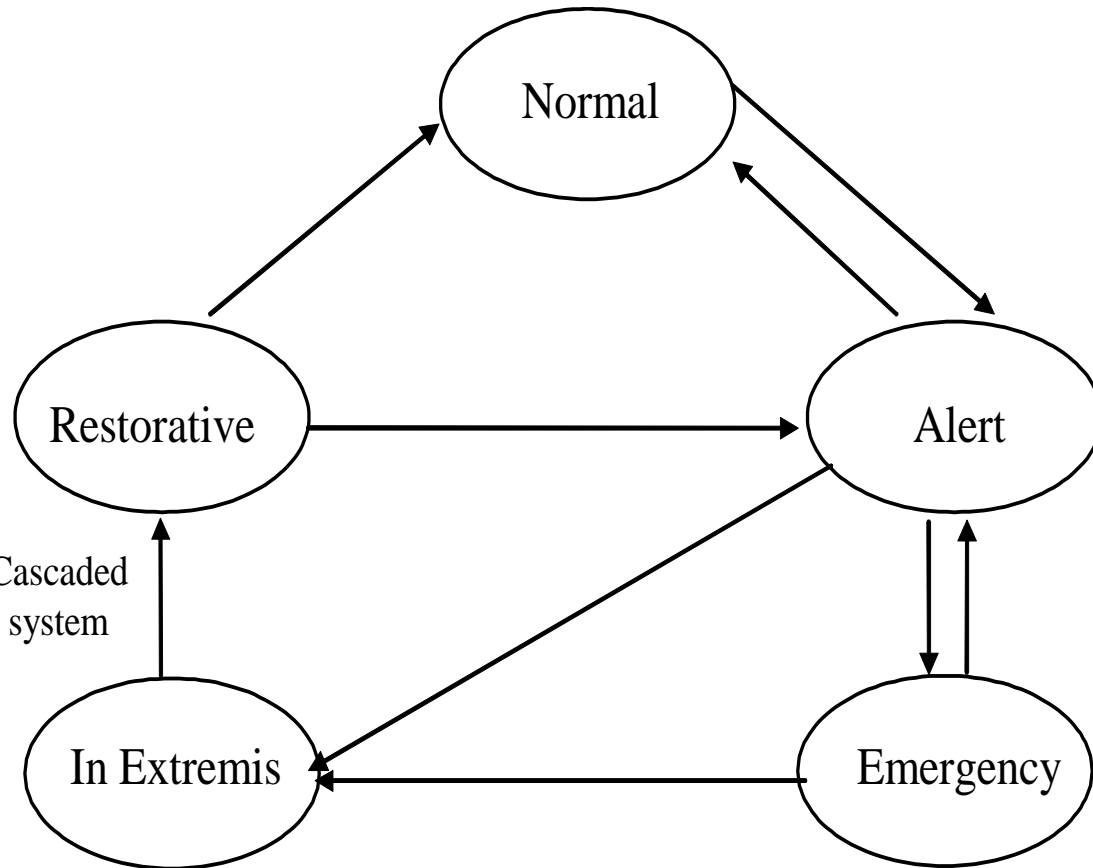
TRANSIENT STABILITY STUDIES



Stability



Power System Operating States



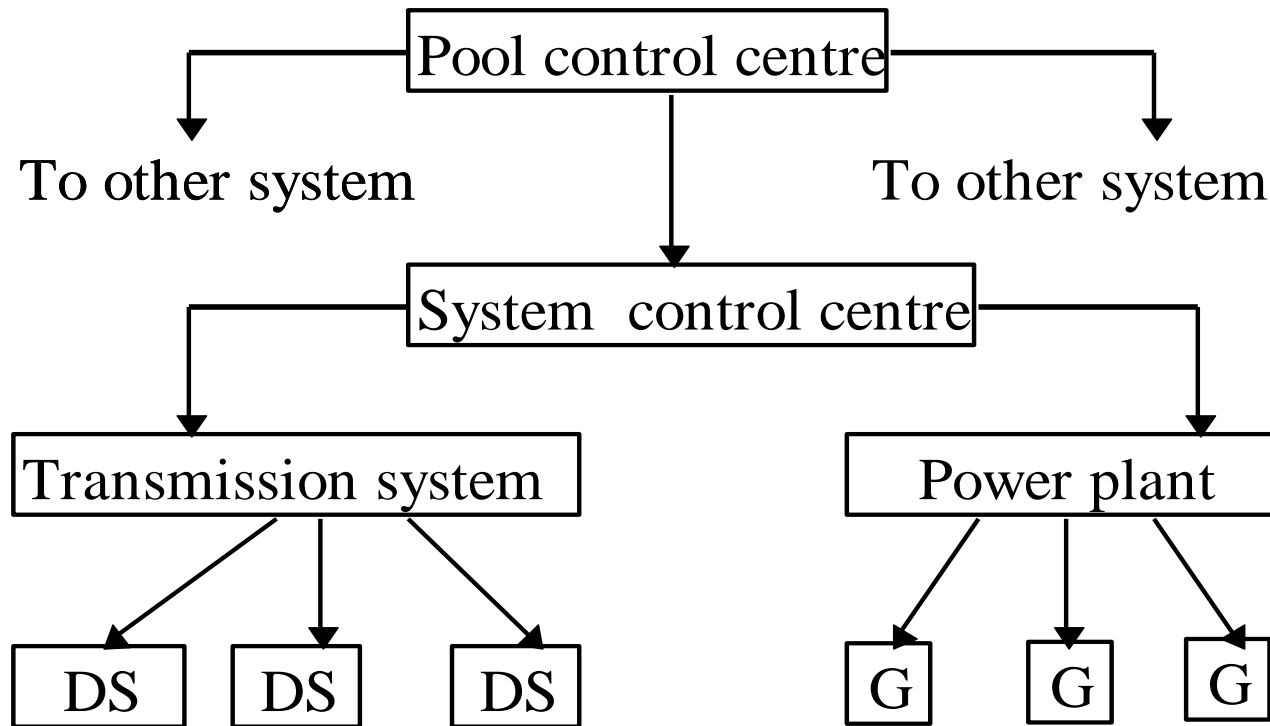
f , v , loading acceptable,
load met, $n-1$ or $n-2$
contingency acceptable

f , v , loading acceptable,
load met
 $n-1$ or $n-2$ contingency
not satisfied

f , v , loading not
acceptable,
load not met



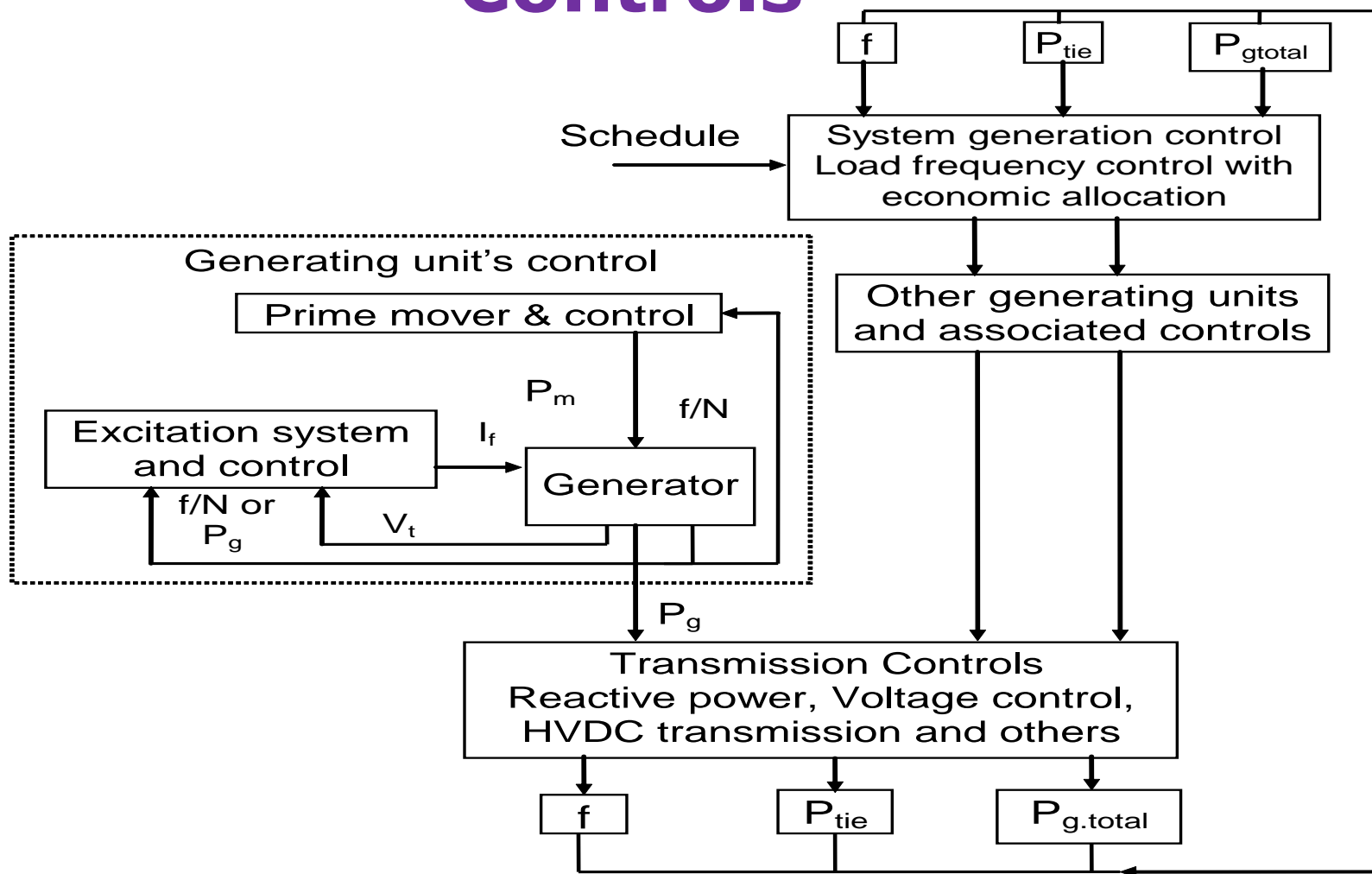
Control Hierarchy



DS: Distribution System

G : Generator

Power System Subsystem & Controls





Power System Stability

Ability of a power system to remain in synchronism.
Classification of transients : Electromagnetic and Electromechanical

Stability classification

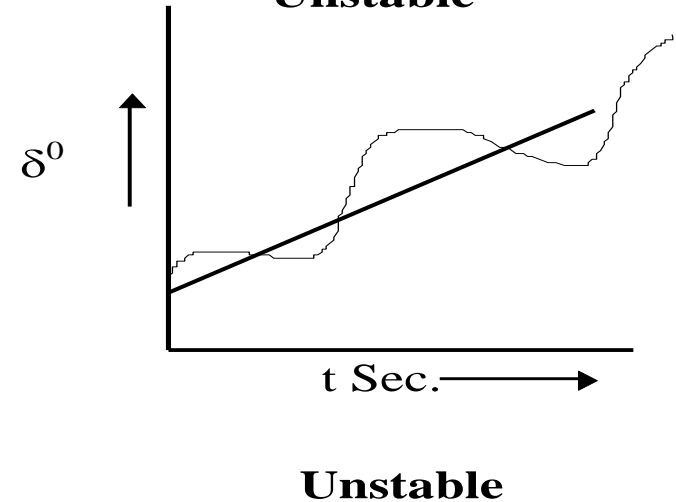
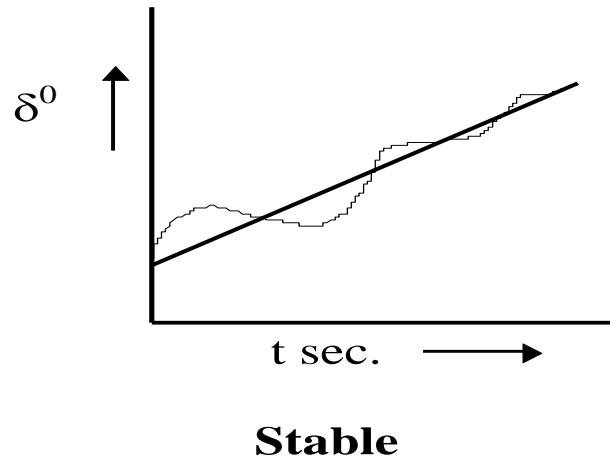
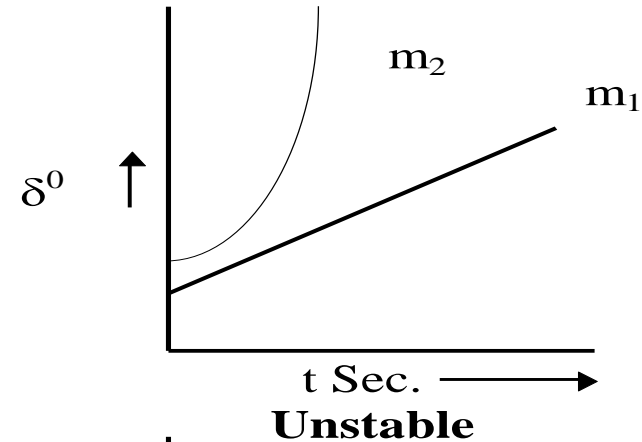
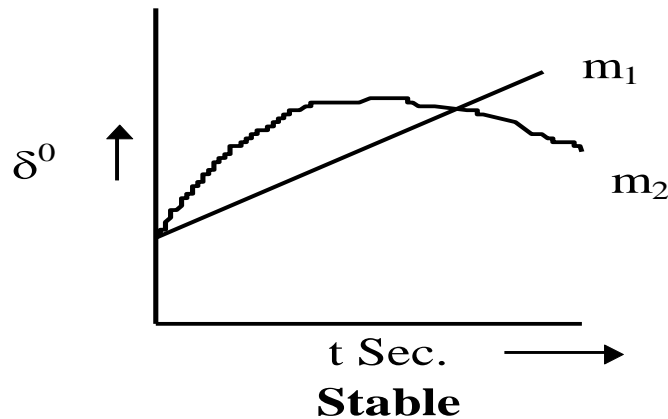
- Transient stability : Transmission line faults, sudden load change, loss of generation, line switching etc.
- Dynamic stability : Slow or gradual variations. Machine, governor-Turbine, Exciter modeling in detail.
- Steady state stability : Changes in operating condition. Simple model of generator.



Transient Stability:

First swing stability problem

Multi-swing stability problem. (normal size)

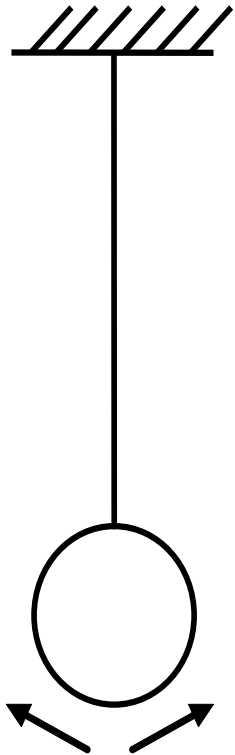




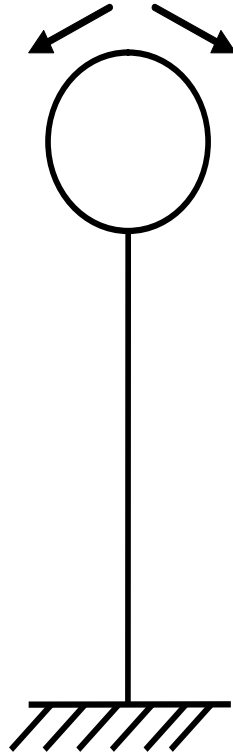
Assumptions :

- Synchronous speed current and voltage are considered.
- DC offset currents, harmonics are neglected.
- Symmetrical components approach.
- Generated voltage is independent of machine speed.
- Circuit parameters are constant at nominal system frequency.(Frequency variation of parameter neglected).

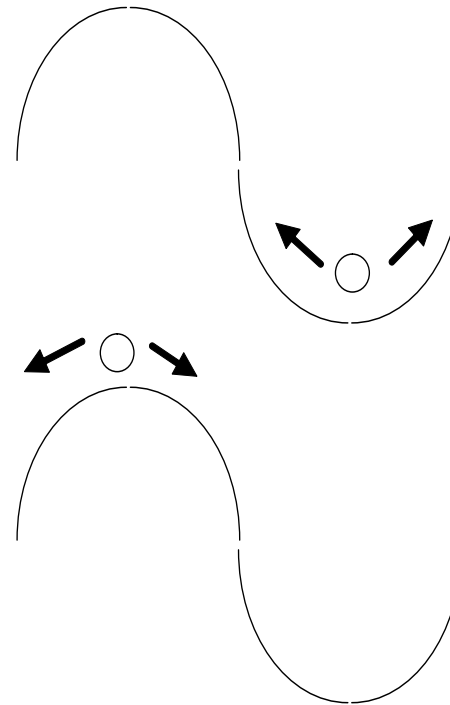
Steady State Stability



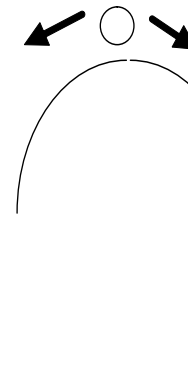
Stable



Unstable



Stable



Unstable



Mechanical Equation :

$$J * \frac{d^2 \theta_m}{dt^2} = T_a = T_m - T_e \quad N - m$$

J : Moment of inertia of rotor masses (kg-mt²)

θ_m : Angular displacement of rotor w.r.t. a stationary axis
(mechanical radians)

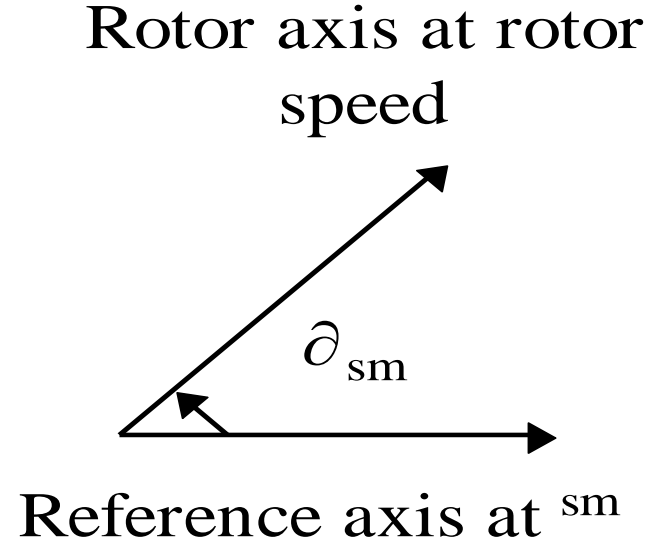
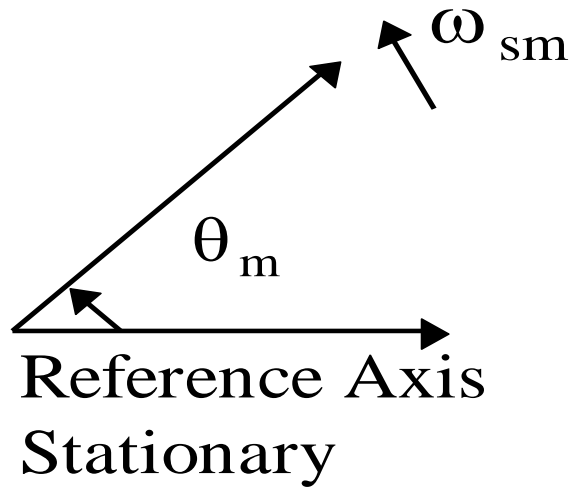
t : Time (seconds)

T_m : Mechanical or Shaft Torque (N-m)

T_e : Net electrical torque (N-m)

T_a : Net accelerating torque (N-m)

For generator, T_m and T_e are +ve.



δ_m : Angular displacement of the rotor in mechanical radians.

$$\theta_m = \omega_{sm} t + \delta_m$$



$$\frac{d\theta_m}{dt} = \omega_{sm} + \frac{d\delta_m}{dt}$$

$$\frac{d^2\theta_m}{dt^2} = \frac{d^2\delta_m}{dt^2}$$

$$J \frac{d^2\delta_m}{dt^2} = T_m - T_e N - m$$

$$\omega_m = \frac{d\theta_m}{dt} \Rightarrow \text{Angular velocity in radians per sec.}$$

$$J \omega_m \frac{d^2\delta_m}{dt^2} = P_m - P_e \text{ watts}$$

$$M \frac{d^2\delta_m}{dt^2} = P_m - P_e (\text{Approx})$$

Where M : Inertia constant = at synchronous speed in Joules-sec per mechanical radian.



Constant is defined as the ratio of stored Kinetic Energy in Mega Joules at synchronous speed and machine rating in MVA

$$H = \frac{\frac{1}{2} J \omega_{sm}^2}{S} = \frac{\frac{1}{2} M \omega_{sm}}{S} \text{ MJ / MVA}$$

$$M = \frac{2HS}{\omega_{sm}} \text{ MJ per mechanical radian}$$

$$M \frac{d^2 \delta_m}{dt^2} = P_m - P_e \text{ watts}$$

$$\frac{2HS}{\omega_{sm}} \frac{d^2 \delta_m}{dt^2} = P_m - P_e$$



$$\frac{2H}{\omega_{sm}} \frac{d^2 \delta_m}{dt^2} = \frac{P_m - P_e}{S}$$

$$\frac{2H}{\omega_{sm}} \frac{d^2 \delta_m}{dt^2} = P_m - P_e \text{ pu}$$

$$\frac{2H}{\omega_s} \frac{d^2 \delta}{dt^2} = P_m - P_e$$



$$\frac{H}{\pi f} \frac{d^2 \delta}{dt^2} = P_m - P_e \text{ pu Swing Equation}$$

If δ in electrical degrees

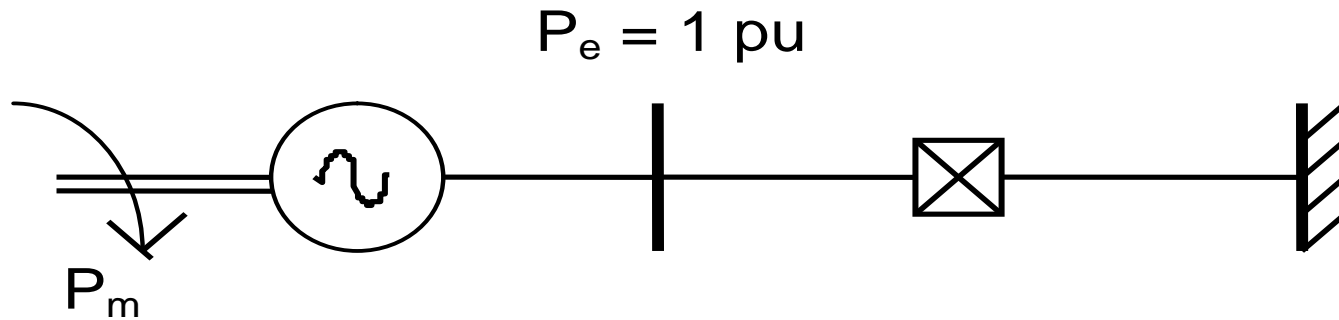
$$\frac{H}{180f} \frac{d^2 \delta}{dt^2} = P_m - P_e \text{ pu}$$

$$\frac{2H}{\omega_s} \frac{d\omega}{dt} = P_m - P_e \Rightarrow \frac{d\delta}{dt} = \omega - \omega_s$$

$$\text{Let } P_m - P_e = 1 \text{ pu}$$

$$\frac{2H}{\omega_s} \frac{d\omega}{dt} = 1 \text{ pu}, \Delta\omega = \frac{\omega_s}{2H} \Delta t$$

$$\text{If } \Delta t = 2H, \Delta\omega = \omega_s$$



At $t = 0$, breaker is opened.

Initially $P_e = 1$ pu on machine rating $P_m = 1$ pu and kept unchanged.

In $2H$ seconds, the speed doubles.



$$H = \frac{\text{Stored KE}}{\text{Machine Rating}}$$

$$H_{mech} \times \text{Machine Rating} = H_{system} \times \text{system MVA}$$

$$\therefore H_{system} = H_{mech} \times \frac{\text{Machine rating}}{\text{System MVA}}$$

Inertia constant (H) is in the range 2 - 9 for various types of machines. Hence H-constant is usually defined for machine.

Relation between H constant and Moment of Inertia is given by:



$$\text{Moment of Inertia} = \frac{WR^2}{32.2} \text{ lb-ft}^2$$

W: Weight of rotational part in pounds

R: Radius of gyration in feet

$$KE = \frac{1}{2} \frac{WR^2}{32.2} \left[\frac{2\pi N}{60} \right]^2 \text{ ft-lb}$$

$$550 \text{ ft-lb/sec} = 746 \text{ Watts}$$

$$H = \frac{\frac{1}{2} \frac{WR^2}{32.2} \left[\frac{2\pi N}{60} \right]^2 \times \frac{746}{550} \times 10^{-6}}{S_{\text{machine}}}$$



Example :

$$S_{\text{mach}} = 1333 \text{ MVA}$$

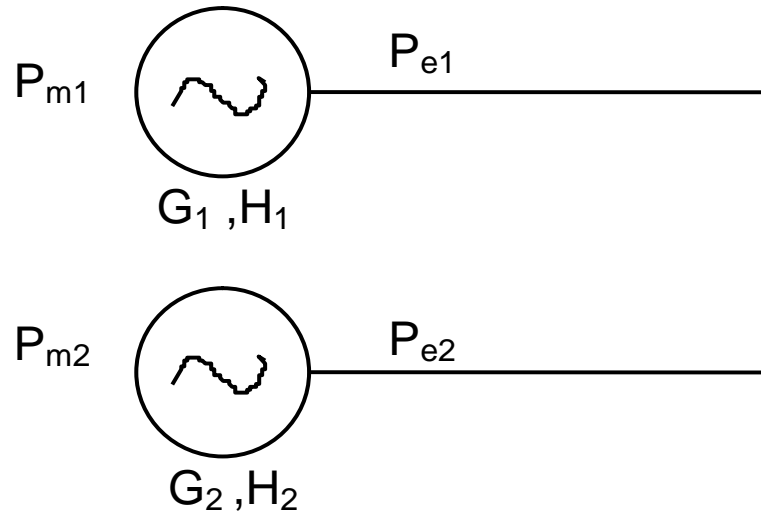
$$WR^2 = 5820000 \text{ lb} - \text{ft}^2$$

$$N = 1800 \text{ RPM}$$

$$H = \frac{\left[\frac{746}{550} \right] \times 10^{-6} \times \frac{1}{2} \times \frac{5820000}{32.2} \times \left[\frac{2\pi 1800}{60} \right]^2}{1333}$$

$$= 3.2677575 \text{ pu (MJ/ MVA)}$$

On 100 MVA base : $H = 1333 / 100 = 43.56 \text{ (MJ / MVA)}$



$$\frac{H_1}{f\pi} \times \frac{d^2\delta_1}{dt^2} = P_{m1} - P_{e1} \quad \frac{H_2}{f\pi} \times \frac{d^2\delta_2}{dt^2} = P_{m2} - P_{e2}$$

$$\left[\frac{H_1 + H_2}{f\pi} \right] \frac{d^2(\delta)}{dt^2} = (P_{m1} + P_{m2}) - (P_{e1} + P_{e2})$$



$\delta_1 = \delta_2 = \delta$; since the machines swing together

$$\frac{H}{\pi f} \frac{d^2 \delta}{dt^2} = (P_m - P_e)$$

$$H = H_1 + H_2$$

$$P_m = P_{m1} + P_{m2}$$

$$P_e = P_{e1} + P_{e2}$$

G_1 and G_2 are called coherent machines.

Inertia Constant

$$H = \frac{\text{Stored energy at rated speed in MWs}}{\text{MVA rating}}$$

MKS System



$$\begin{aligned} \text{Stored energy} &= \text{Kinetic energy} = \frac{1}{2} J [\omega_{om}]^2 \text{ watts} \\ &= \frac{1}{2} J [\omega_{om}]^2 \times 10^{-6} \text{ MWs} \end{aligned}$$

J : Moment of inertia in kg-m^2

ω_{om} : Rated speed in mechanical radian / sec $= \frac{2\pi}{60} \text{ RPM}$

$$\therefore H = \frac{\frac{1}{2} J \omega_{om}^2 \times 10^{-6}}{\text{MVA rating}} = 5.48 \times 10^{-9} \left[\frac{J (\text{RPM})^2}{\text{MVA rating}} \right]$$

British Units



Given

$$WR^2 = (\text{Weight of rotating part}) \\ \times (\text{square of radius of gyration})(lb - ft^2)$$

$$\therefore J = \frac{WR^2}{32.2} \times 1.356 \text{ kg} - m^2$$



Example: MVA rating : 555 WR² : 654158 lb-ft²

$$J = \frac{WR^2}{32.2} \times 1.356 = 27547.77168 \text{ kg} - \text{m}^2$$

$$H = 5.48 \times 10^{-6} \frac{J(RPM)^2}{MVA \text{ rating}} = MWs / MVA$$

Stored energy

$$= H \times MVA \text{ rating} = MWs$$

Mechanical starting time

$$= 2H = \text{sec}$$



Typical values

Unit Type	H Constant
Hydo unit	2 to 4
Thermal unit	
2 pole - 3600 RPM	2.5 to 6
4 pole - 1800 RPM	4 to 10

Non coherent machines

$$\frac{H_1}{\pi f} \frac{d^2 \delta_1}{dt^2} = P_{m1} - P_{e1}$$

$$\frac{d^2 \delta_1}{dt^2} = \frac{\pi f}{H_1} [P_{m1} - P_{e1}]$$

$$\frac{H_2}{\pi f} \frac{d^2 \delta_2}{dt^2} = P_{m2} - P_{e2}$$

$$\frac{d^2 \delta_2}{dt^2} = \frac{\pi f}{H_2} [P_{m2} - P_{e2}]$$



$$\frac{d^2}{dt^2}(\delta_1 - \delta_2) = \frac{\pi f}{H_1}(P_{m1} - P_{e1}) - \frac{\pi f}{H_2}(P_{m2} - P_{e2})$$

$$\frac{1}{\pi f} \frac{d^2(\delta_1 - \delta_2)}{dt^2} = \frac{H_2(P_{m1} - P_{e1}) - (P_{m2} - P_{e2})H_1}{H_1 H_2}$$

$$\frac{H_1 H_2}{H_1 + H_2} \times \frac{1}{\pi f} \frac{d^2(\delta_1 - \delta_2)}{dt^2} = \frac{H_2}{H_1 + H_2}(P_{m1} - P_{e1}) - \frac{H_1}{H_1 + H_2}(P_{m2} - P_{e2})$$

$$\frac{H_1 H_2}{H_1 + H_2} \times \frac{1}{\pi f} \times \frac{d^2(\delta_1 - \delta_2)}{dt^2} = \frac{H_2 P_{m1} - H_1 P_{m2}}{H_1 + H_2} - \frac{H_2 P_{e1} - H_1 P_{e2}}{H_1 + H_2}$$

$$\frac{H}{\pi f} \times \frac{d^2 \delta_{12}}{dt^2} = P_{m12} - P_{e12}$$

Where,

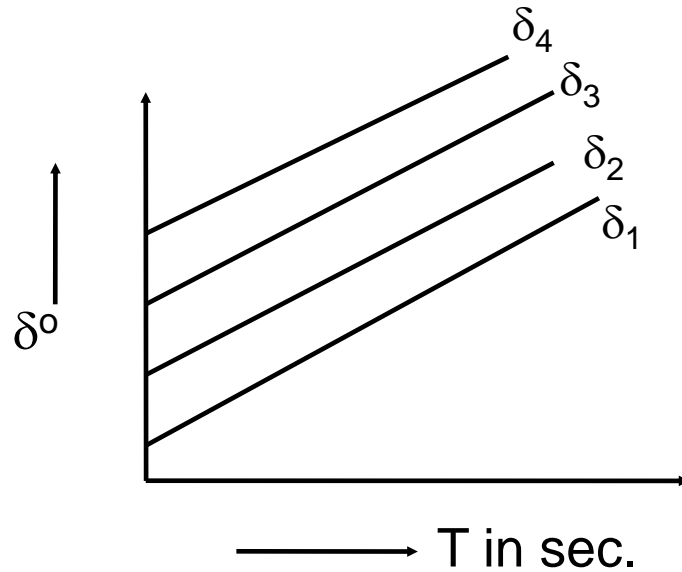
$$H = \frac{H_1 H_2}{H_1 + H_2} P_{m12} = \frac{H_2 P_{m1} - H_1 P_{m2}}{H_1 + H_2}$$

$$P_{e12} = \frac{H_2 P_{e1} - H_1 P_{e2}}{H_1 + H_2}$$

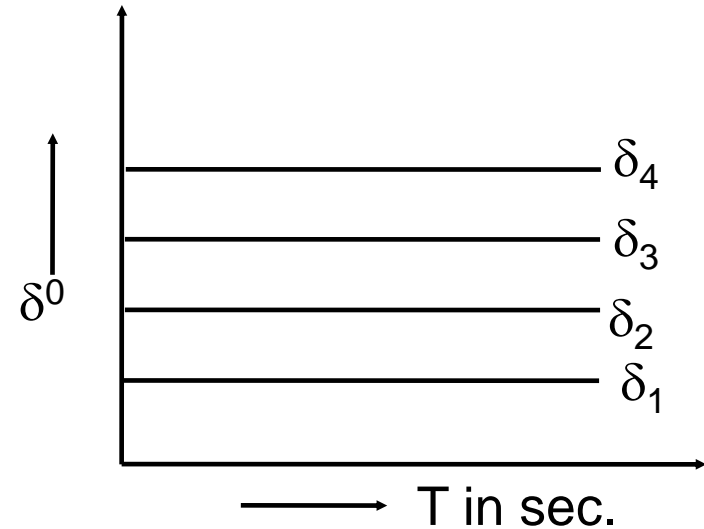
Relative swing (with reference to one machine) is more important, rather than absolute swing.



Swing Curves



Absolute Plot

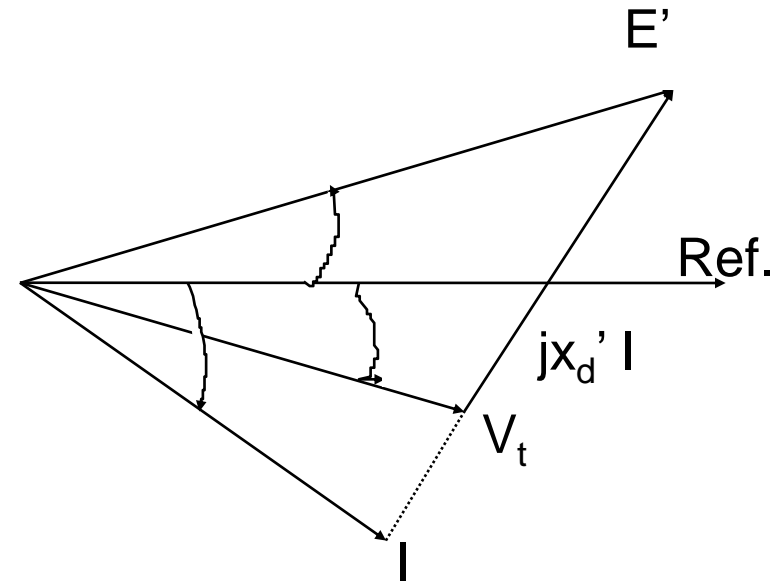
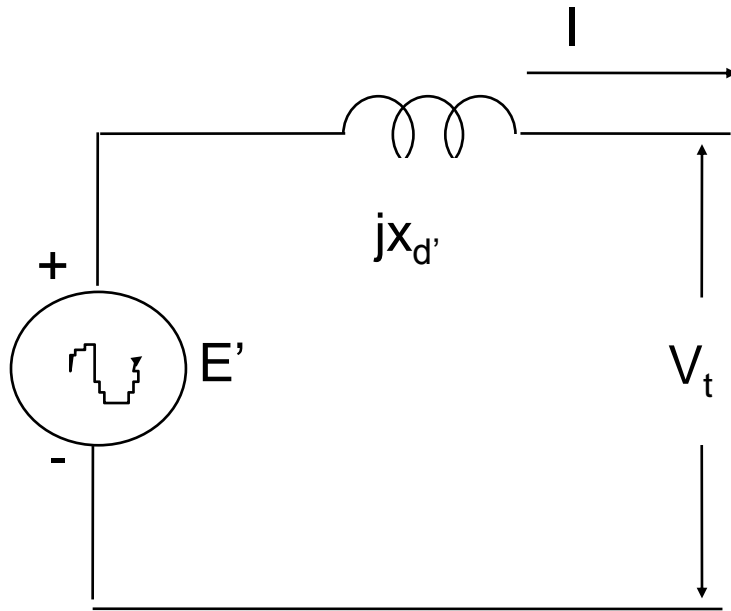


Relative Plot ($\delta_i - \delta$)

Relative swing (with reference to one machine) is more important, rather than absolute swing.

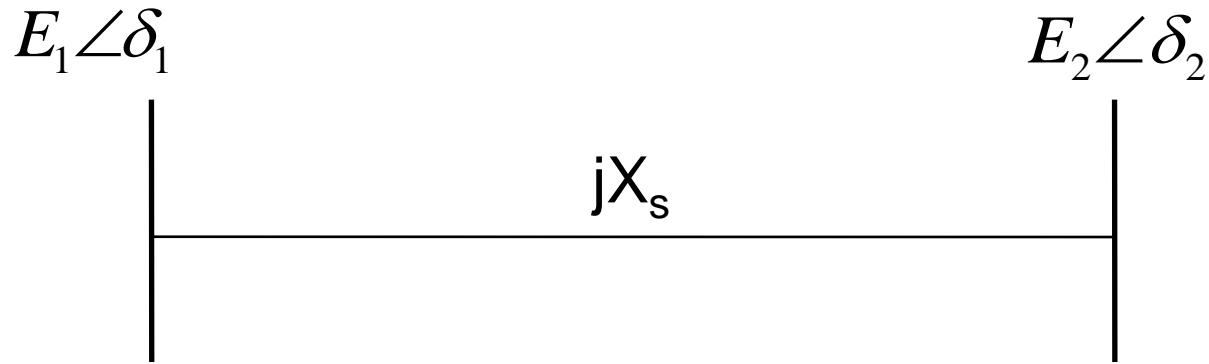


Classical model : (Type 1) Constant voltage behind transient reactance.



$$E' = V_t + (0 + jx_{d'}) I$$

Power angle equation jX_s



$$P = \frac{E_1 E_2}{X_s} \sin \delta$$

E_1 : Magnitude of voltage at bus1

E_2 : Magnitude of voltage at bus2

δ : $\delta_1 - \delta_2$

X_s : Reactance

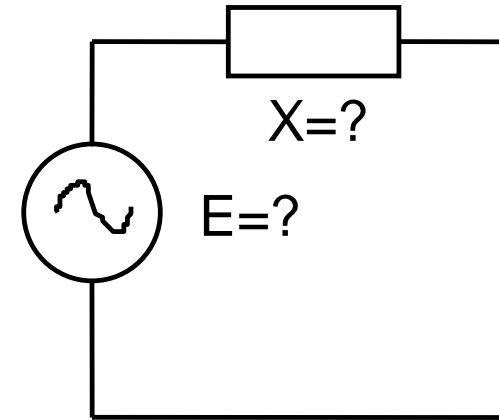


Machine Parameters

Synchronous : Steady state, sustained.

Transient : Slowly decaying

Sub-transient : Rapidly decaying



$$X_d \geq X_q \geq X_q' > X_q'' \geq X_d''$$

$$T_{d0}' > T_{d0}''$$

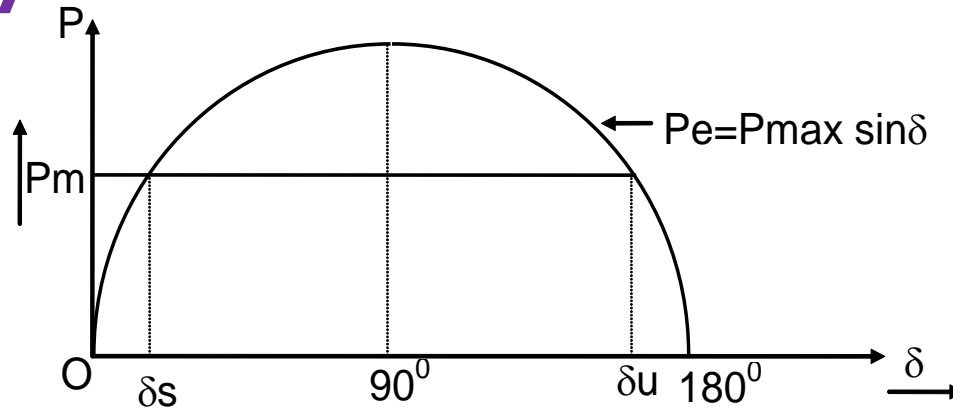
$$T_{q0}' > T_{q0}''$$

Typical values



Parameter	Hydro (pu)	Thermal (pu)
X_d	0.6 - 1.5	1.0 - 2.3
X_q	0.4 - 1.0	1.0 - 2.3
X_d'	0.2 - 0.5	0.15 - 0.4
X_q'	-----	0.3 - 1.0
X_d''	0.15 - 0.35	0.12 - 0.25
X_q''	0.2 - 0.45	0.12 - 0.25
T_{d0}'	1.5 - 9.0 s	3.0 - 10.0 s
T_{q0}'	-----	0.5 - 2.0 s
T_{d0}''	0.01 - 0.05 s	0.02 - 0.05 s
T_{q0}''	0.01 - 0.09 s	0.02 - 0.05 s
R_a	0.002 - 0.02	0.0015 - 0.005

Stability



Stable

- At δ_s ; $P_m = P_e$; net accelerating torque = 0.
- Let P_e decrease slightly.

- $$\frac{H}{\pi f} \frac{d^2 \delta}{dt^2} = P_m - P_e$$

δ increase (acceleration)

δ comes back to original position.

- Stable region . Hence δ_s is stable operating point.



Unstable

- At δ_u ; $P_m = P_e$; Net accelerating torque = 0
- Let P_e decrease slightly.
- $$\frac{H}{\pi f} \frac{d^2 \delta}{dt^2} = P_m - P_e \text{ is } +ve$$
 δ increases, (acceleration)
- P_e further decreases.
- Chain reaction $\rightarrow \delta$ never comes back to normal value .

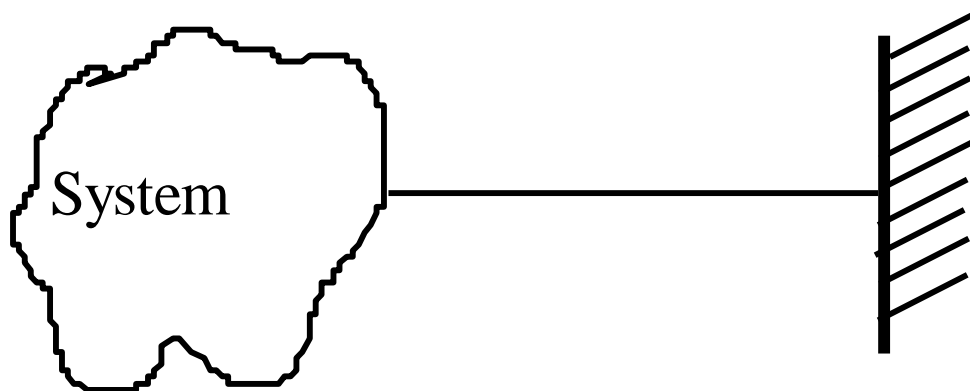
Hence δ_u is unstable operating point.

Infinite bus



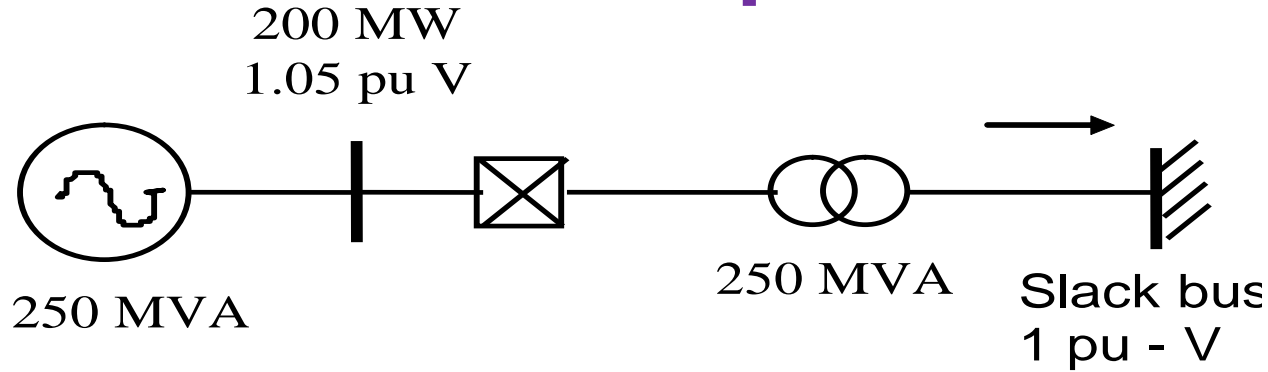
Generator connected to infinite bus.

- High inertia. $H \gg$ compared to other machines in the system.
- Frequency is constant.
- Low impedance. X_d' is very small.
- E' is constant and V_t is fixed.
- Infinite fault level symbol.





Example :



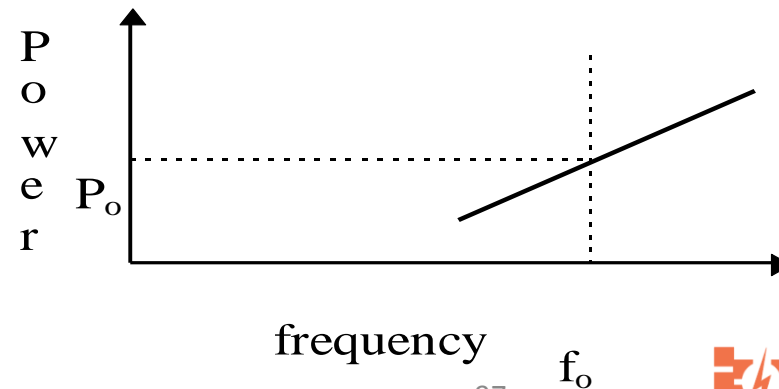
$H = 3.2$, $Z = 10\%$ on own rating , $X_d^1 = 25\%$, tap = 1,
 $R_a = 0.0$ and neglect R.

1. Establish the initial condition.
2. Perform the transient stability without disturbance.
3. Open the transformer as outage & do the study.
4. How long the breaker can be kept open before closing, without losing synchronism.





- Vary the tap.
- Switch on the capacitor.
- Determine the response (charge) in load.
- Compute the parameters. $P = P_0 (C_P + C_I \cdot V + C_Z \cdot V^2) (1 + K_f \cdot f)$
- P varies with time, voltage and frequency.
- P_0 varies with time - can be constant at a given time of a day.
- C_P , C_I , C_Z & K_f are constants.
- V & f are known at any time instant.
- P is known from measurements.
- Solve the non linear problem over a set of measurements.





Let the load be 10,000 MW. i.e. $P_0 = 10,000$

Let for 1 Hz change in frequency, let the load change be 700 MW.

$$P_o \times \Delta f \times C_f^P = -700 (\text{decrease in load})$$

$$P_o (f - f_o) \times C_f^P = \frac{-700}{-1} = 700 \text{ power number}$$

$$C_f^P = \frac{700}{10,000} \Rightarrow 7\%$$

If P is in pu; Δf is the per unit change in frequency then on 100 MVA base :

$$C_f^P = \frac{7}{1} \frac{100}{50} = 3.5$$

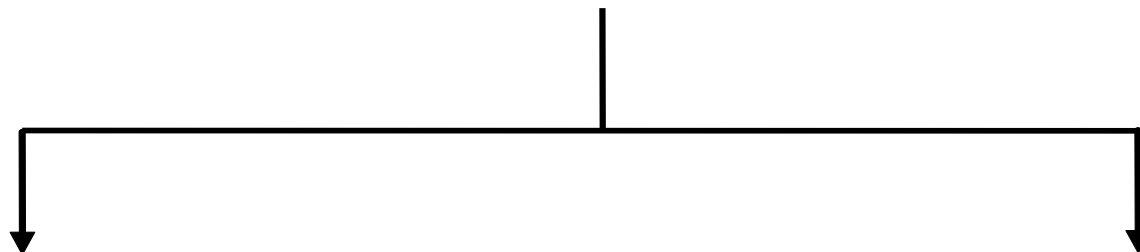
What it implies :

- Initial load 10,000 MW.
- Loss of generation 700 MW
- Increase in load 700 MW
- Frequency 49 Hz.

Load Model Parameters



Load model paraters



Measurement based approach

Input: Connected load

Measurement: P,V, f over a period

Out put: Parameters

Component based approach

Industrial

Commercial

residential

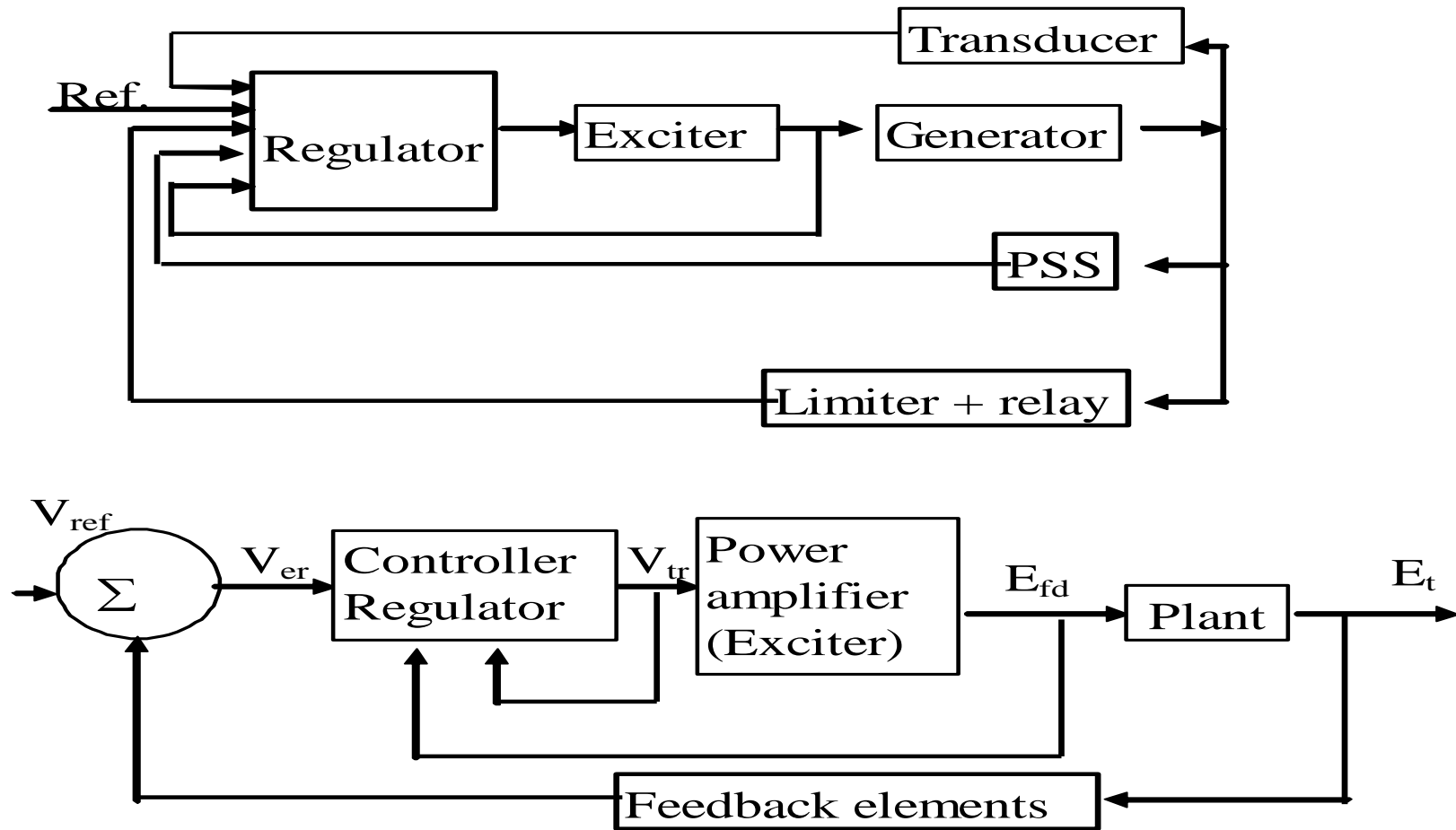
Agricultural



Component	pf	$\partial P/\partial V$	$\partial Q/\partial V$	$\partial P/\partial f$	$\partial Q/\partial f$
Air conditioner 3 p central heating	0.90	0.088	2.5	0.98	-1.3
Arc furnace	0.7	2.3	1.6	-1.0	-1.0
Industrial Motors	0.88	0.07	0.5	2.5	1.2
Agricultural pumps	0.85	1.4	1.4	5.0	4.0
Residential					
Summer	0.9	1.2	2.9	0.8	-2.2
winter	0.99	1.5	3.2	1.0	-1.5
Commercial					
summer	0.85	0.99	3.5	1.2	-1.6
winter	0.9	1.3	3.1	1.5	-1.1
Industrial	0.85	0.18	6.0	2.6	1.6
Power plant	0.8	0.1	1.6	2.9	1.8



Excitation System Components



Block Schematic



Reactive Power Control

- Synchronous generators
- Overhead lines / Under ground cables
- Transformers
- Loads
- Compensating devices



Control Devices:

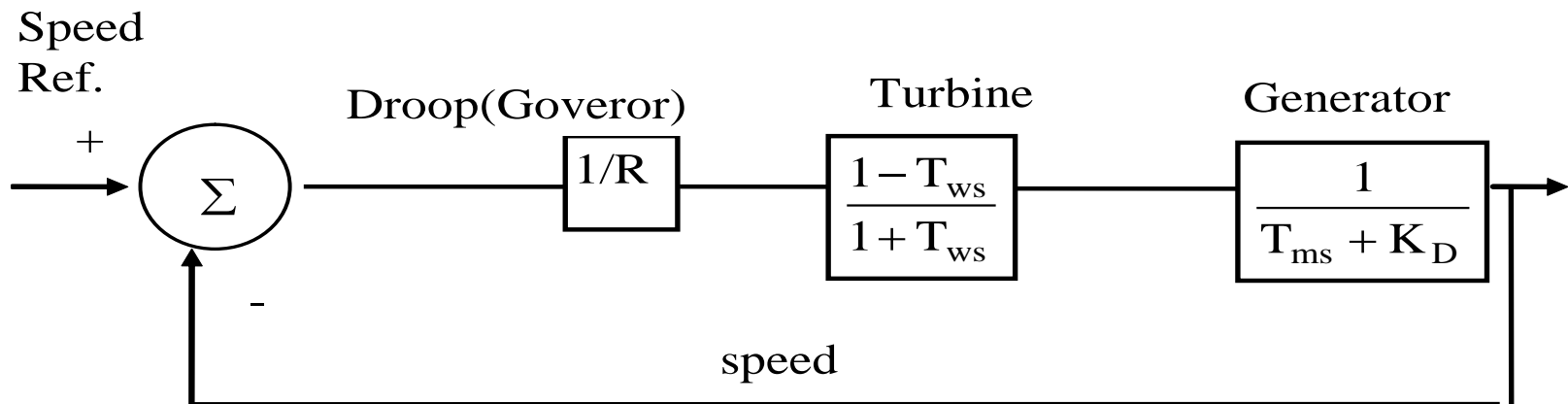
- Sources /Sinks --- Shunt capacitor, Shunt inductor (Reactor), Synchronous condenser, and SVC.
- Line reactance compensation --- Series capacitor
- Transformer -----OLTC, boosters





Types of Control:

- Primary Control : Governor action
- Secondary Control : AGC, load frequency control (For selected generators)



Under Frequency operation:

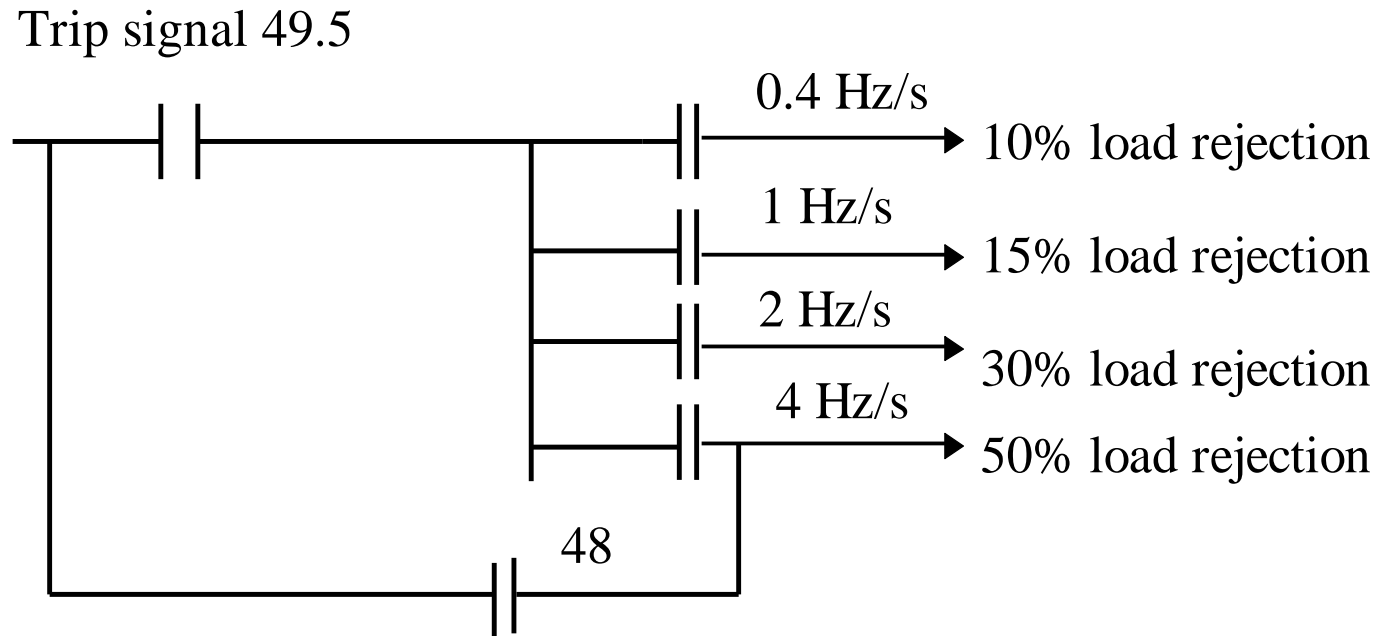
- Vibratory stress on the long low pressure turbine blades
- Degradation in the performance of plant auxiliaries say, induction motor.



Limitations:

- Only maximum spinning reserve can be achieved
- Turbine pickup delay
- Boiler slow dynamics
- Speed governor delay

Load Shedding:



Other measures:

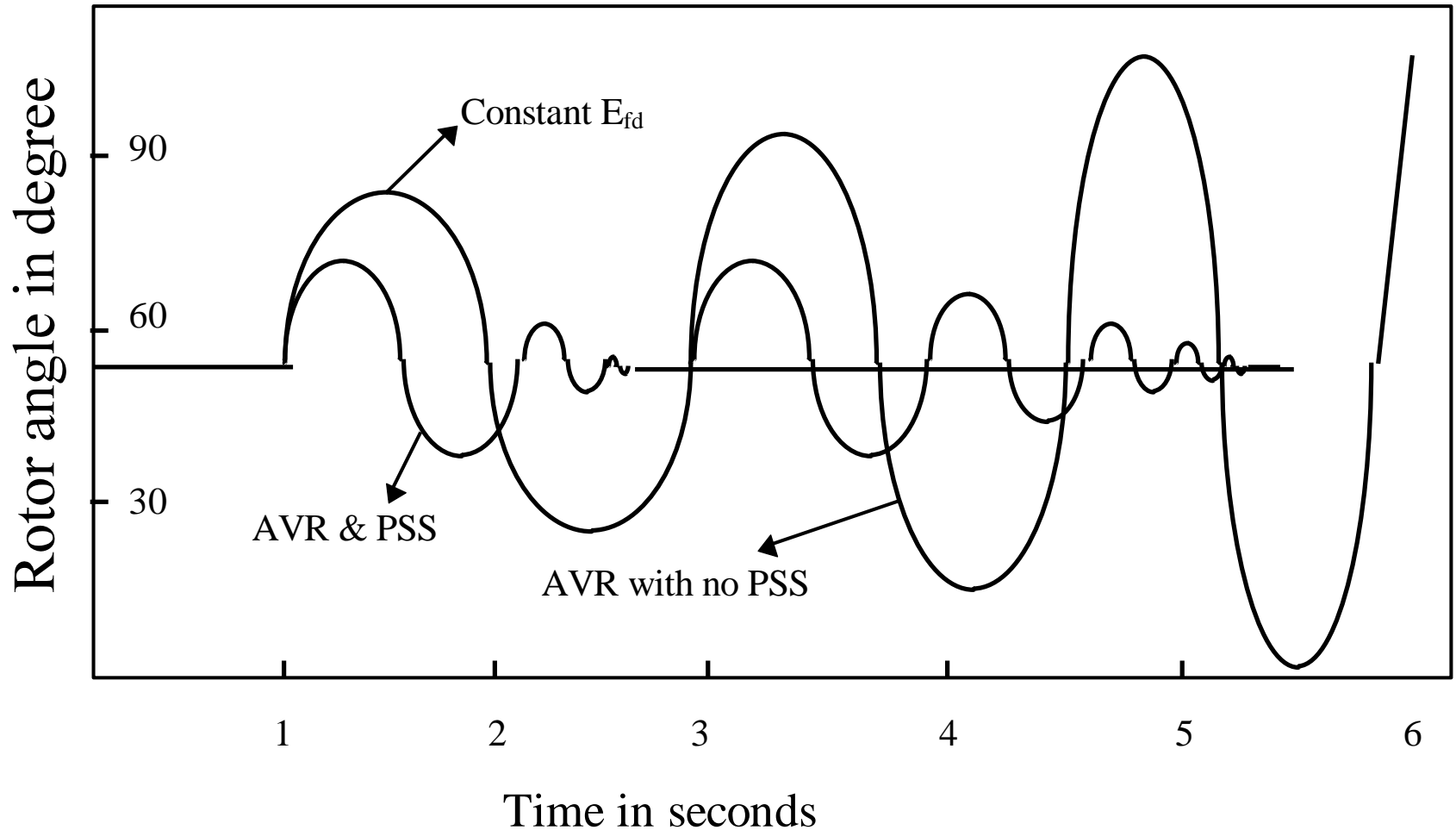
- * Fast valving
- * Steam by-passing



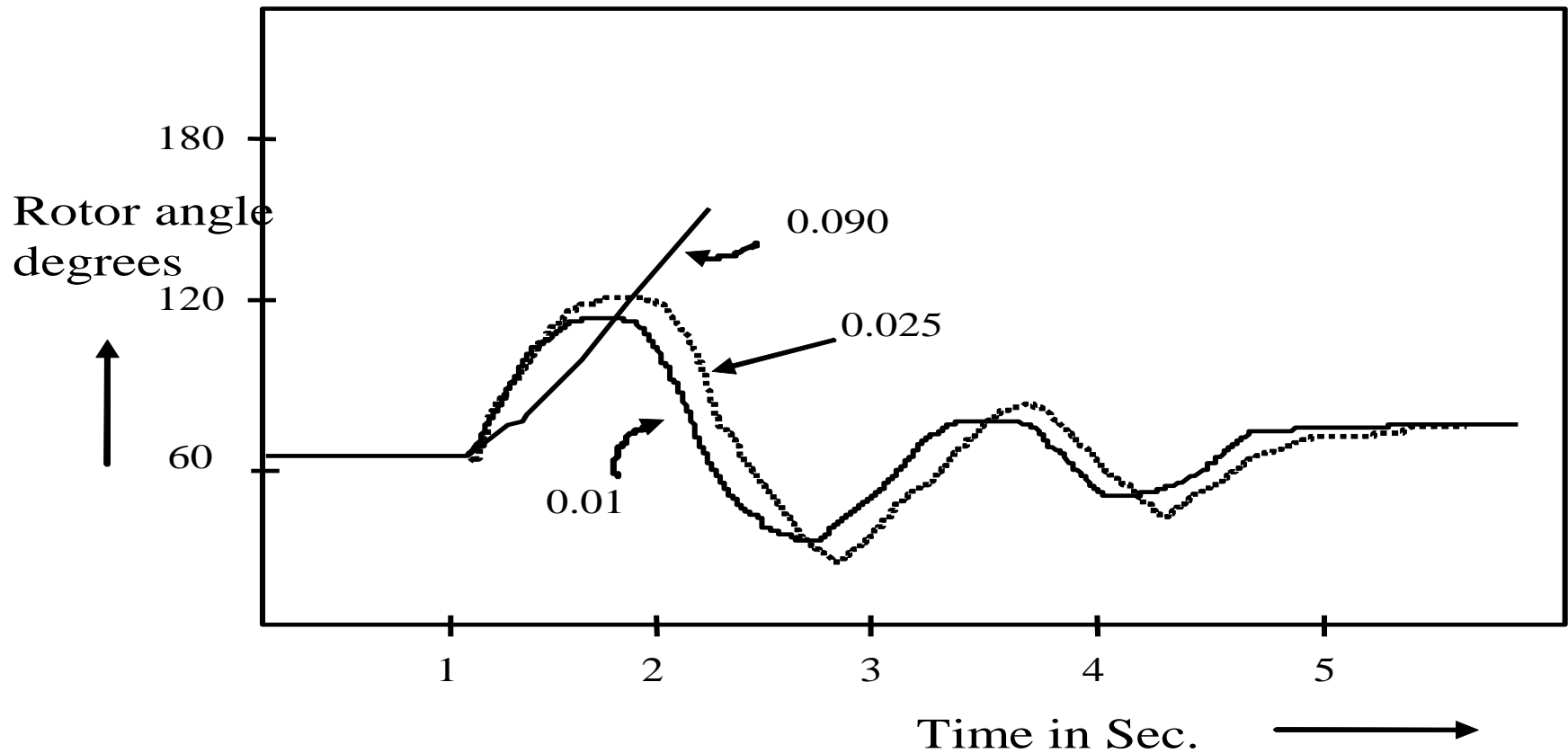
Modules in a Program:

1. Data reading
2. Initialization
 - Steady state load flow
 - Control block parameter AVR, Gov., Machine, Motor, PSS, VDC, SVC.
3. Disturbance model
4. Control block modeling
5. Machine modeling
6. Load flow solution
7. Protective relay modeling
8. Special functions
 - Cyclic load
 - Arc furnace
 - Re-closure
9. Results output
 - Report
 - Graph

Typical Swing Curve :

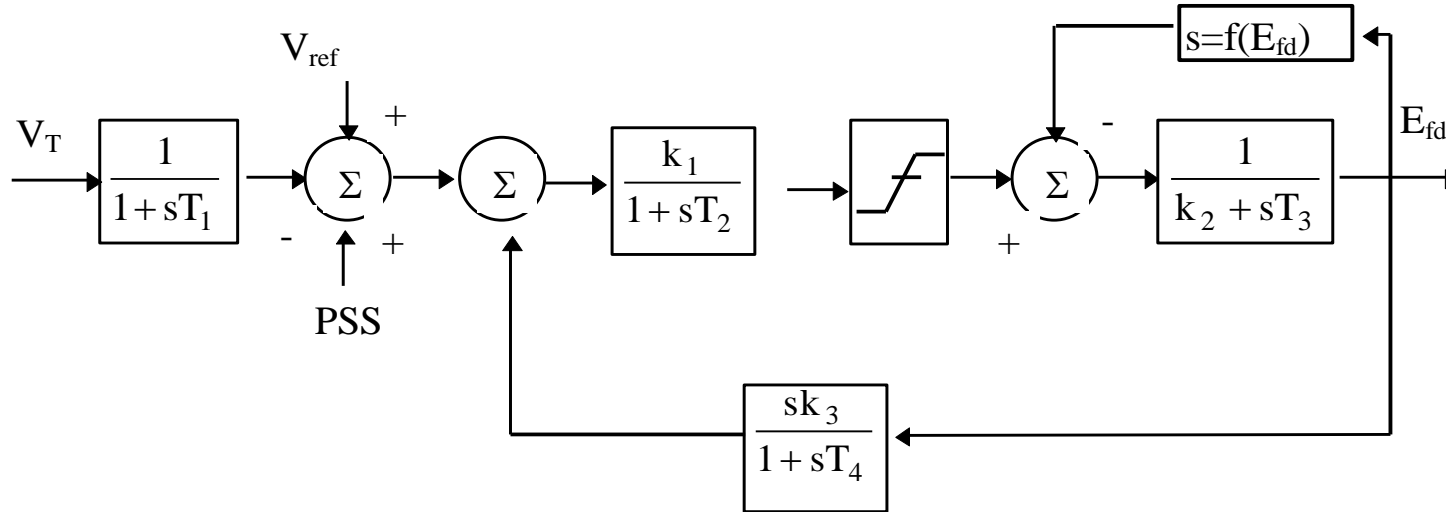


Typical Swing Curve :



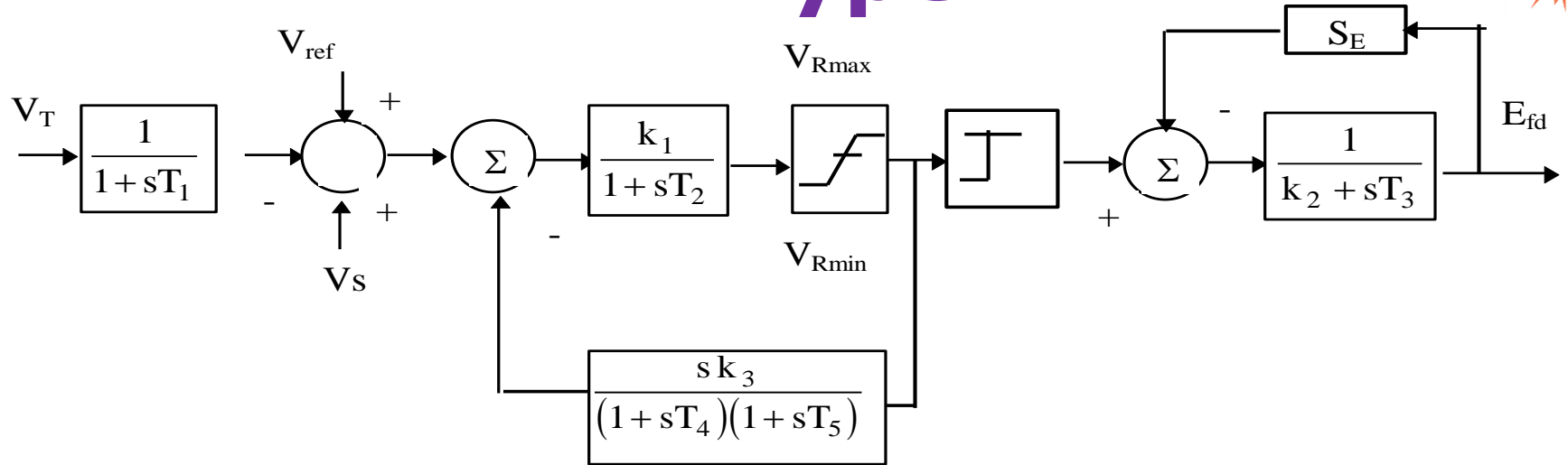
Integration step size : Typical value : 0.01 seconds,
Range : 0.005 to 0.02 seconds

AVR : Type 1



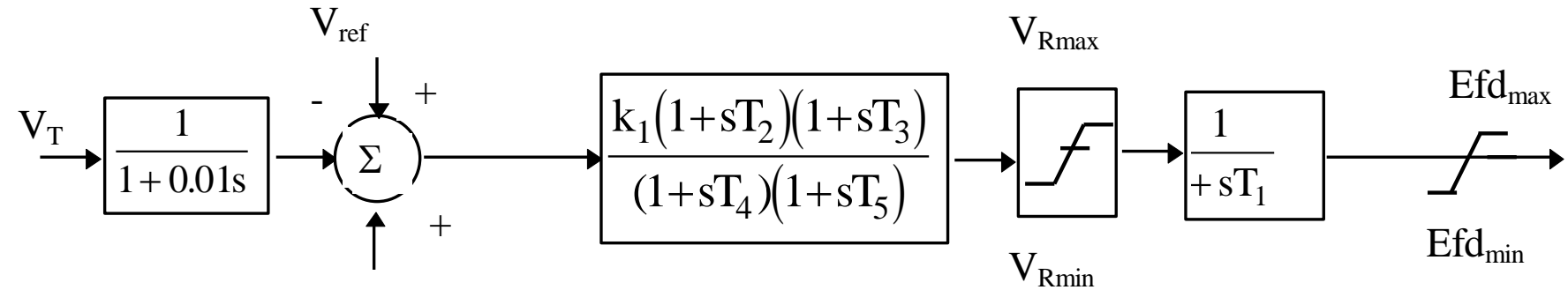
Mapping		Range
T_1	T_r	0.01 -- 0.10
T_2	T_a	0.025 -- 0.2
T_3	T_E	0.5 -- 1.0
T_4	T_{F1}	0.5 -- 1.0
K_1	K_A	25 -- 200
K_2	K_E	-0.5 -- 1.0
K_3	K_F	0.01 -- 0.1

AVR : Type 2



Mapping		Range
T_1	T_R	0.01 --- 0.05
T_2	T_A	0.01 --- 0.05
T_3	T_E	0.5 --- 1.0
T_4	T_{F1}	$\cong 1.0$
T_5	T_{F2}	$\cong 0.1$
k_1	K_A	50--200-400-600
k_2	K_E	$\cong 1.0$
k_3	K_f	0.01 - 0.05

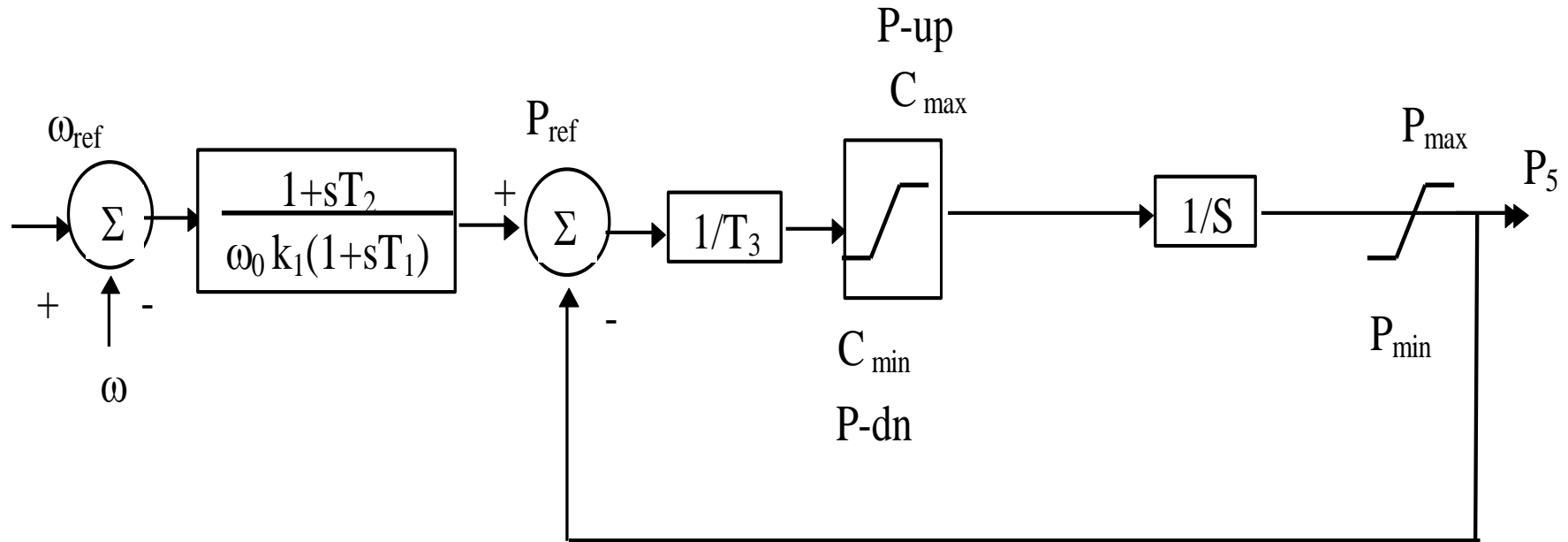
AVR TYPE – 5



Mapping		Range
0.01	T_r	0.01 -- 0.025
T_1	T_s	0.025
T_2	T_E	$\cong 1.0$
T_3	T_{F1}	$\cong 0.06$
T_4	T_A	40.0
T_5	T_{F2}	$\cong 0.024$
k_1	k_A	$\cong 200.0$



Steam Turbine Governing System



$K_1 : 0.05 - 0.04$

$T_1 : 0.1$

$T_2 : 0.03$

$T_3 : 0.4$

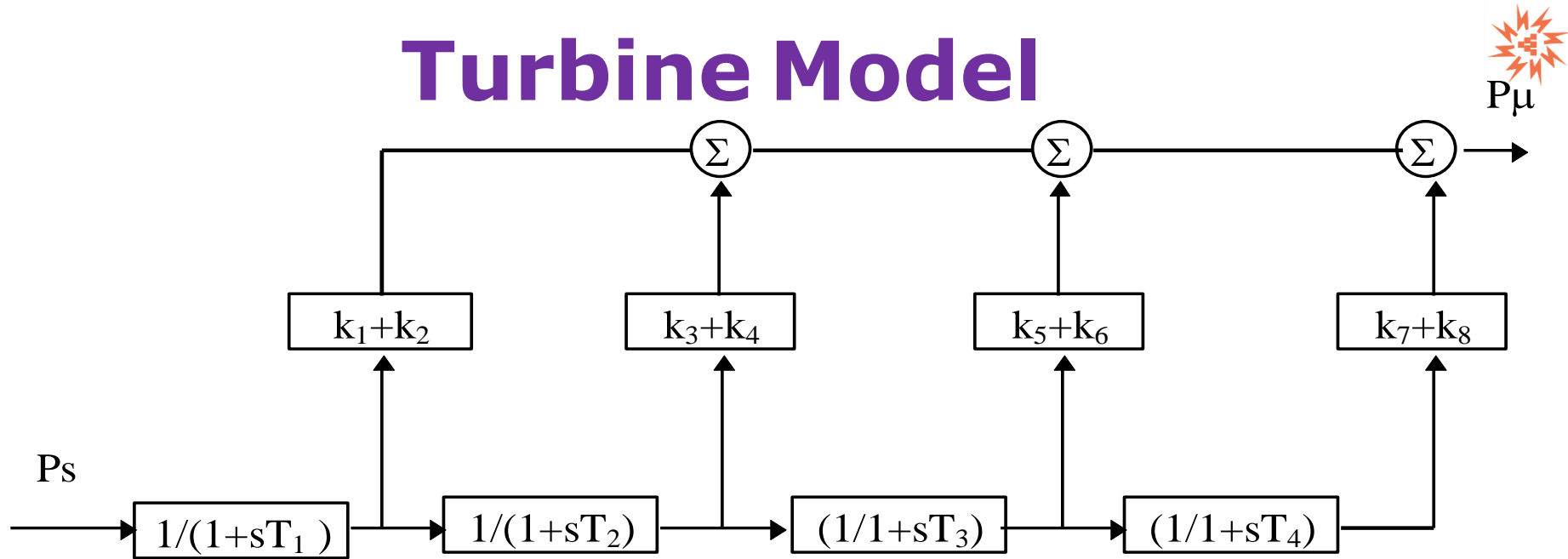
$P_{max} : 1.0$

$P_{min} : 0.0$

$P_{up} : 0.1$

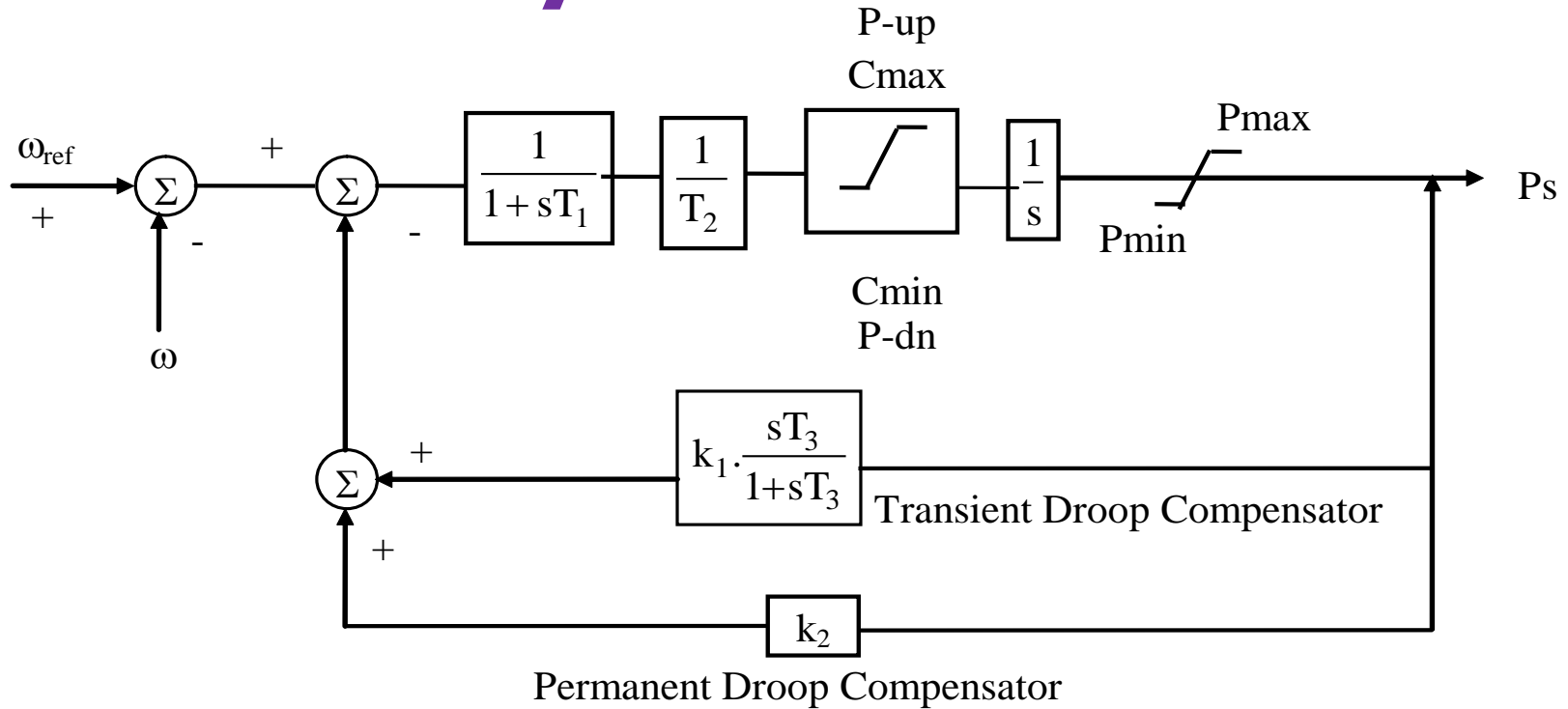
$P_{dn} : -1.0$

Turbine Model



T_1 : 0.26	k_1 : 0.2760	$k_1 + k_2$: VHP
T_2 : 10.0	k_3 : 0.324	$k_3 + k_4$: HP
T_3 : 0.5	k_5 : 0.4	$k_5 + k_6$: IP
T_4 : 99.9	k_7 : 0.0	$k_7 + k_8$: LP

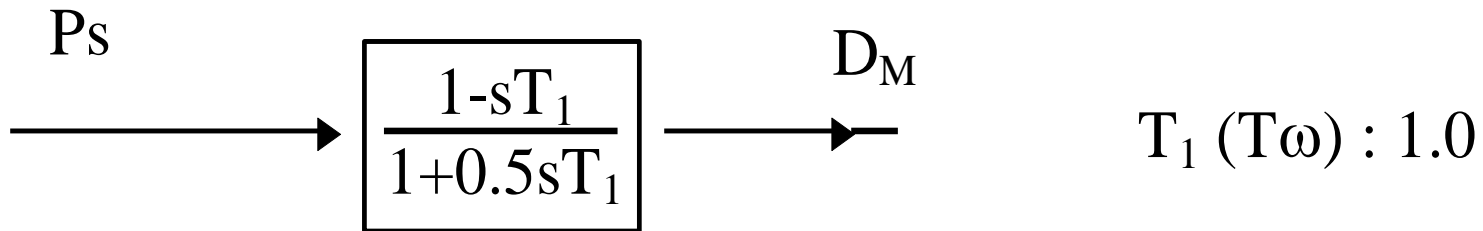
Hydro Governor



$k_1 : 0.36$	$P_{max} : 1.1$	$T_2 : 0.2$
$k_2 : 0.04$	$P_{min} : 0.0$	$T_3 : 5.0$
$T_1 : 0.05$	$P_{up} : 0.1$	$P_{down} : -1.0$



Hydro Turbine



Transient Stability Enhancement

Philosophy :

1. Minimize the disturbance influence by minimizing the fault severity and duration.
2. Increase the restoring synchronizing forces.
3. Reduce accelerating torque.

Transient Stability Enhancement



Methods :

1. High speed fault clearing.
2. Reduction of transmission system reactance.
3. Regulated shunt compensation.
4. Dynamic Braking.
5. Reactor switching.
6. Independent pole operation of circuit breaker.
7. Single pole switching
8. Fast valaving.
9. Generator tripping.
10. Controlled system separation and load shedding.
11. High speed excitation systems.
12. HVDC transmission link control.



Major references used in the development of Transient Stability Studies Module

1. Dommel, N. Sato "Fast Transient Stability Solutions", IEEE Transactions on Power Apparatus and Systems, 1972, PP 1643 - 1650.
2. W. Dommel, "Digital computer solution of electromagnetic transients in single and multiphase networks", IEEE Transactions on Power Apparatus and Systems, April 1969, Vol. PAS-88, PP 388 - 399.
3. IEEE Committee Report, "Dynamic Models for Steam and Hydro Turbines in Power System Studies", IEEE PES Winter Meeting, New York, Jan./Feb. 1973. (Paper T 73 089-0).
4. IEEE Committee Report, "Proposed Excitation System Definitions for Synchronous Machines", IEEE Transactions on Power Apparatus and Systems, Vol. PAS-88, No. 8, August 1969.
5. IEEE Committee Report, "Computer representation of excitation systems", IEEE Transactions Power on Apparatus and Systems, June 1968, Vol. PAS-87, PP 1460 - 1464.



Queries & Discussions





Thank You





Introduction to Power System Protection



Topics for Discussion

- Protective relaying
- Need for protection
- Types of Protection
- General Philosophy
- Over-Current Relays
- Distance Relays



Introduction



Protective Relaying

- Safeguard equipment from damage during abnormal operating conditions.
- Protective Relaying should:
 - ✓ Ensure normal operation
 - ✓ Prevent equipment failure
 - ✓ Limit the effects of disturbances



Need for Protection

- Loss of equipment (Permanent or Partial damage)
- Loss of production
- Revenue loss
- Fire hazard, loss of life
- Loss of confidence level in using electricity as a commodity



Functions of Protection

- Primary function - Prompt removal of faulty element suffering a short circuit, or when it starts to operate in an abnormal manner
- Secondary function, to provide indication of location and type of failure

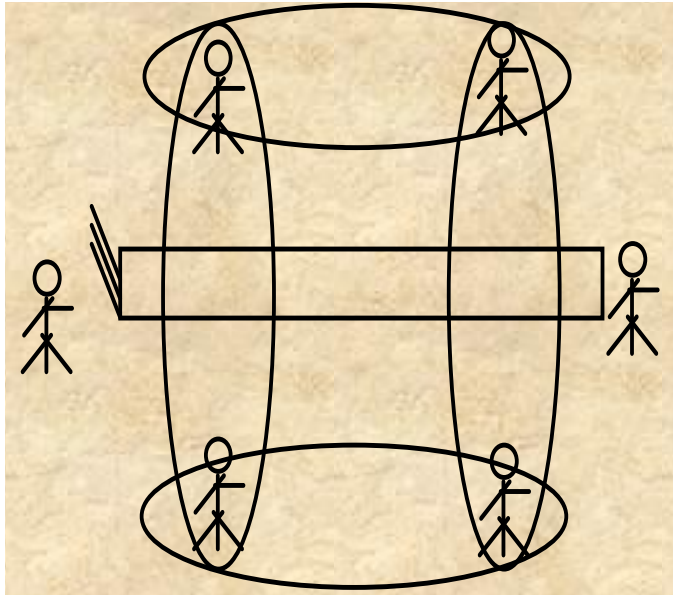


Types of Protection

- Over voltage protection – Lightning/Surge arrestors, Insulation co-ordination
- Fault protection (over loading/current) – Application of Relays
- Protection for human (safety) – Earthing and Earth mats, clearances, insulation



Protection Philosophy



Cricket	Protection
Position the fielders	Designs the system and sets the relays
Delivers the ball	Charges the system
Batsman hits the ball	Fault occurs
Mid-off stops/fails	Primary relay operates/ fails
Long-off stops/ fails	Backup relay operates / fails
Match lost ?	Loss of Power/Revenue



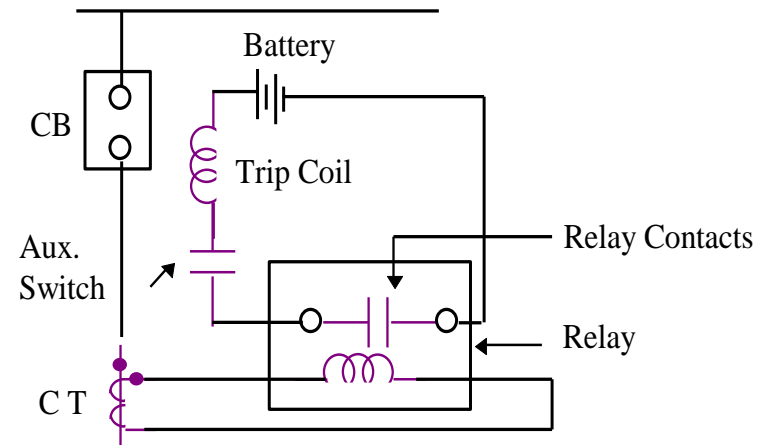
Protection Features

- Sensitive – detection of short circuit or abnormal condition
- Selectivity – ensure that only the unhealthy part of the system is disconnected
- Speed – to prevent or minimize damage and risk of instability of machines
- Reliability – to ensure proper action even after long periods of inactivity and also after repeated operations under severe conditions



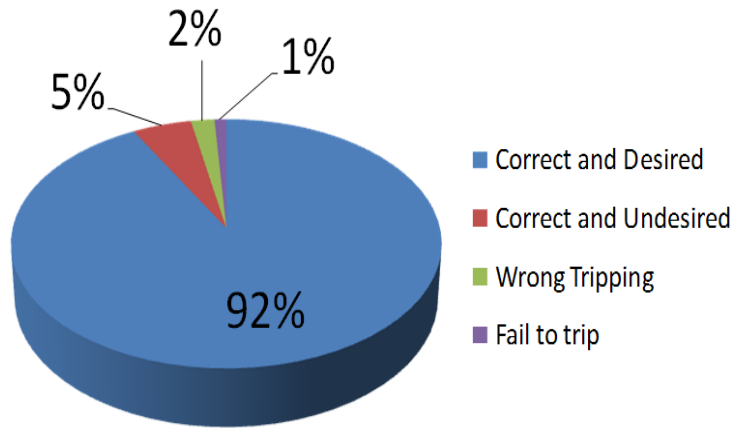
Protection System Design

- ❖ Design of circuit breakers and isolating devices
- ❖ Transducer (sensing devices)
- ❖ Relay design
- ❖ Relay application and co-ordination
- ❖ Simulation and testing





Protection Statistics



- ❖ Correct and Undesired
 - ❖ Operation as per the settings.
 - ❖ Settings are wrong, not updated
- ❖ Human Error
 - ❖ Leaving the trip circuit open after test
 - ❖ Open circuited trip coils
 - ❖ Mechanical failure of circuit breaker



Causes of Protection Failure

- Current or voltage supply to the relays
- DC-tripping voltage
- Protective relays
- Tripping circuit or breaker mechanism
- Circuit breaker



Equipment Selection

- Relay selection
 - ✓ Selecting a relay scheme to recognize the existence of a fault within a given protective zone
 - ✓ Initiate circuit breaker operation
- Circuit breaker selection
 - ✓ Determine the interruption requirement
 - ✓ Normal current and voltage rating
 - ✓ Selection of breakers and location



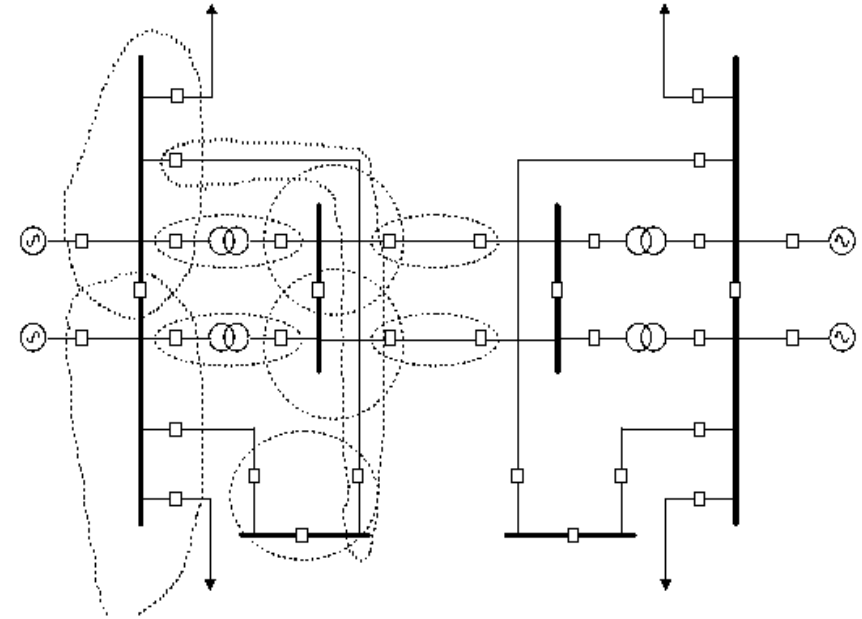
Fault Characteristics

- Magnitude
- Frequency
- Phase angle
- Duration
- Rate of change
- Direction or order of change
- Harmonics or the wave shape



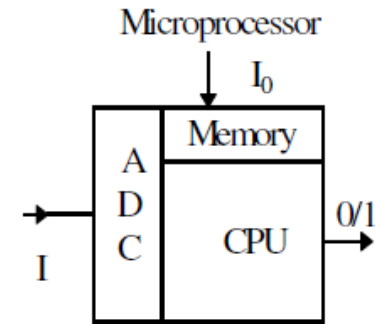
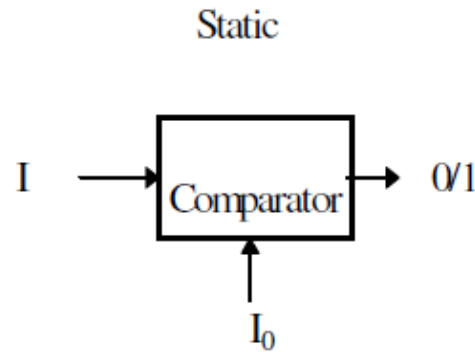
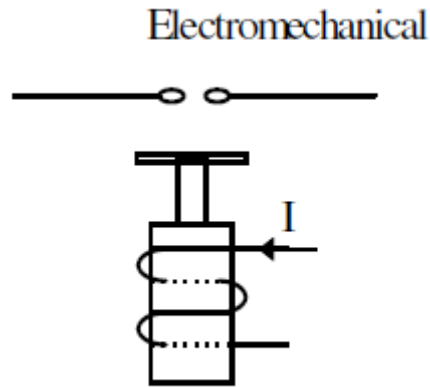
Protection Scheme Design

- Divide the system into zones
- Design appropriate breakers
- Minimize the amount of load being disconnected



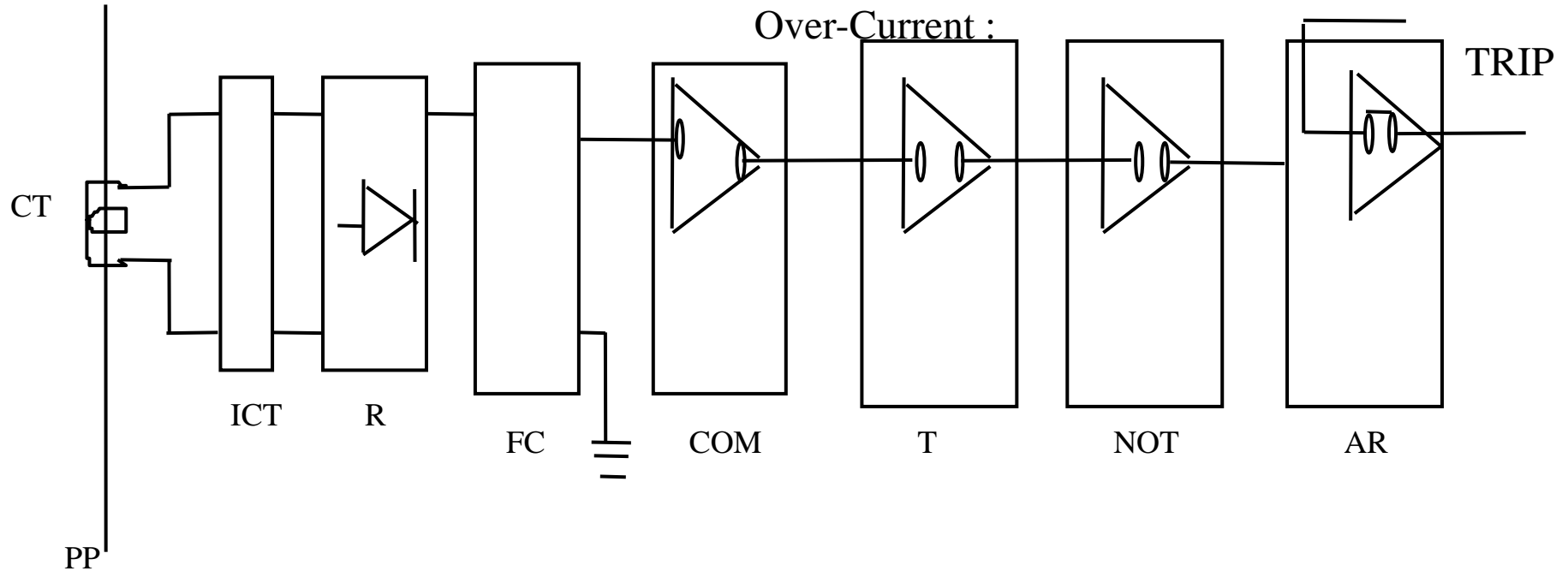


Types of Relays



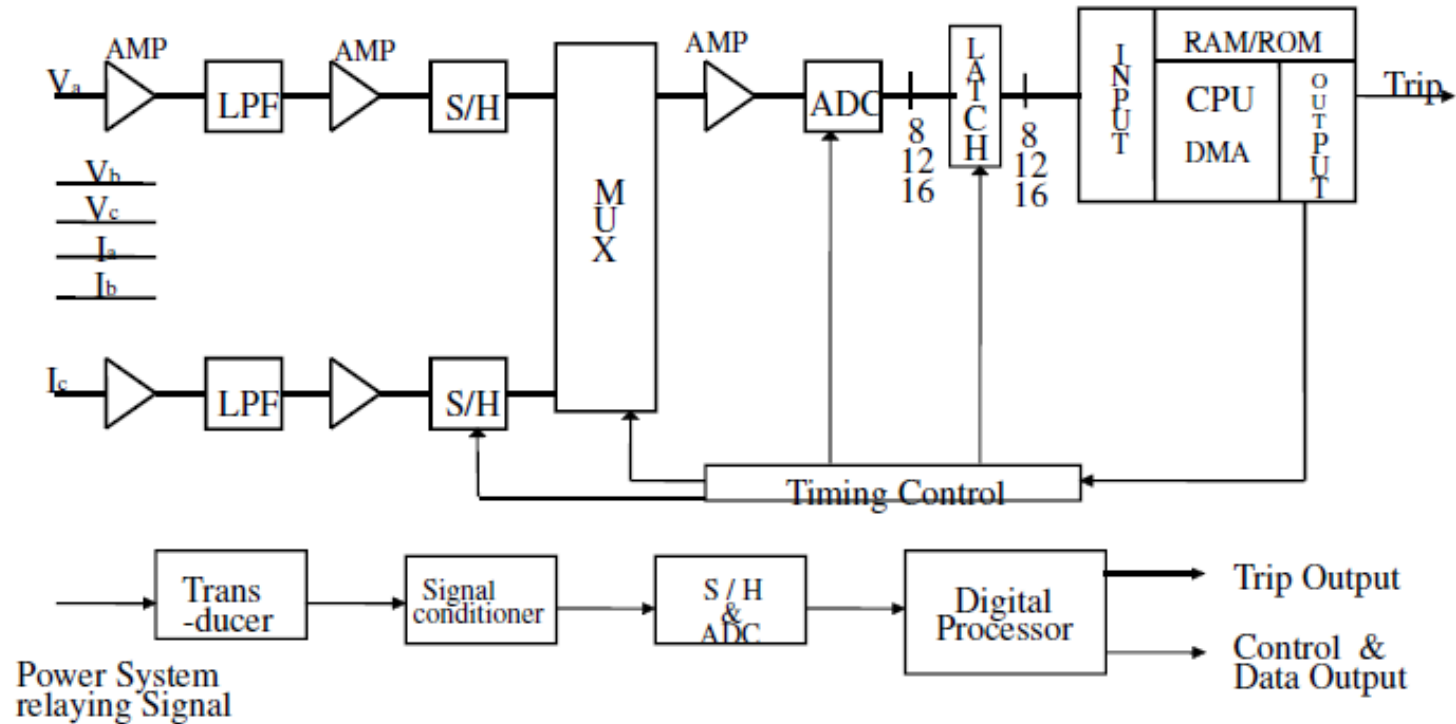


Schematic of a Static Relay





Schematic of an NR





Over-Current Relays



Basics

- Relays operate based on the current sensed.
- Can be used as primary or backup protection
- May be directional or non-directional
- Operation time depends on curve selected
- Settings involve selecting the plug setting and the time setting



Definitions

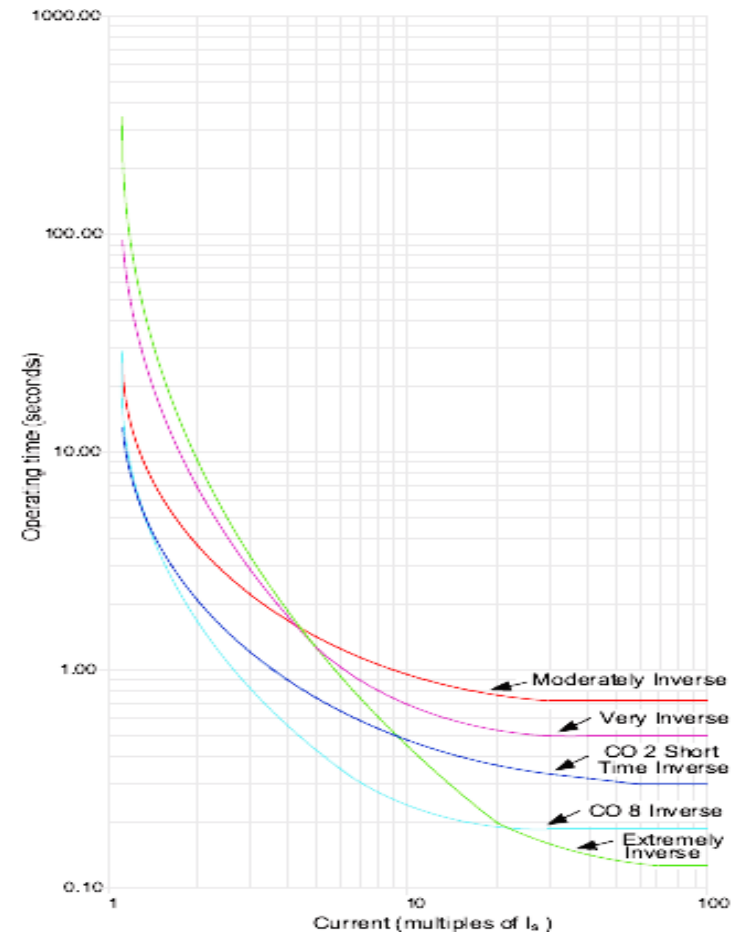
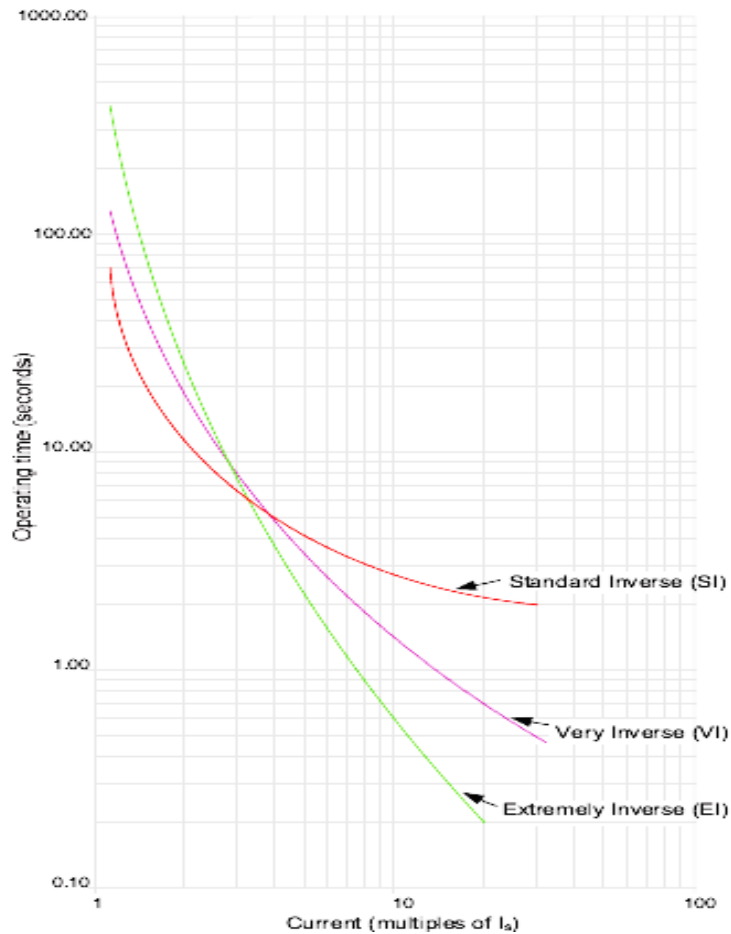
- **Plug Setting**

Plug setting is that value of current above which the relay should operate.

- **Time dial setting**

The time dial setting of the relay provides the discrimination between the primary and backup relay.

Standard Curves





Curve Equations

Relay Characteristic	Equation (IEC 60255)
Standard Inverse (SI)	$t = TMS \times \frac{0.14}{I_r^{0.02} - 1}$
Very Inverse (VI)	$t = TMS \times \frac{13.5}{I_r - 1}$
Extremely Inverse (EI)	$t = TMS \times \frac{80}{I_r^2 - 1}$
Long time standby earth fault	$t = TMS \times \frac{120}{I_r - 1}$



Relay Co-ordination

- Identification of main and backup relays
- Steady state analysis
- Determination of plug setting
- Determination of definite time setting
- Determination of time dial setting



Distance Relays



Basics

- *Distance relays are the most widely used relays for transmission lines protection.
- *The relay measures the distance in terms of impedance by measuring the voltage and current.
- *Major advantage is that relay acts as primary as well as remote back up.
- *The present digital distance relays offer more functionalities in terms of protection, monitoring and control rather than just impedance measurement



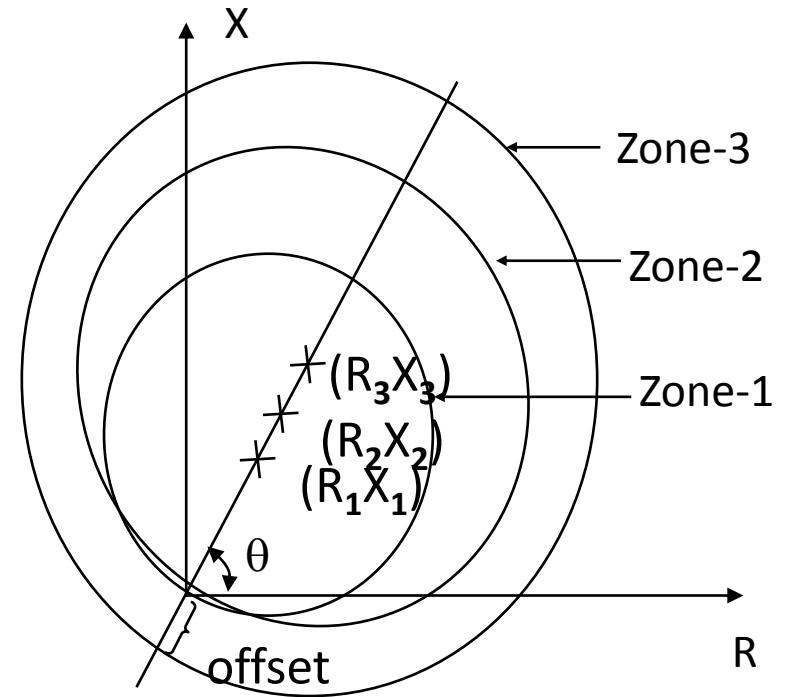
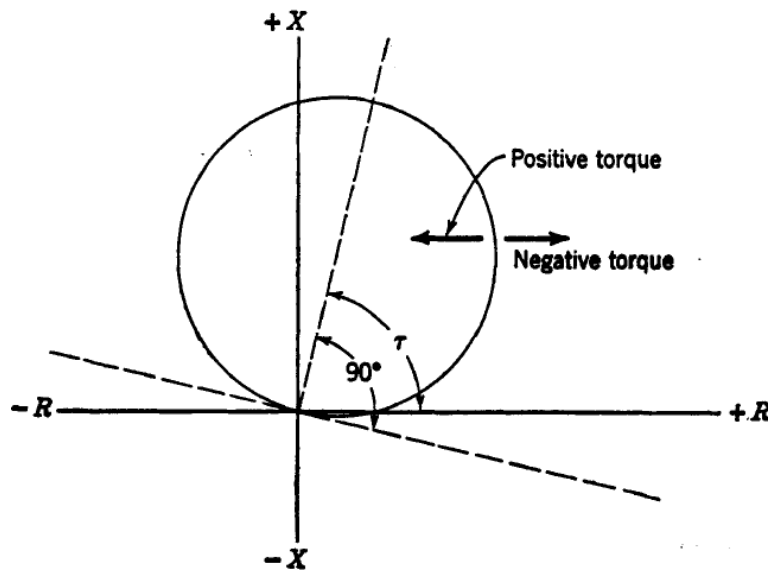
Types of Characteristics

- Mho
- Quadrilateral
- Lentical
- Quadra-Mho
- Elliptical Characteristics
- Circular



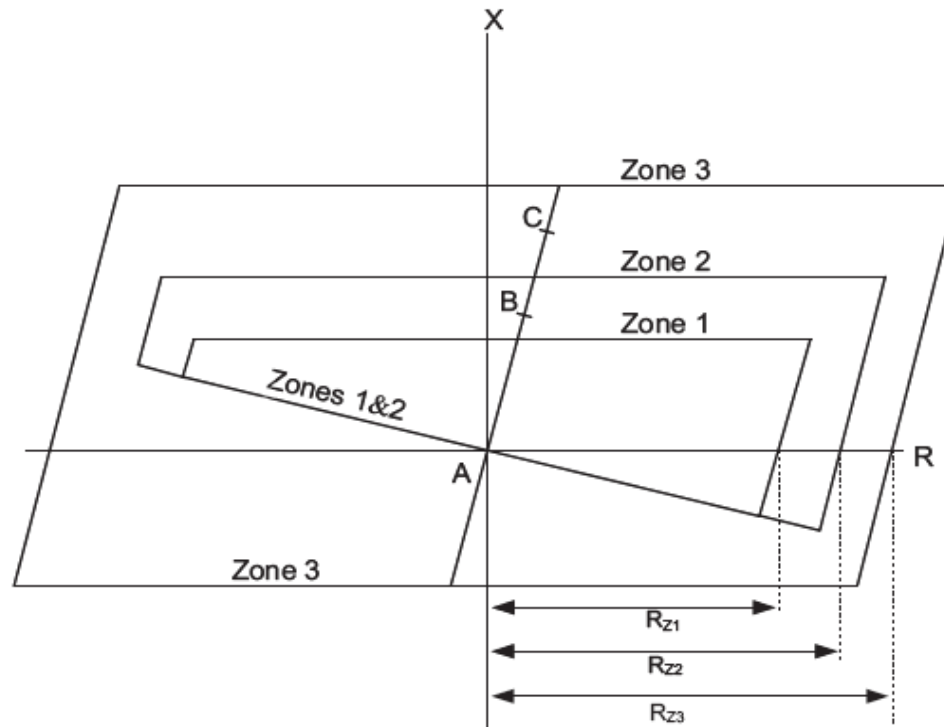
Mho Characteristic

$$Z = \frac{K_1}{K_2} \cos (\theta - \tau)$$





Quadrilateral Characteristics





Impedance Calculation

- Relays operate if the impedance seen is within the set characteristics known as zones.
- Separate zones are present for phase and earth loops.

$$Z_{AB} = \frac{V_B - V_A}{I_B - I_A}$$

$$Z_{AE} = \frac{V_{AE}}{I_A - \frac{Z_E}{Z_L} I_E}$$



Philosophy

Zone	Direction	Protected Reach	Time Setting (s)
Zone 1	Forward	80 % of the PL	Instantaneous
Zone 2 (for 400kV and above)	Forward	For Single Circuit – 120 % of the PL	0.35
		For Double Circuit – 150 % of PL	0.5 to 0.6 – If Z2 reach overreaches 50% of the shortest line; 0.35 – otherwise
Zone 2 (for 220kV and below)	Forward	120% of PL or 100% of PL + 50% of ASL	0.35

PL: Protected Line,

ASL: Adjacent Shortest Line,

ALL: Adjacent Longest Line



Philosophy

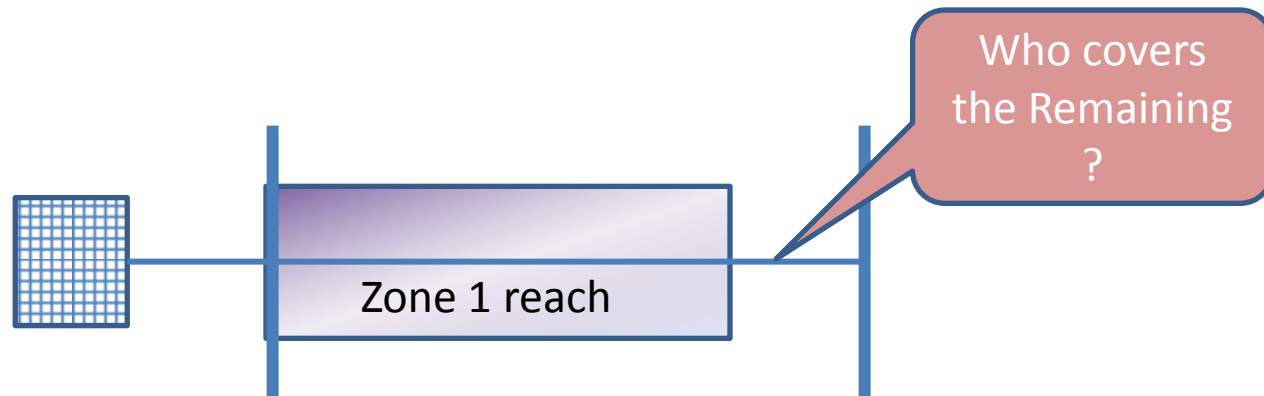
Zone	Direction	Protected Reach	Time Setting (s)
Zone 3	Forward	120% Of (PL + ALL)	0.8 to 1.0
Zone 4	Reverse	10% for the Long line (>100 km) 20% for short line (<100 km)	0.5 if Z4 overreaches 50% of reverse shortest line 0.35: otherwise

Note : Z2 reach should not encroach the next lower voltage level
: If Z3 reach encroaches next voltage level (after considering in feed), Z3 time must be coordinated
: If utility uses carrier blocking scheme, then the Z4 reach may be increased as the requirement. It should cover the LBB of local bus bar and should be coordinated with Z2 time of the all other lines.



Zone 1

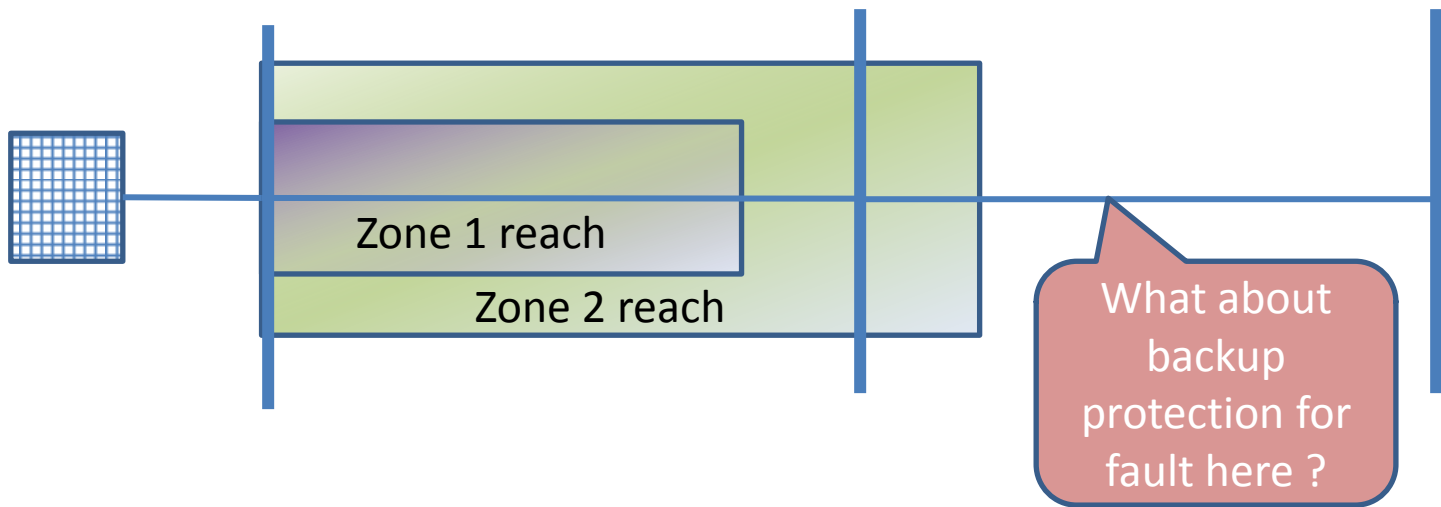
- Instrument Transformer errors
- Transmission line is not completely balanced
- Hence apparent impedance is susceptible to an error of 20%.
- Zone 1 is under reached to prevent incorrect operation for fault on next line (Eg. Close to adjacent bus)





Zone 2 for single circuit line

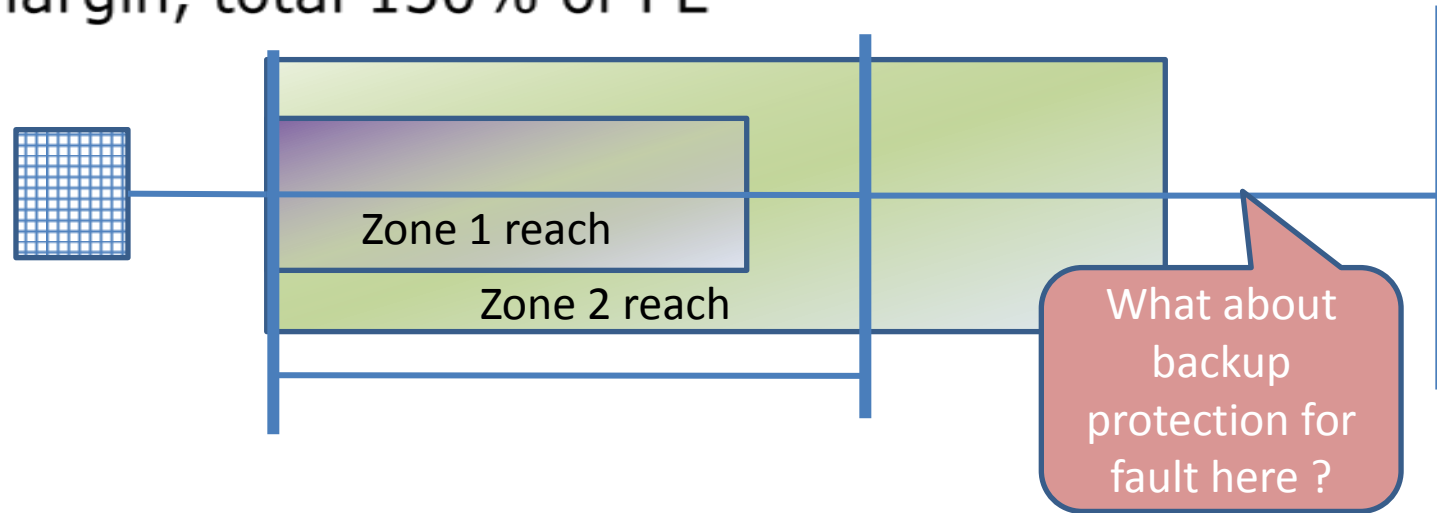
- To provide coverage to remaining portion of protected line
- Over reach margin should be min 20% (for reason discussed in Zone1)





Zone 2 for double circuit line

- Under reach due to mutual coupling between parallel line
- $\Delta Z = \frac{k_{0m}}{1+k_0}, k_{0m} = \frac{Z_{0m}}{3Z_1}, k_0 = \frac{Z_0-Z_1}{3Z_1}$
- For twin moose, $\Delta Z = 27\%$ considering additional 20% margin, total 150% of PL

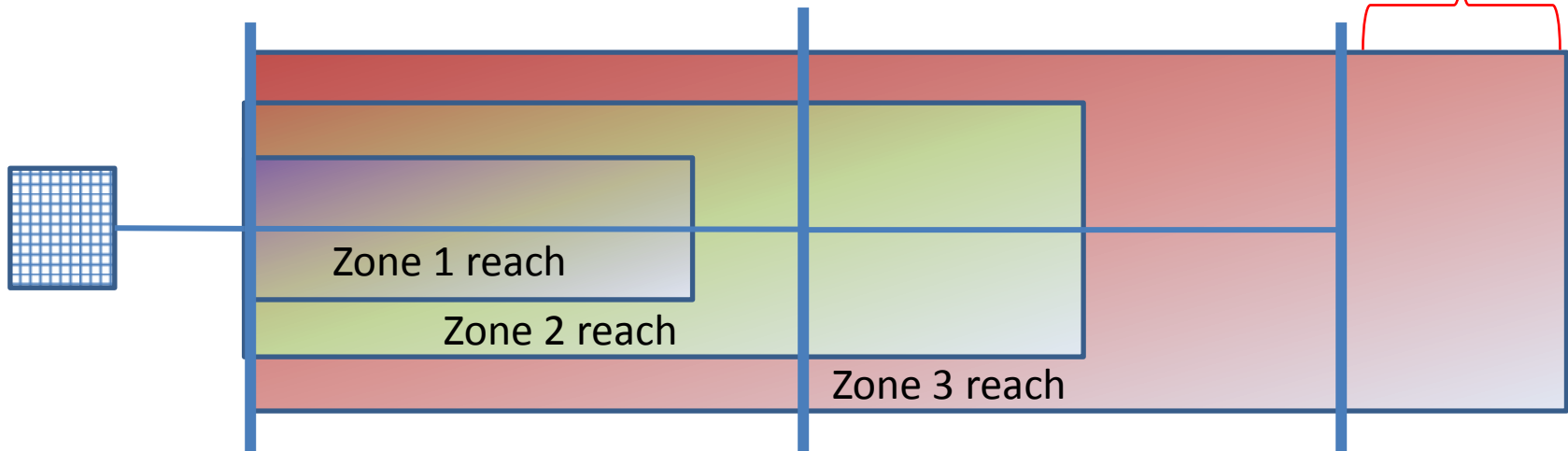




Zone 3

- Zone 3 protection is backup protection for fault on adjacent line.
- Need to reach the PL + ALL

Considering Errors





Resistive Reach (Zone 1)

- Earth
 - ✓ Should provide maximum coverage considering fault resistance, arc resistance and tower footing resistance.
 - ✓ Should be $< 4.5 * X1$ ($X1 = \text{Zone 1 reach}$)
- Phase
 - ✓ Reach should be set to provide coverage against all types of anticipated phase to phase faults subject to check of possibility against load point encroachment
 - ✓ Should be $< 3 * X1$

Resistive Reach (Zone 2 and Zone 3)



- The philosophy used for Zone 1 is applicable here also.
- Additionally
 - ✓ Due to in-feeds, the apparent fault resistance seen by relay is several times the actual value, this should be considered before arriving at the setting.



Queries and Discussions





Thank You



Protection Case Studies



Topics for Discussion

- Overcurrent Relays
- Distance Relays
- Differential Relays

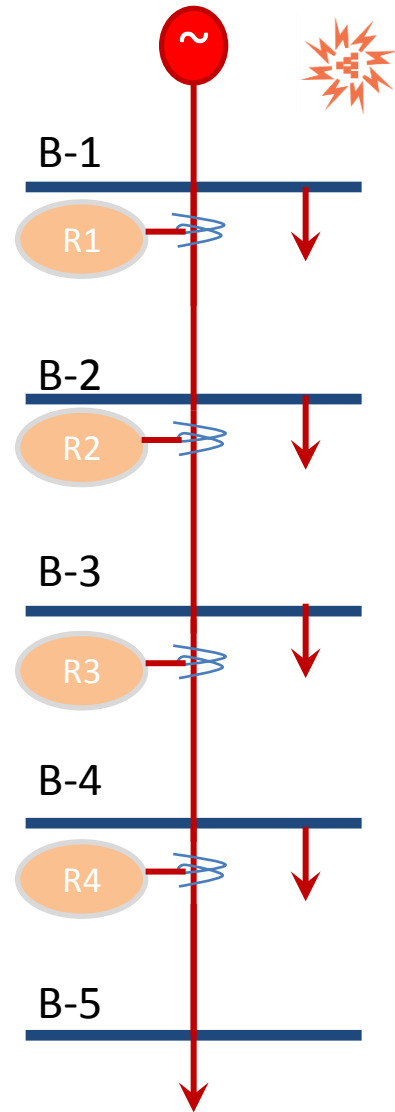


Overcurrent relays

Relay coordination sample

- Generator data
 - Generator fault level :
 - Maximum : 1000 MVA
 - Minimum : 500 MVA

Transmission Line Details			
Sl. No	From Bus	To Bus	Impedance(pu)
1	1	2	0.1
2	2	3	0.1
3	3	4	0.1
4	4	5	0.1





Relay data

SI No	Relay Name	Maximum Load Current(A)	CT rating	Relay Characteristics
1	R1	800	800/1	3s
2	R2	400	400/1	3s
3	R3	200	200/1	3s
4	R4	100	100/1	3s

Relay Pairs

SI No	Primary Relay	Backup Relay
1	R4	R3
2	R3	R2
3	R2	R1



Fault Studies results

Relay	Impedance	Fault Bus	Fault MVA	Fault Current in A
R1	0.1	1	1000	52486.388
R2	0.2	2	500	26243.194
R3	0.3	3	333.33	17495.288
R4	0.4	4	250	13121.590

SI No	Primary Relay	Backup Relay	Fault Bus	Backup Relay Current in A
1	R4	R3	4	13121.590
2	R3	R2	3	17495.288
3	R2	R1	5	26243.194



Plug setting computation

For Relay R4		
% Setting	Primary Setting	Remarks
50	50	< Load Current
75	75	< Load Current
100	100	= Load Current

Relay	Load Current	CT Rating	% Setting	Primary Current
R1	800	800/1	100	800
R2	400	400/1	100	400
R3	200	200/1	100	200
R4	100	100/1	100	100



Time setting computation

- Time of operation given by
- $t = \frac{3}{\log M} * TMS$
- $M = \frac{I_{sensed}}{I_{PS}}$
- Assuming minimum TMS of 0.05 for R4, time of operation is computed as:
- $t = \frac{3}{\log \frac{13121.59}{100}} * 0.05 \approx 0.071 s$



Time setting computation

- For R3,
- $t_{backup} = t_{primary} + t_{discrimination}$
- $= 0.07 + 0.4 = 0.47$
- Therefore, the TMS for R3 is given by:
 - $TMS = \frac{0.47 * \log \frac{13121.59}{200}}{3} \approx 0.29$
- Similarly for other relay pairs



Final relay settings

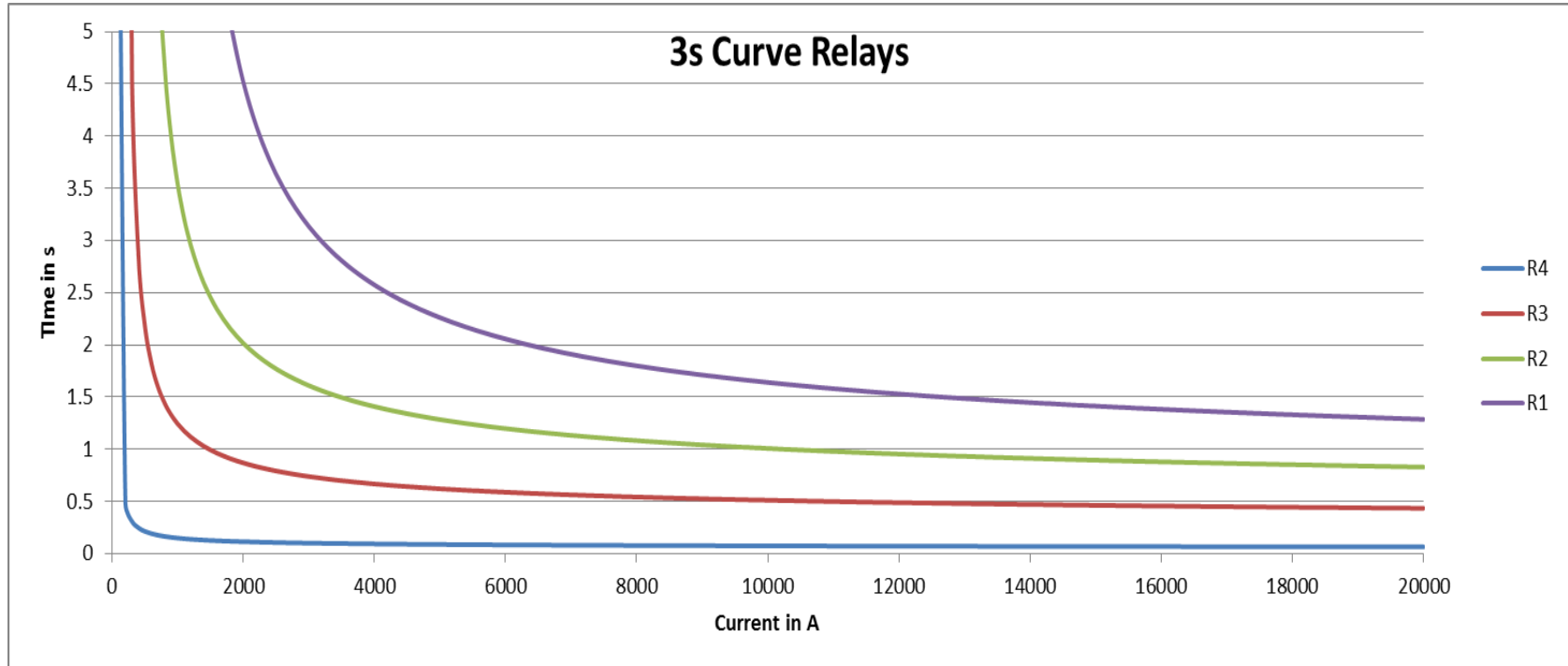
Relay	Plug Setting	TMS
R1	800	0.6
R2	400	0.47
R3	200	0.29
R4	100	0.05

Operating times for a fault at Bus 5, with a fault current of 10, 500 A

R1	≈ 1.61 s
R2	≈ 1.00 s
R3	≈ 0.51 s
R4	≈ 0.07 s



Co-ordinated Curves





Application

- Backup to distance relays (220/132 kV and below)
- HV and LV side of ICT as backup to differential relays
- DEF is used in 400 kV line as protection for high impedance earth faults.
- Non directional OC is also used in 400kV line under fuse fail condition

DOC Setting Philosophy



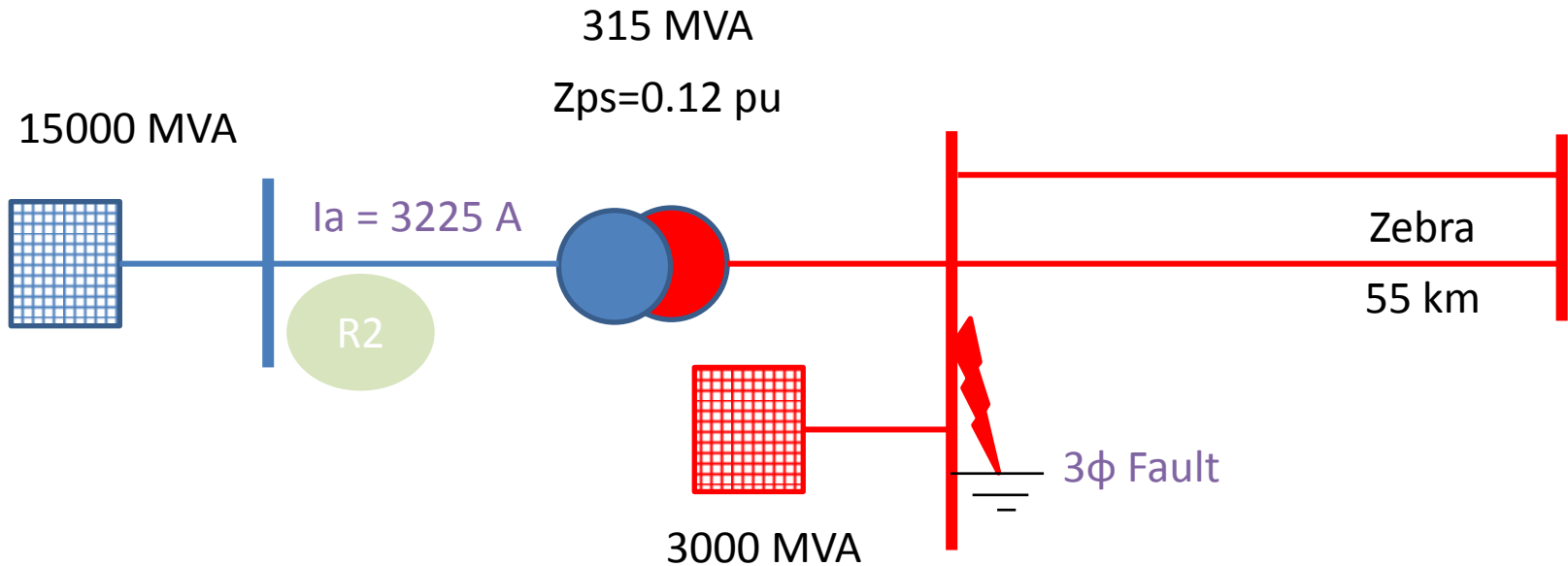
- For 220 kV and 132 kV line with only one main distance protection, DOC must be set in such a way that for fault at remote bus the DOC (IDMT) is coordinated with Zone 2 time typically 1.1 s
- For DOC at 400 kV side of ICT, it is to be set such that for fault at remote end bus (longest line), DOC (IDMT) is coordinated with Zone 3 time
- Instantaneous DOC can be used at 400 kV side of ICT, set such that
 - It does not pickup for fault on 220 kV bus
 - It does not pickup for transformer charging current
 - Time setting of **0.05 s** to 0.1 s can be considered.

DEF Setting Philosophy



- For 220 kV and 132 kV line with only one main distance protection, DEF (IDMT) must be set in such a way that it is coordinated with Zone 2 time
- For 400 kV line or where two main distance protection is used, DEF is used only for protection against high impedance faults and is coordinated with Zone 3 time
- For DEF at 400 kV side of ICT, it is to be set such that for fault at remote end bus (longest line), DEF (IDMT) is coordinated with Zone 3 time
- Instantaneous DEF can be used at 400 kV side of ICT, set such that
 - It does not pickup for fault on 220 kV bus
 - It does not pickup for transformer charging current
 - Time setting of **0.05 s** to 0.1 s can be considered.

Instantaneous Setting calculation



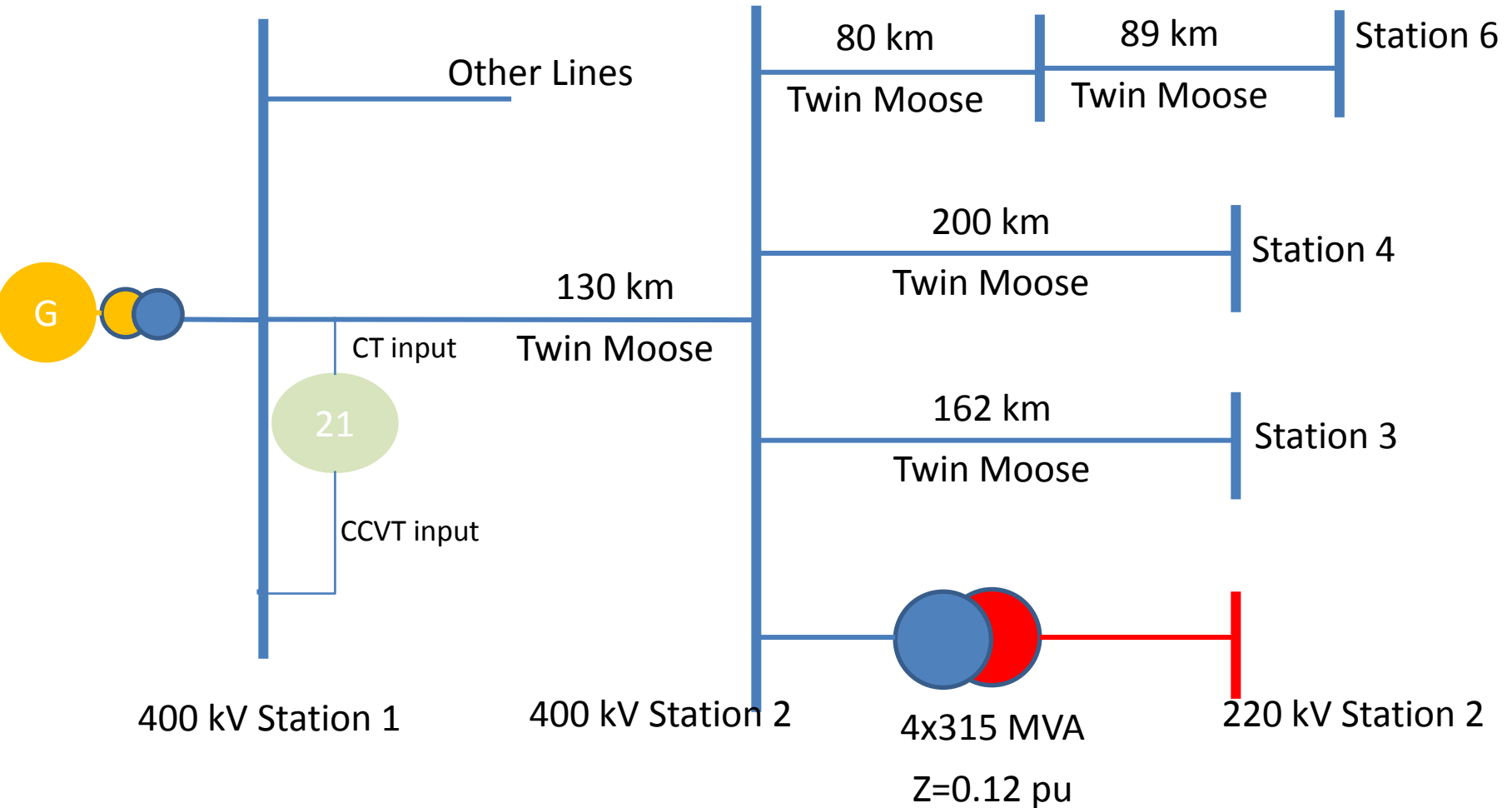
- Reflected Current = $1.3 * 3225 = 4195 \text{ A}$
- Inrush Current = $8 * 450 = 3600 \text{ A}$
- $I_p >> =$ Highest of the above two = 4200 A (Set value).



Distance relays

• Sample System

$R1 = 0.0297 \text{ } \Omega/\text{km}$
 $X1 = 0.332 \text{ } \Omega/\text{km}$
 $R0 = 0.161 \text{ } \Omega/\text{km}$
 $X0 = 1.24 \text{ } \Omega/\text{km}$
 $Zm = 0.528 \text{ } \Omega/\text{km}$





Zone 1

- Primary referred
 - $X1_{\text{prim}} = 0.332 * 130 * 0.8 = 34.5 \Omega$
- Secondary referred
 - $X1_{\text{sec}} = 34.5 * \text{CTR} / \text{PTR}$, CTR:CT Ratio, PTR: PT Ratio
- Operating Time: Instantaneous



Zone 2

- Protected line is single circuit
- Adjacent Shortest Line: 80 km to Station 5
- $X2_Prim = 0.332 * 130 * 1.2 = 51.79 \Omega$ (130+26 km)
- X2 covers only 32% of Adjacent Shortest Line.
- Operating Time : 0.35s

Zone 3



- Adjacent Longest Line is 200 km to Station 4
- $X3_Prim = 0.332 \times (130 + 200) \times 1.2 = 131.47 \, \Omega$
 - That is 130 km PL + additional 266 km
- Time Setting
 - Check if Zone 3 of PL encroach Zone 3 of adjacent line protection
 - Zone 3 of Station 2- Station 5 line is 202.8 km.
 - The Two Zone 3 are overlapping and hence must be time coordinated.
 - $Time = 0.8 + 0.06 (t_{cb}) + 0.03 (t_{reset}) + 0.06 (t_{sf}) = 0.95$ (set 1s)
 - t_{cb} , t_{reset} and t_{sf} values are as per CEA report



Points to be Considered

- Obtain the actual line parameters from line impedance test results. If not available, consider the standard values.
- Check Relay Setting type
 - Primary or secondary referred values
 - RX or Z_0
 - Computation of Zero sequence compensation factor. (K_0 , K_n or K_r - K_x)

$$k_0 = \frac{Z_0 - Z_1}{3Z_1} \quad k_n = \frac{Z_0 - Z_1}{Z_1} \quad k_r = \frac{R_0 - R_1}{3R_1} \quad k_x = \frac{X_0 - X_1}{3X_1}$$



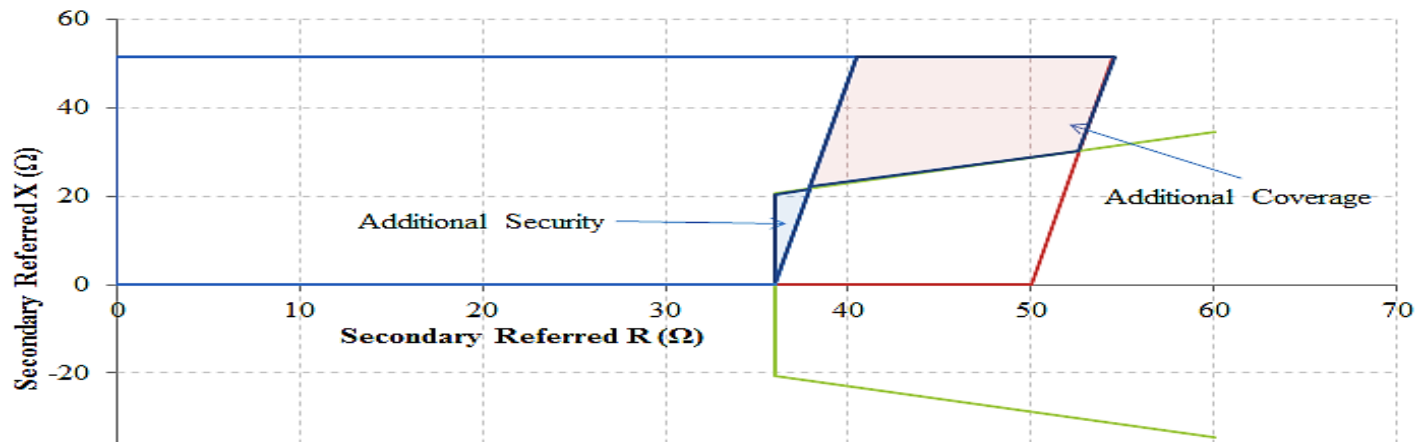
Points to be Considered

- Note the shortest and longest line emanating from the adjacent substation, along with impedance values
- For double circuit lines, check if it is two single circuit tower or one double circuit tower
- If necessary, carry out system study to study the effect of in feed, mutual coupling, power swing to achieve coordinated setting.



Load Encroachment Consideration

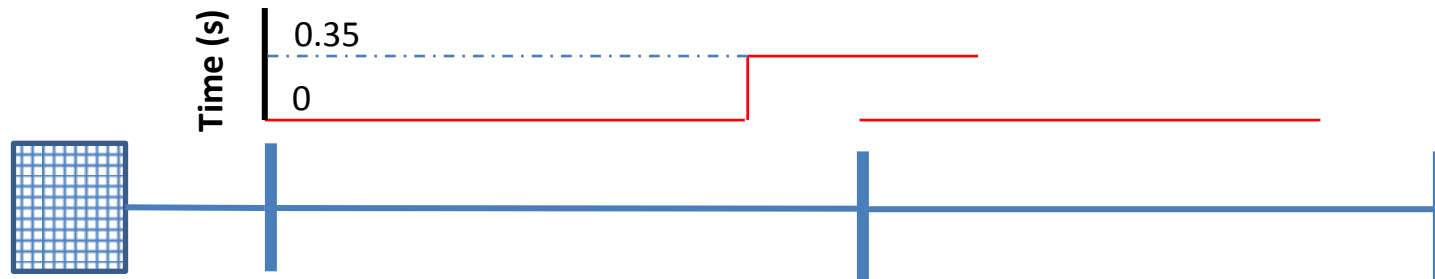
- Basic Check
 - Rated $V = 63.5$ V and Rated $I = 1$ A. (Secondary Referred)
 - Phase Impedance $= (0.85 \cdot V) / (1.5 \cdot I) = 36 \Omega$
 - R reach must always be less than 36Ω





Operating Time coordination

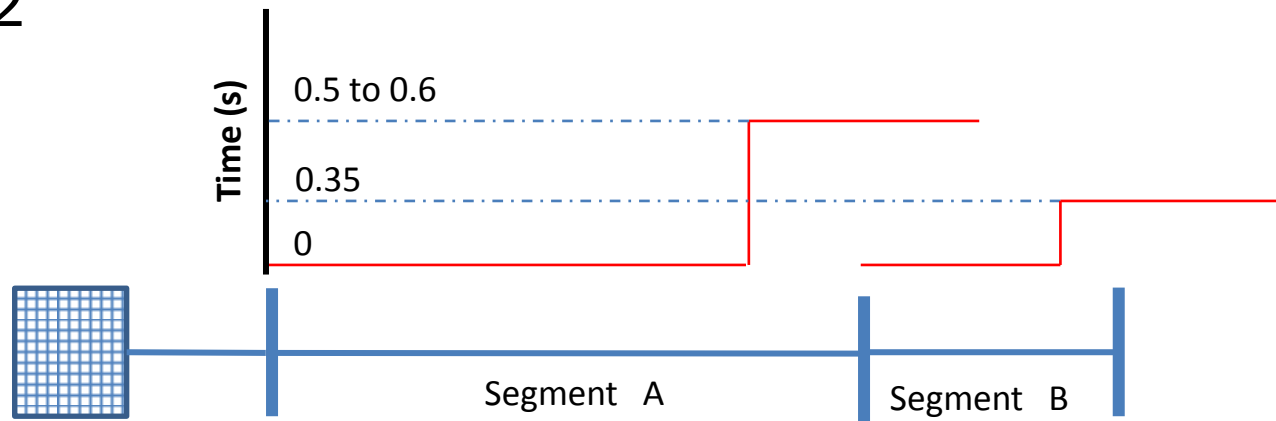
- Zone 1 is primary protection, hence instantaneous operation
- Zone 2 is a overreach zone and hence needs to be delayed.
 - If errors involved is less, then Zone 2 can trigger for Zone 1 fault of adjacent line. Hence Zone 2 is to be coordinated with Zone 1.



Operating Time Coordination



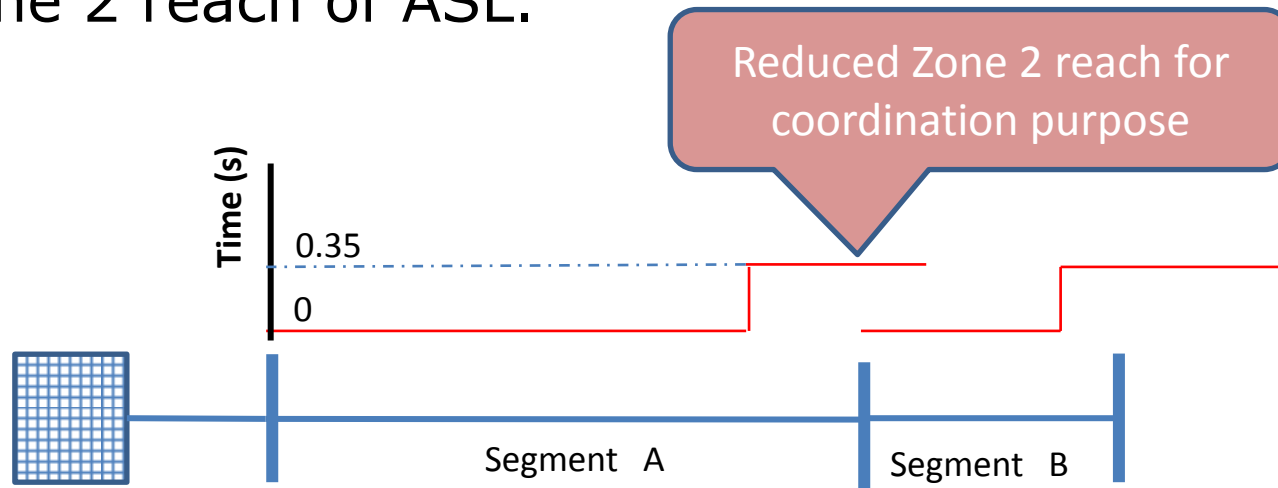
- For fault at 80% of segment B, Segment B zone 1 can also under reach by 20%
- Hence only Zone 2 of Segment B pick up
- Segment A Zone 2 can also pickup.
- Hence segment A Z2 to be coordinated with segment B Z2





Operating Time coordination

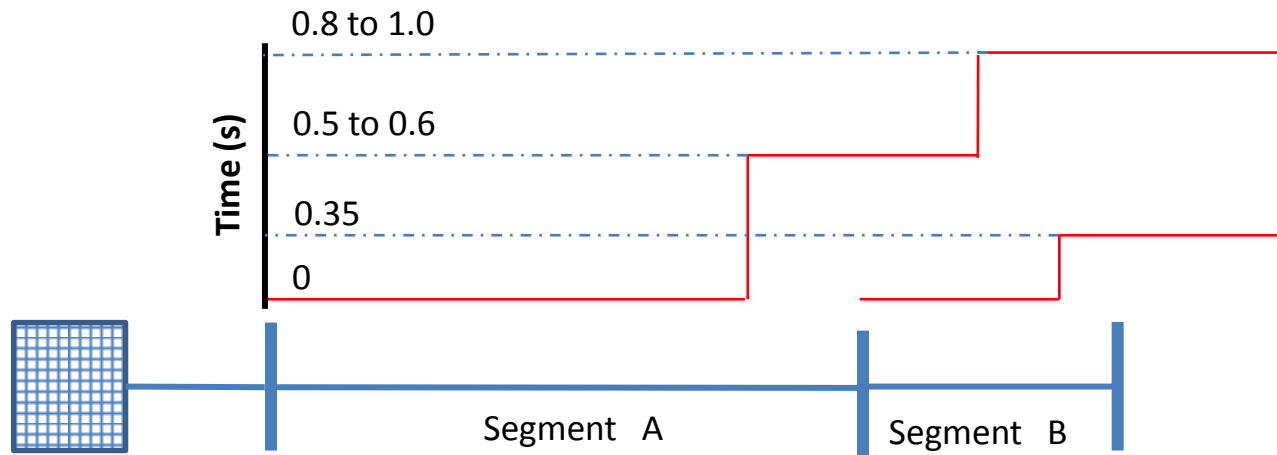
- For 220 kV and below, if Zone 2 of PL can encroach the Zone 2 of ASL, then coordination is achieved by reducing the Zone 2 reach of PL to coordinate with Zone 2 reach of ASL.





Operating Time coordination

- Zone 3 is the backup protection and hence needs to be operate after Zone 1 or Zone 2 has failed to clear the fault.
- Zone 3 is coordinated with Zone 2 time of adjacent line relay.





Load Encroachment Consideration

- Reach setting is given considering the various “under reach” effect that can occur. This makes the resistive setting “high”
- Phase loop measures the phase impedance and hence has to be set such that it does not trip for abnormal or emergency system loading condition
- Emergency loading condition is to be used to decide the load encroachment point.

Load Encroachment Consideration

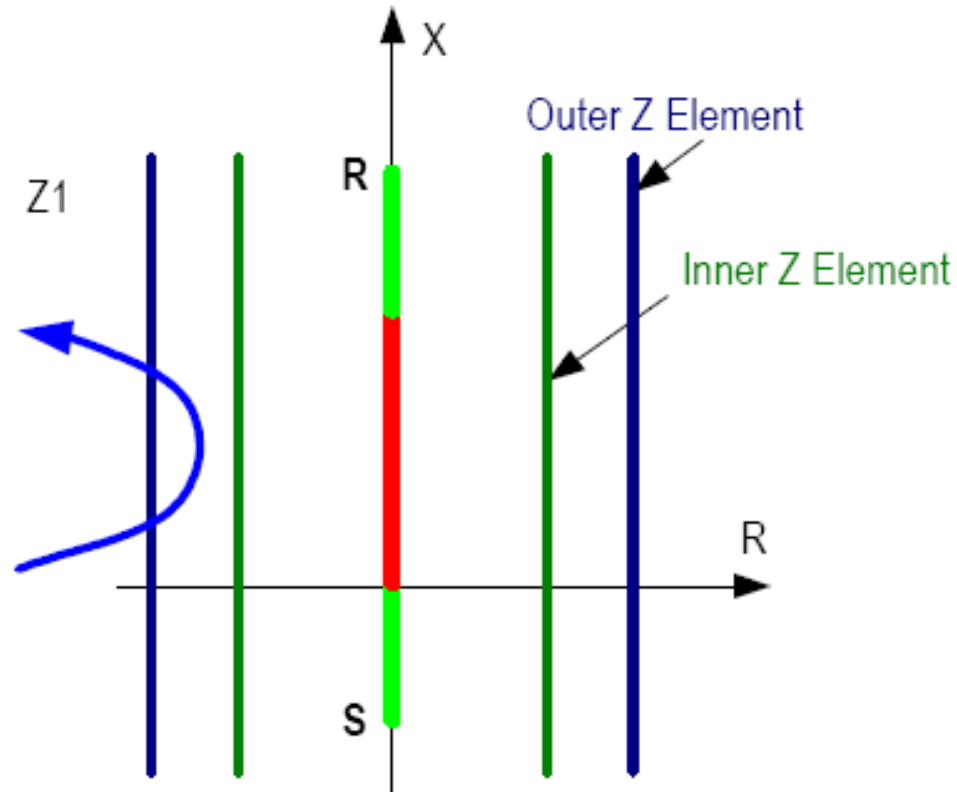
- Following criteria may be considered
 - 1.5 times the thermal rating of lineOR
 - 1.5 times associated bay equipment rating (minimum of all equipment)
 - Minimum voltage of 0.85 pu to be considered
- Load encroachment angle can be considered as 30° (approx. 0.85 pf)



Power Swing Blocking

- During power system disturbances, unbalance exist between generators which cause the operating point to oscillate
- R-X trajectory might enter the zones of protection
- Blinder schemes are traditionally used to detect swings and prevent unnecessary tripping
- The rate of change of impedance is used to differentiate between power swings and faults

Power Swing Blocking Schemes





PSB Options

No power swing blocking

Block all zones

Block zone 2 and higher

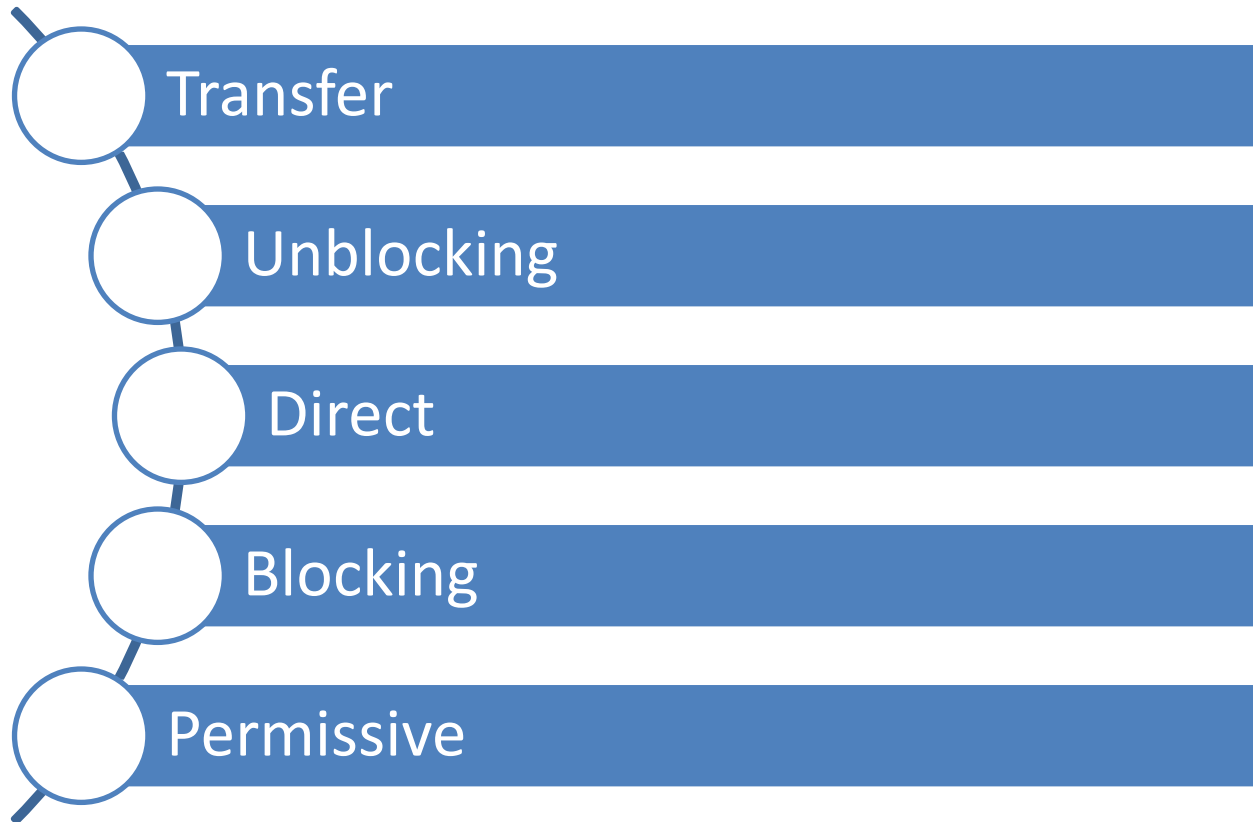
Block all zones but allow OST

Stability Studies for PSB Settings

- Identify the generators which are prone to instability and the lines where power swings are observed.
- Determine the location where system should be separated
- Time and reach settings are calculated
- Outermost zone reach should be within the inner boundary
- Outer boundary should be less than load impedance

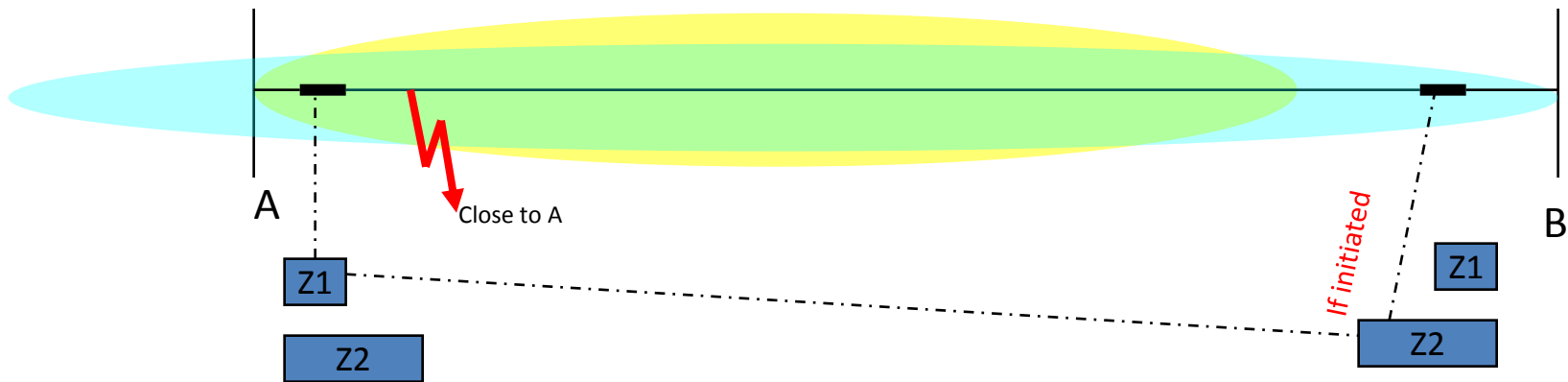


Carrier Aided Protection



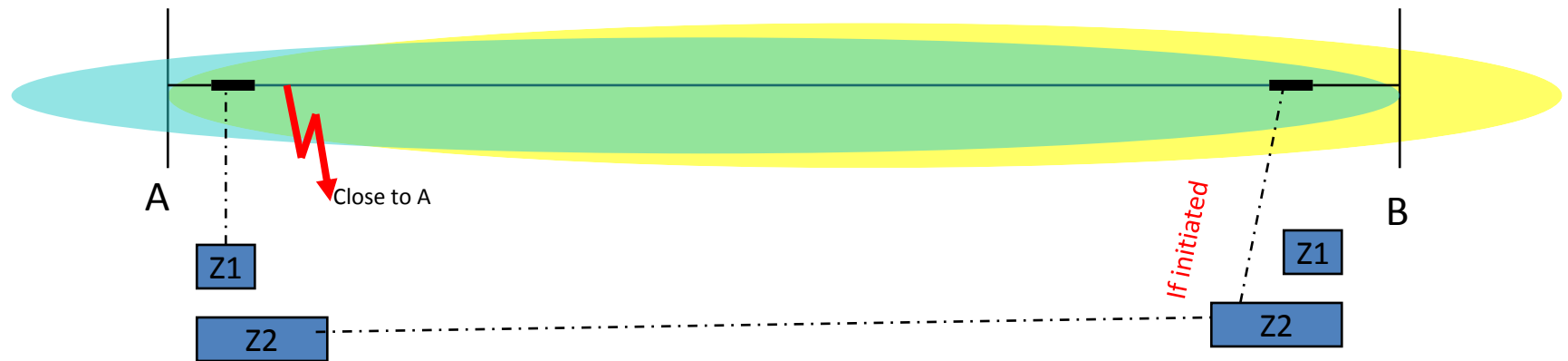


Permissive Under-Reach





Permissive Over-Reach





Queries & Discussions





Thank You





Principles of Unit Protection



Topics for Discussion

- Introduction to Unit Protection
- Differential Protection – Simple, Percentage Biased and High Impedance
- Applications
- Setting Examples

Introduction



Meaning

- Protection which responds to faults only in one zone
- No need for time grading
- Normally fast acting – not affected by fault severity
- Operates based on the comparison of boundary conditions



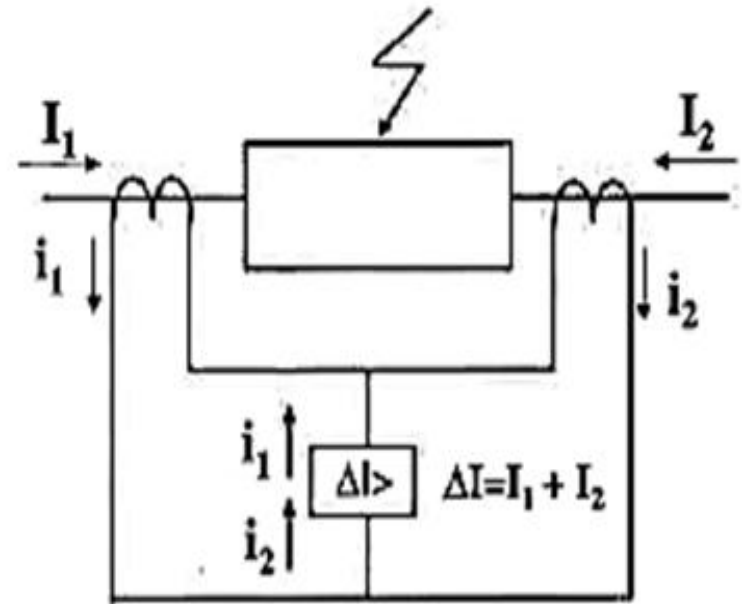
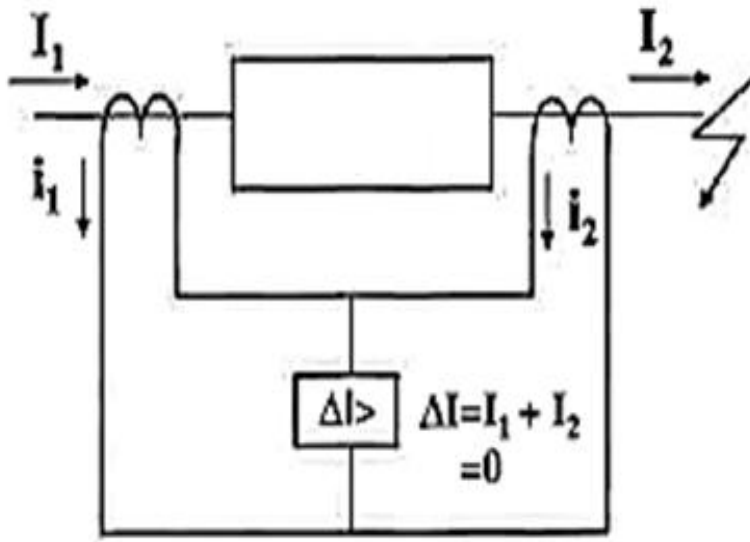
Types of Unit Protection

- Differential Protection
 - ✓ Utilizes Current
- Over-Fluxing Protection
 - ✓ Utilizes Voltage and Frequency
- Backup-Impedance Protection
 - ✓ Utilizes Current and Voltage



Differential Protection

Simple Differential Protection



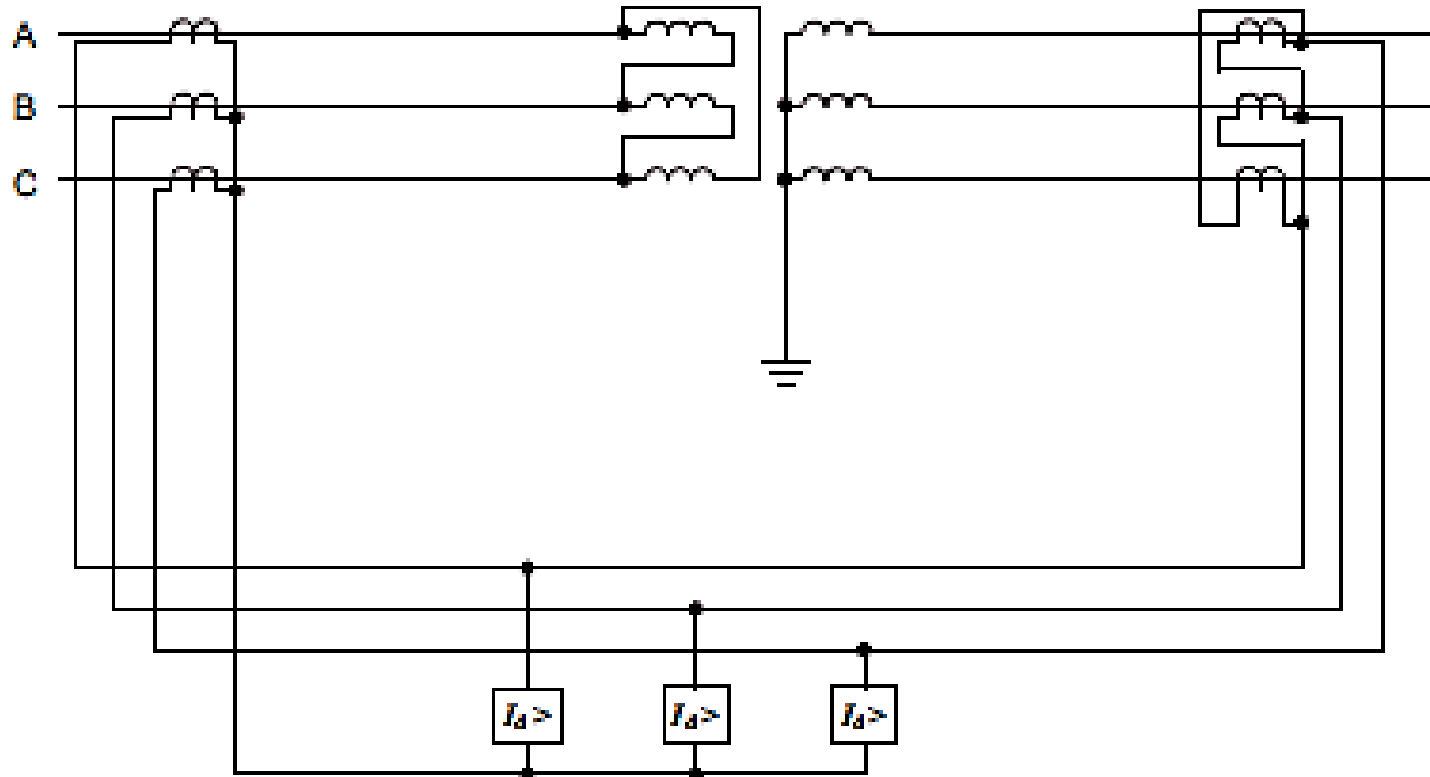


Setting Consideration

- The effect of magnetizing inrush during initial energization should be considered.
- Correction for possible phase shift across the transformer windings (phase correction)
- The effects of different earthing and winding arrangements (filtering of zero sequence currents)
- Correction for possible unbalance of signals from current transformers on either side of the windings (ratio correction)

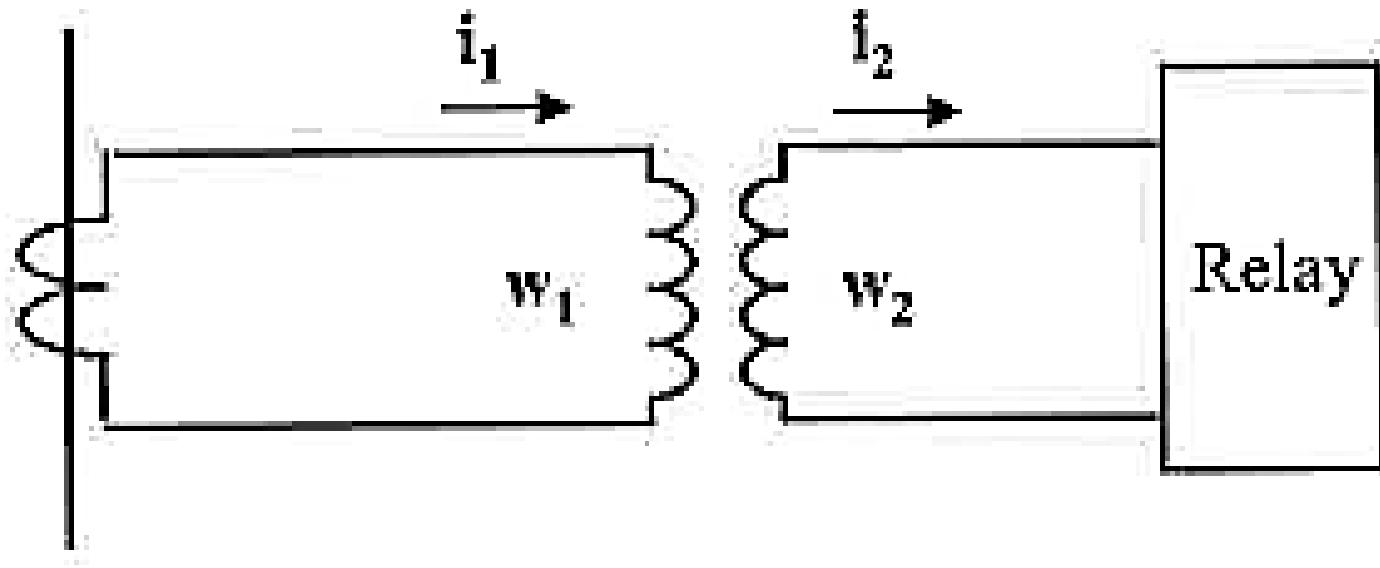


Phase Correction and Zero Sequence Filtering



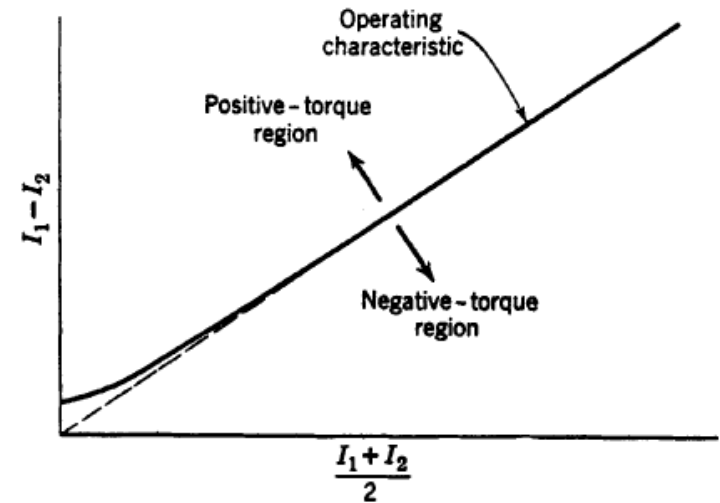
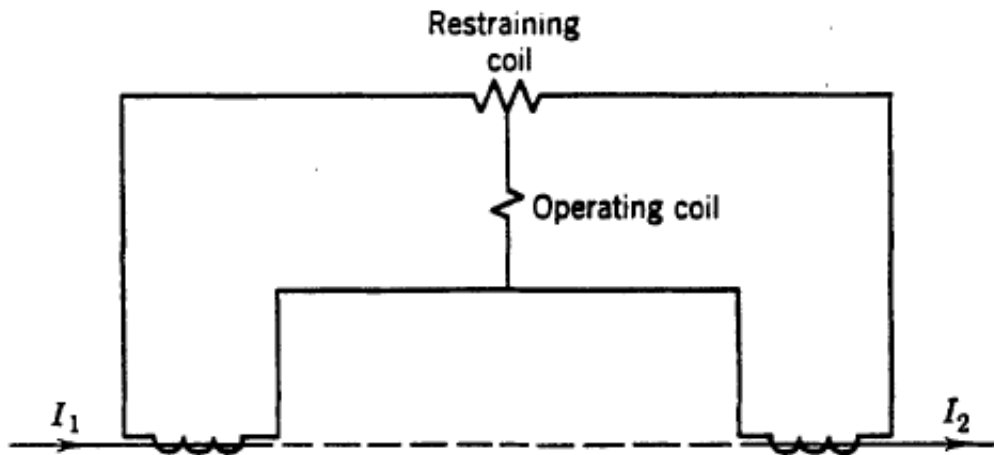


Ratio Correction





Biased Differential Relay





Requirement of Biased Relays

Errors which vary proportionally with the operating conditions such as:

- Errors due to transformer taps
- CT errors
- Ratio Mismatch – Difficulty in obtaining exactly similar currents in both secondaries

Transient Errors

- CT Saturation

Operating Characteristics



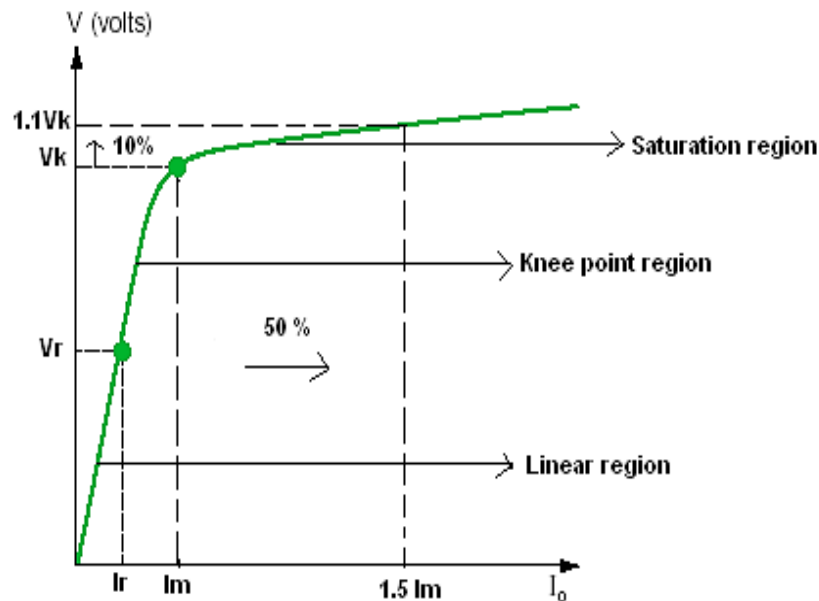
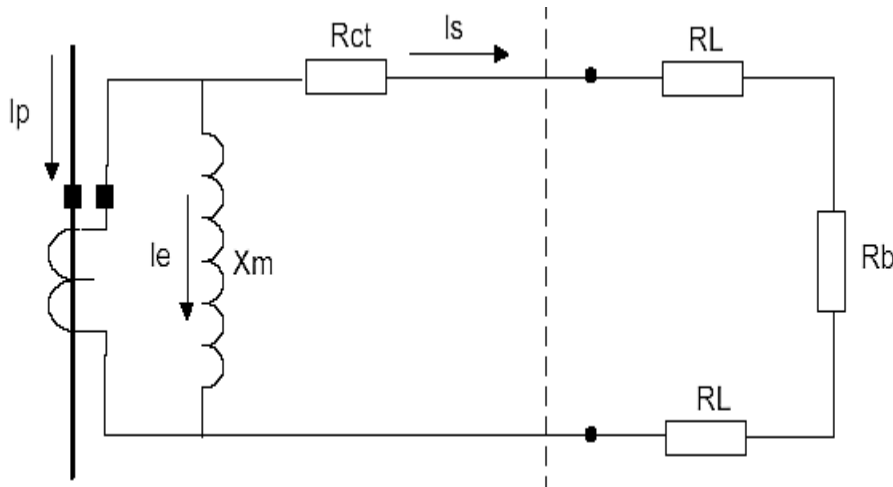
$$I_r = N_r * \frac{(I_1 + I_2)}{2}$$

$$I_o = N_o * (I_1 - I_2)$$

For relay operation,

$$I_o > K * I_r$$

Where, $K = \frac{N_r}{N_o}$



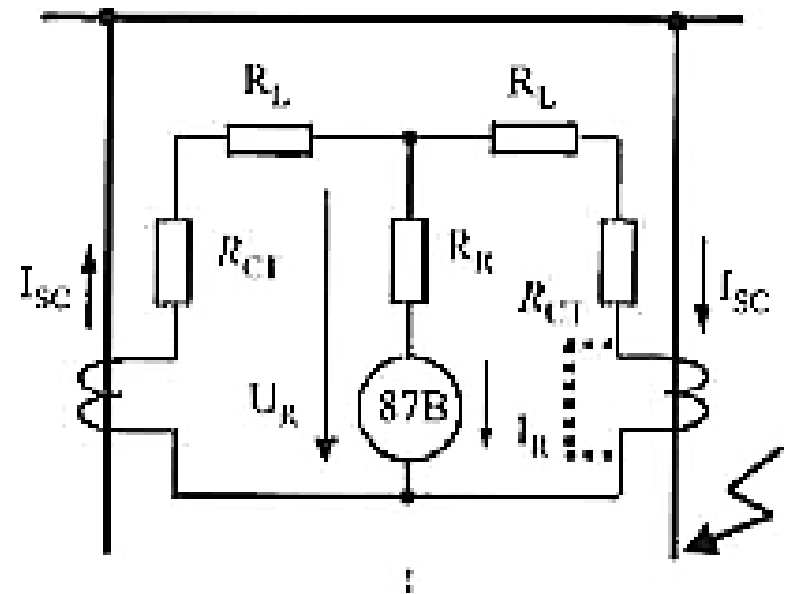
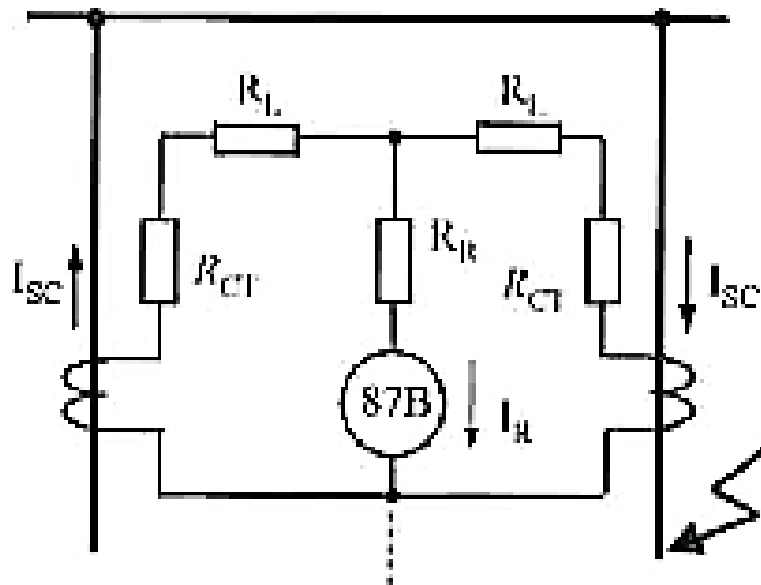
CT Saturation

- During CT saturation magnetizing impedance = zero
- Infinite magnetizing current will flow in the shorted path.
- Secondary of the network acts as open circuit.
- During this situation secondary current $I_s = \text{zero}$





High Impedance Differential Protection



Comparison of Differential Schemes



Low Impedance

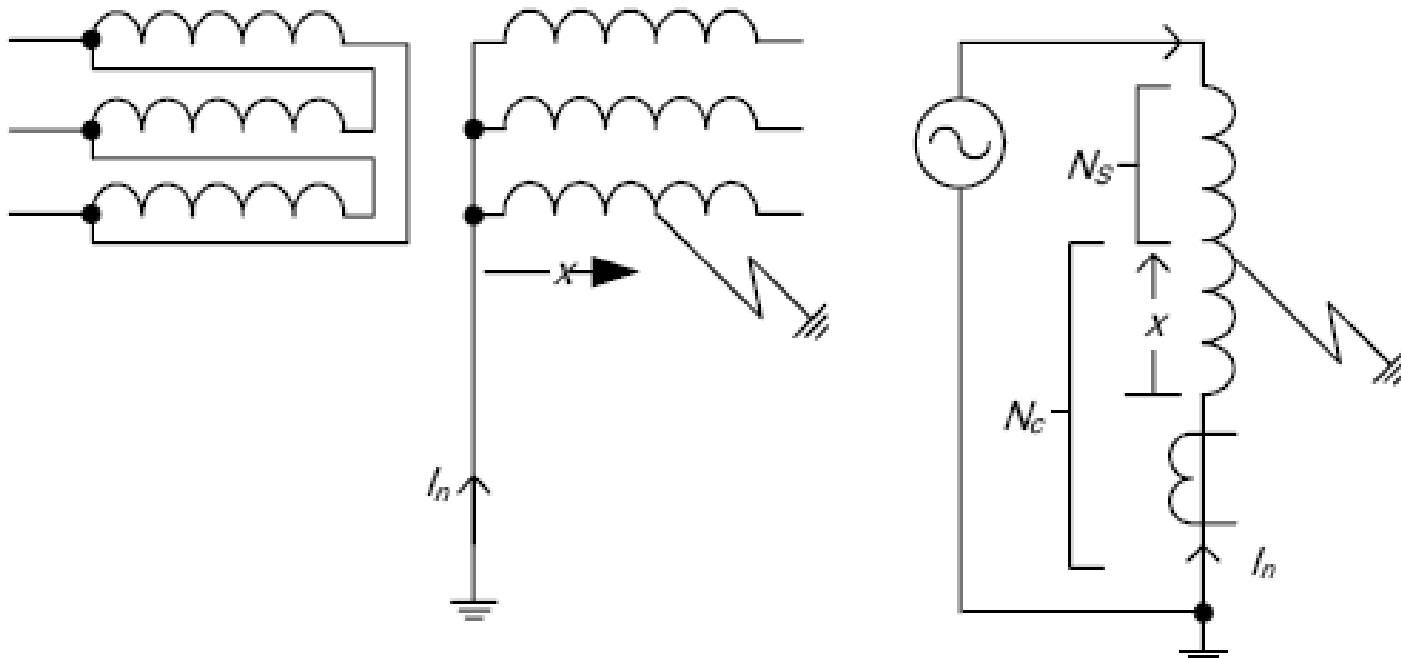
- Identical CTs not required
- Not stable for CT Saturation for external faults
- No protection for over-voltage required

High Impedance

- Stable for CT saturation for external faults
- Identical CTs are preferred for sensitive operation
- May require an MOV to protect Relay against voltage developed during external faults

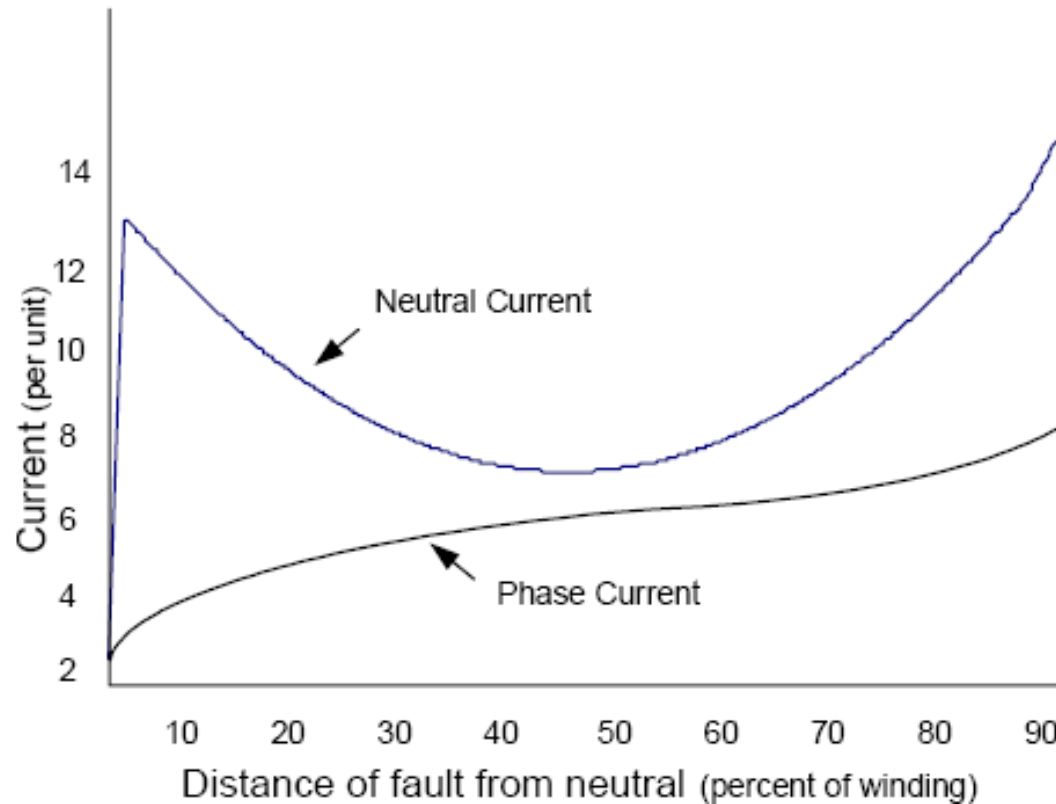


Restricted Earth Fault Protection



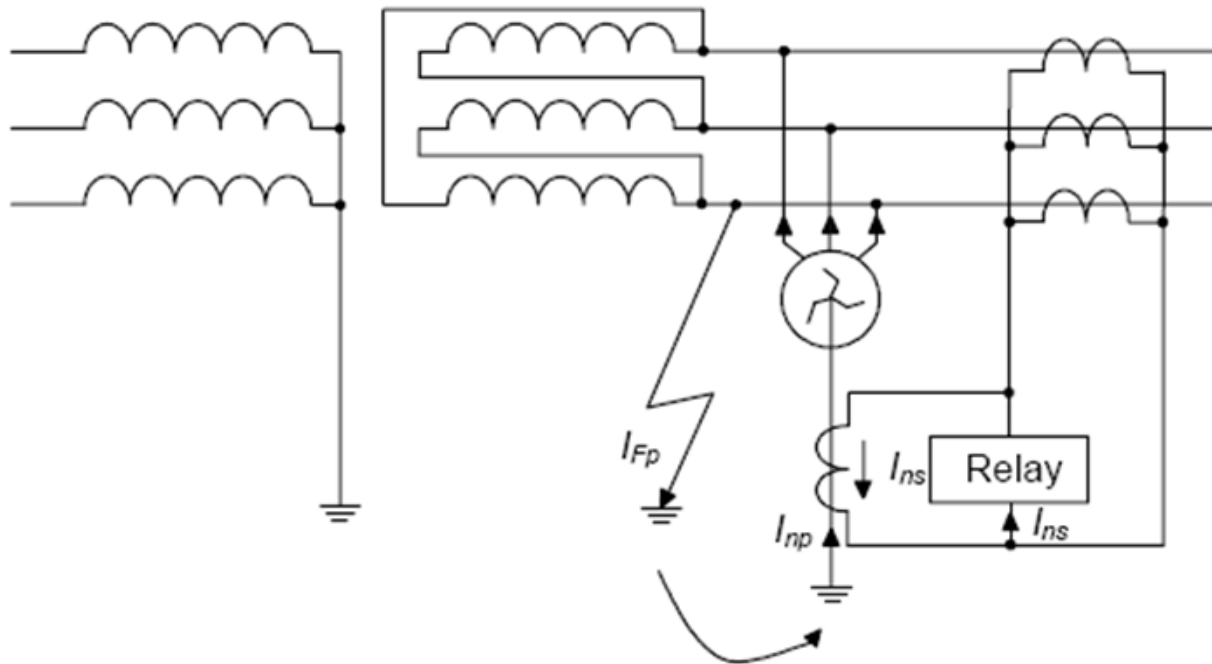


Amplification of Neutral Current





Currents During an Internal Fault



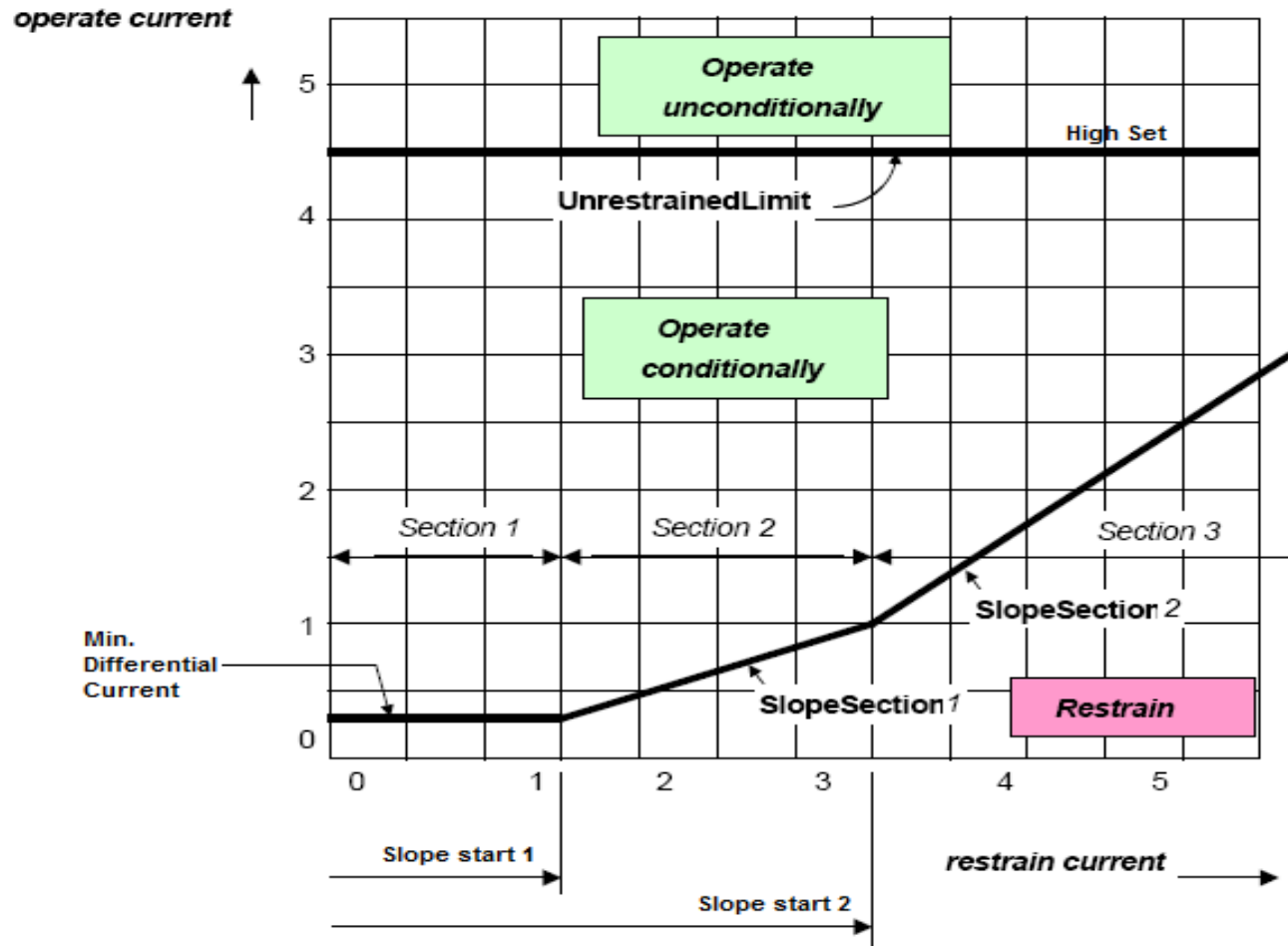


Applications

Transformer Protection

- Differential Relays
 - ✓ Mainly percentage biased relays
 - ✓ 2nd and 5th harmonic restraints are provided
 - ✓ High Set may be provided on HV winding
- Restricted Earth Fault Relay
 - ✓ High Impedance Schemes are popular

Modern Day Transformer Protection





Line/Cable Protection

Differential Protection

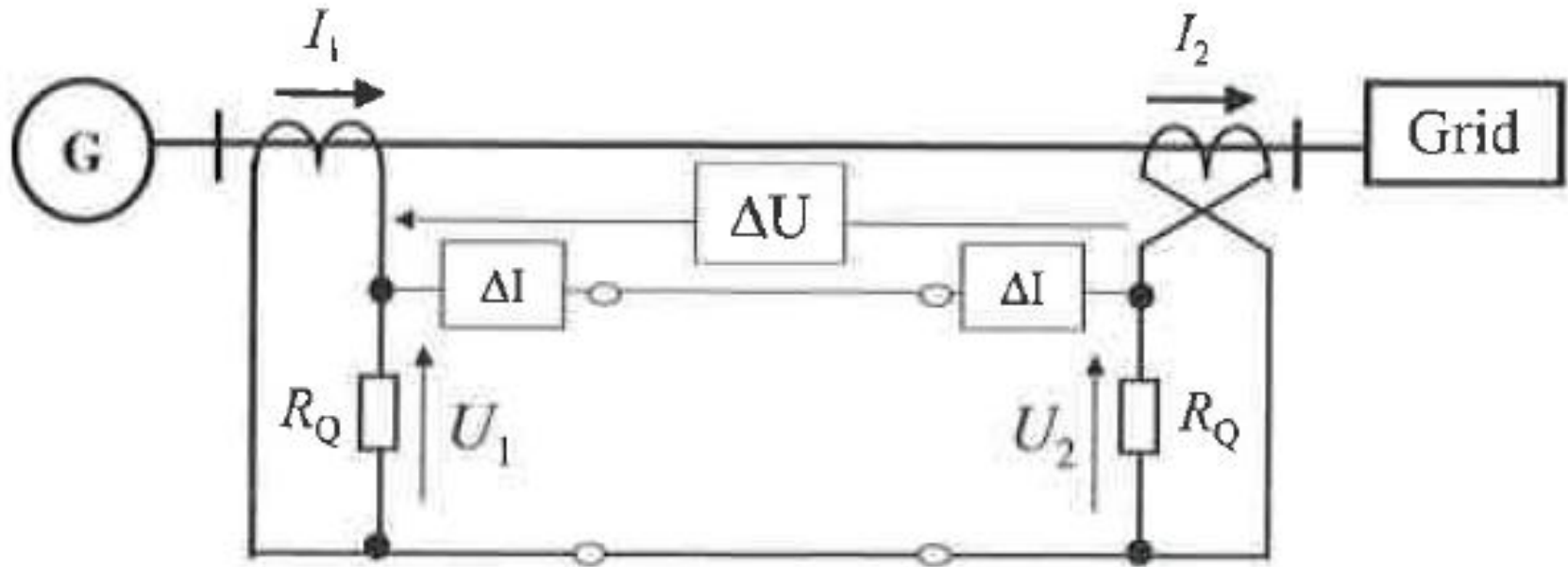
- Percentage biased schemes are used
- Inrush currents are considered
- Major challenge was the distance between two ends

Pilot Wire Protection

- Measurements communicated over the pilot wire
- Balanced voltage as well as circulating current schemes are used



Balanced Voltage Scheme





Comparison of Pilot Wire Schemes

Balanced Voltage

- Works on the tripping principle
- Interruption to the pilot wires causes blocking
- Short circuit of pilot wires leads to tripping
- Overcurrent protection required to prevent incorrect tripping due to short circuit of pilot wires

Circulating Current

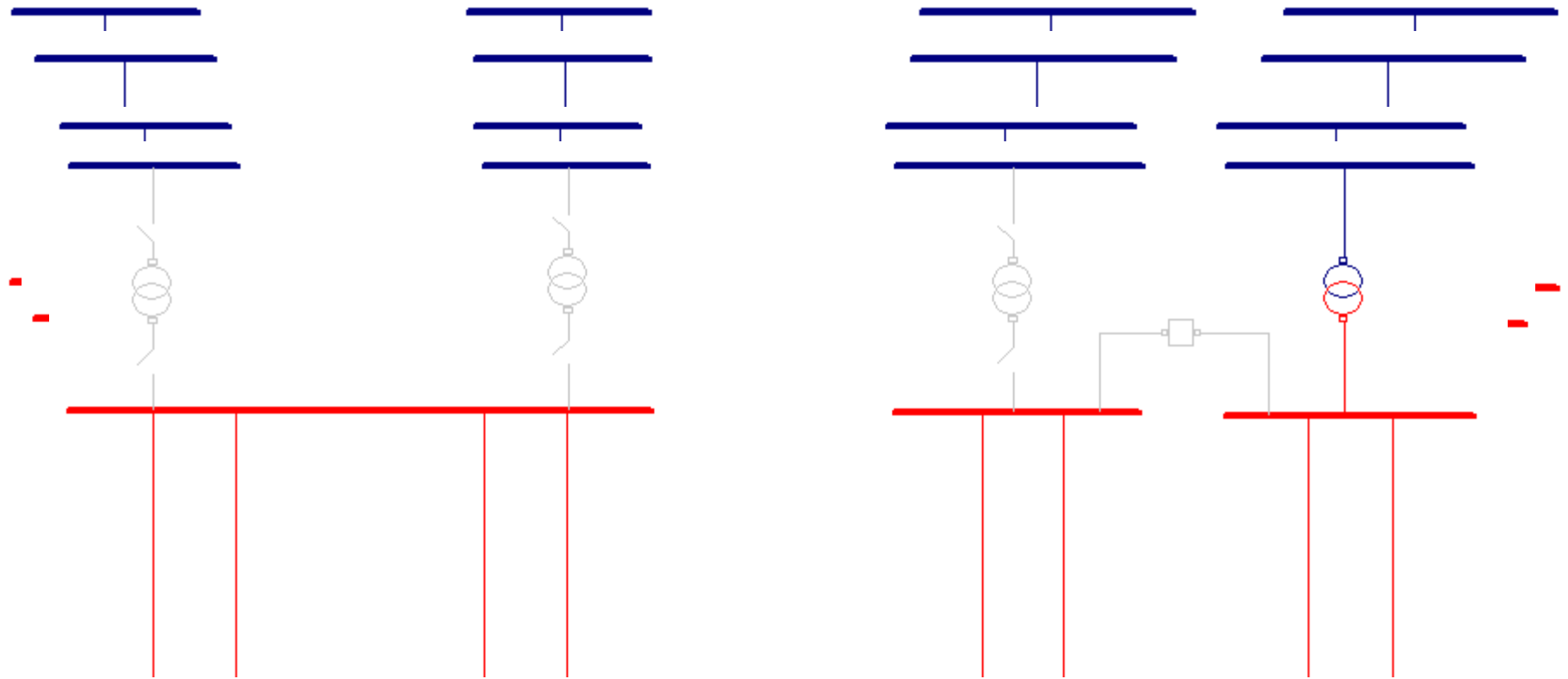
- Works on blocking principle
- Interruption of the pilot wires causes tripping
- Short circuit of pilot wires leads to blocking
- Overcurrent protection required to block operation for large currents due to pilot wire interruption



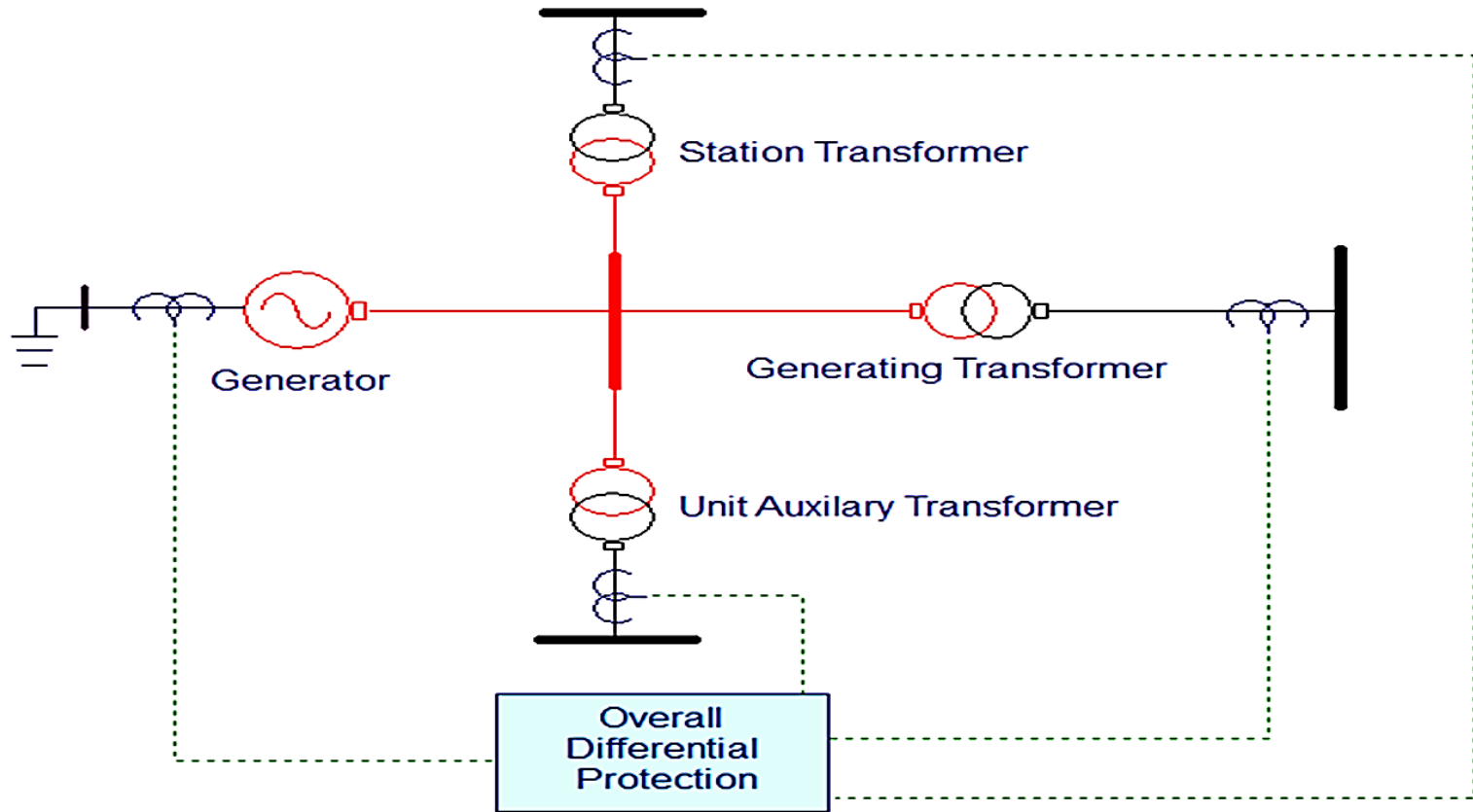
Bus-Bar Protection

- Differential Schemes
 - ✓ Incoming and outgoing currents are balanced
 - ✓ Multiple CT connections
 - ✓ Both High and Low Impedance Schemes are used
- Partial Bus Bar Relay
 - ✓ Retention of supply to healthy portion of the network

Partial Bus Bar Relay Example



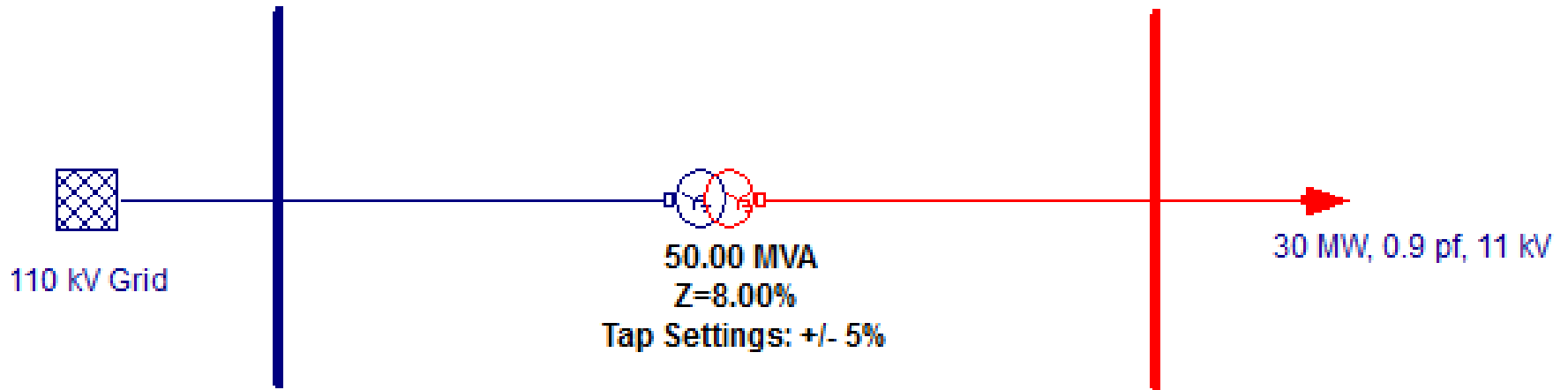
Overall Differential Protection





Setting Examples

Sample Network





General Parameters

Parameter	Value	Unit
Mid tap Voltage in %	0	
Primary side Full load Current at Mid tap Voltage	262.4319405	A
Secondary side Full load current	2624.319405	A



Secondary Ratio Compensation

Parameter	Value	Unit
Secondary side Full load Current on CT secondary	0.874773135	A
Secondary side ratio compensation	1.143153533	
Secondary Full load CT secondary current with ratio correction	1	A



Primary Side Ratio Compensation

Parameter	Value	Unit
Primary full Load current At Maximum tap Voltage	249.9351815	A
Primary full Load current At Minimum tap Voltage	276.2441479	A
Primary side Full load Current on CT secondary side at Mid tap Voltage	0.874773135	A
Primary full Load current on CT secondary side At Maximum tap Voltage	0.833117272	A
Primary full Load current on CT secondary side At Minimum tap Voltage	0.920813826	A
Primary side ratio compensation	1.143153533	



Differential Current Computation

Parameter	Value	Unit
Primary full Load current on CT secondary with ratio correction At Maximum tap Voltage	0.952380952	A
Primary full Load current on CT secondary with ratio correction At Minimum tap Voltage	1.052631579	A
Differential current at maximum tap	0.047619048	A
Differential current at minimum tap	0.052631579	A



Restraint Current Calculation

Parameter	Value	Unit
Restraint current at maximum tap	0.976190476	A
Restraint current at minimum tap	1.052631579	A
Setting Error at maximum tap	4.87804878	%
Setting Error at minimum tap	5.00	%

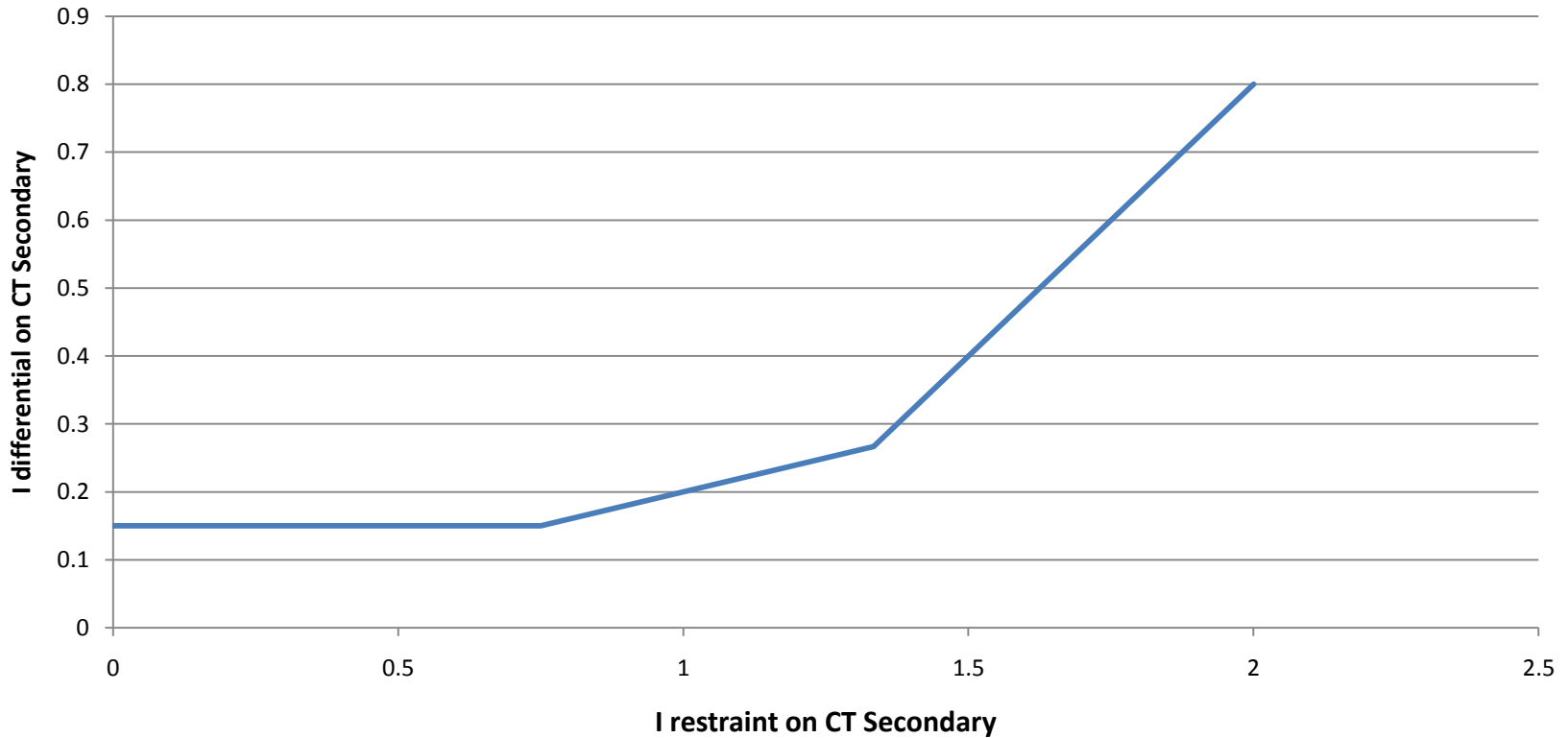


Relay Settings

Setting	Value	Unit
Min Current	0.15	A
Slope 1 Start	0.75	A
Slope 1	20	
Slope 2 Start	1.33	A
Slope 2	75	
High Set	12.5	A



Relay Characteristics





REF - CT Selection

- The voltage across the stabilizing resistor at maximum through fault current is given by

$$V_s = k \cdot I_{kmax} \cdot (R_{CT} + 2 \cdot R_L) / n \text{ volts}$$

Where:

R_{CT} = current transformer secondary winding resistance

R_L = One way maximum lead resistance from the CT to the relaying point

I_{kmax} = maximum external fault current

k = stabilizing factor used to account for the distorted voltage wave due to faults.

n = transformation ratio of the CT

- **The knee point voltage of the CTs should be chosen at least 2 times the stability voltage setting**



REF - Voltage Settings Considerations

- Always, relay operating voltage should be less than $V_k/2$ but more than V_s .
- If stability voltage increases beyond V_k , CT enters saturation region for which there is infinite Magnetization (Current), but voltage remains at the same level (no huge change in voltage). This condition is seen as open circuited on the secondary.
- $V_{set} > V_s$, such that relay will not operate for external fault with CT saturation condition.

REF - Stabilizing Resistor Design



- The value of the I_{prim} at which the relay operates at certain settings can be calculated as follows:

$$I_{\text{prim}} = n * (I_r + m * (V_s / V_k) * I_o) \text{ A}$$

Where,

n = the transformation ratio of the current transformer

I_r = the current value representing the relay setting

m = the number of current transformers included in the

protection

I_o = the magnetizing current of one current transformer at knee point voltage, V_k .

- The relay setting current I_r can be computed as

$$I_r = (I_{\text{prim}} / n) - m * (V_s / V_k) * I_o \text{ A}$$

- The setting of the stabilizing resistor (R_s) must be calculated in the following manner, where the setting is a function of the required stability voltage setting (V_s) and the relay current setting (I_r).
- Stabilizing Resistor value, **$R_s = V_s / I_r$**



REF - Metrosil Requirement

- The following equations should be used to estimate the peak transient voltage that could be produced for an internal fault.

$$V_p = 2 * \sqrt{2 \cdot V_k(V_f - V_k)} \text{ volts}$$

$$V_f = I_f * (R_{CT} + 2 \cdot R_L + R_s) \text{ volts}$$

Where:

V_p = Peak voltage developed by the CT under internal fault conditions.

V_k = Current transformer knee-point voltage.

V_f = Maximum voltage that would be produced if CT saturation did not occur.

I_f = Maximum internal secondary fault current.

R_{CT} = Current transformer secondary winding resistance.

R_L = One way maximum lead burden from current transformer to relay.

R_s = Stabilizing resistor.



Queries & Discussions





Thank You

